

# Binary Models for Motor-Imagery Brain—Computer Interfaces: Sparse Random Projection and Binarized SVM

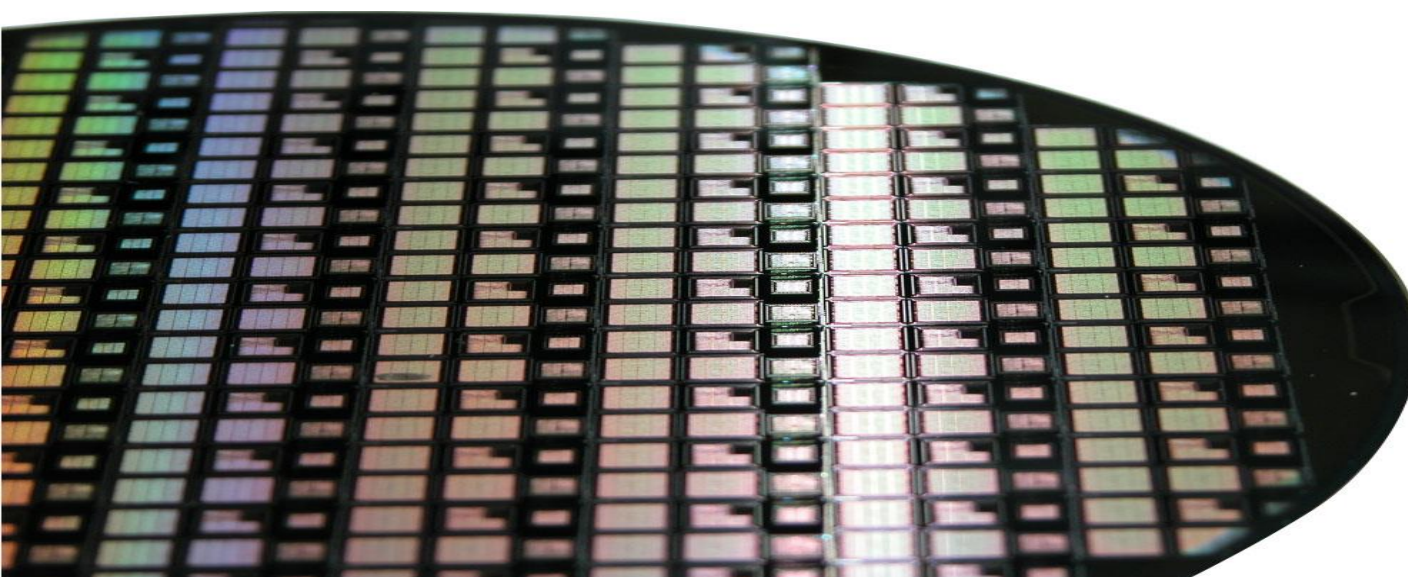


4 September 2020

**Michael Hersche**

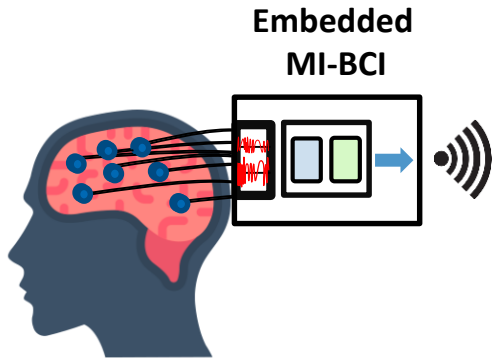
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# Towards wearable embedded Motor-Imagery Brain – Computer Interfaces (MI-BCIs)



## Why embedded MI-BCI?

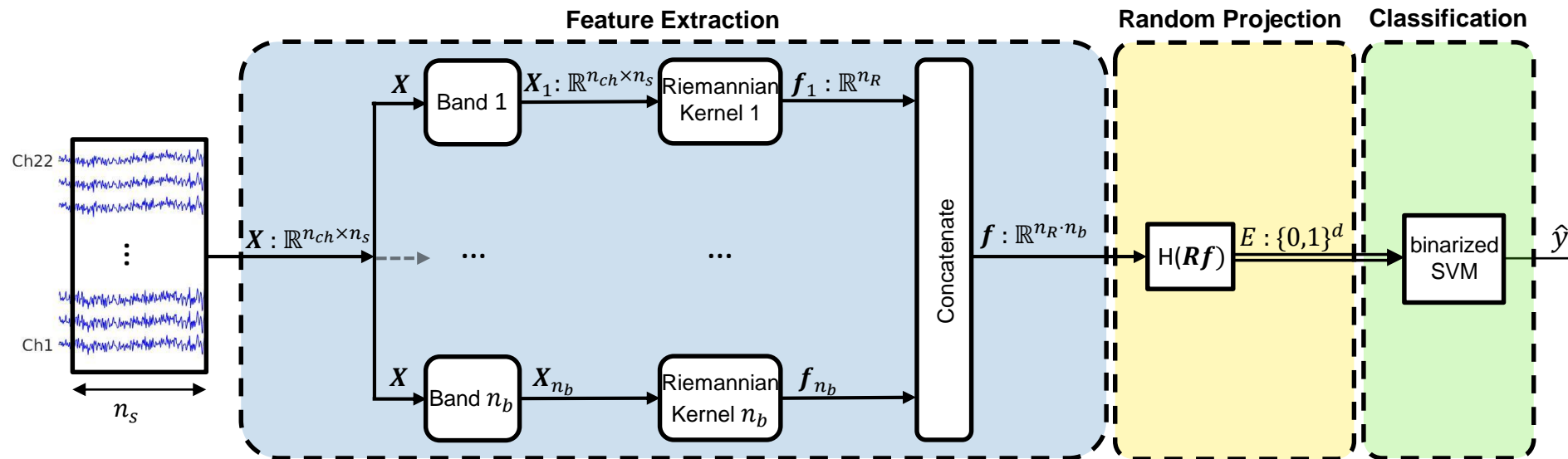
- User comfort
- Latency
- Security & privacy
- Long battery lifetime

## Challenges for embedding

- Complexity
- Memory requirements of model

# This work reduces the MI-BCI model size with random projection and binarized SVM

- Project Riemannian features to binary space with **random projection**
- Novel **binarized SVM** for classification
- Test on two different MI datasets
- Reduce the model size by **1.5-1.9x** with less than 1.27% accuracy loss



# We test our models on two MI datasets

## 4-class: BCI Competition IV-2a

- 9 subjects
- 2 sessions per subject on 2 days: training and test set
- 288 trials per session and subject
- 4 MI tasks initiated by visual cue
  - Left hand/right hand/feet/tongue
- 22 EEG channels sampled with 250 Hz

## 3-class: Saeedi et al. [1]

- 5 subjects
- 4 sessions per subject on same day
  - 4-fold cross validation: 3 sessions for training and one for testing
- 45 trials per session and subject
- 3 MI tasks
  - Left hand/right hand/feet
- 16 EEG channels sampled with 512 Hz

[1] Saeedi, et al. "Adaptive Assistance for Brain-Computer Interfaces by Online Prediction of Command Reliability." *IEEE Computational Intelligence Magazine*. 2016.

# Riemannian covariance method extracts features in unsupervised manner

- Spatial covariance matrix:

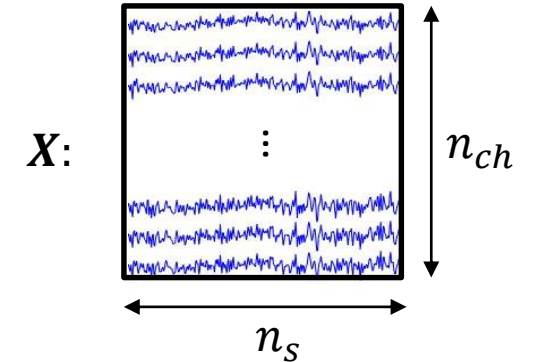
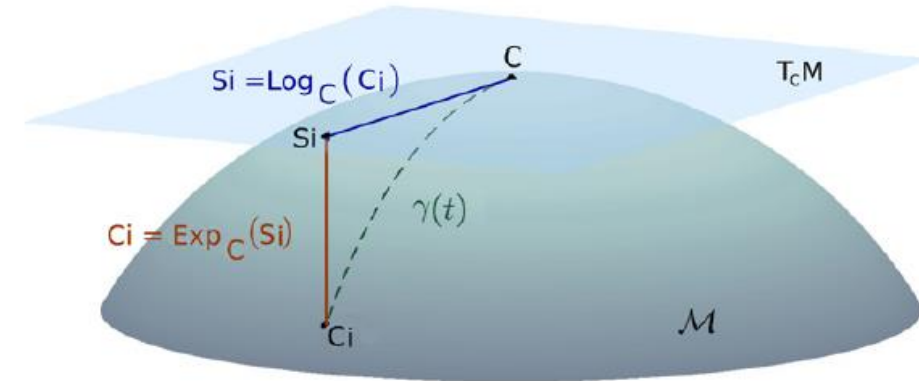
$$\mathbf{C} = \mathbf{X}\mathbf{X}^T + \rho\mathbf{I} \quad \mathbf{C} \in \mathbb{R}^{n_{ch} \times n_{ch}}$$

- Riemannian kernel:

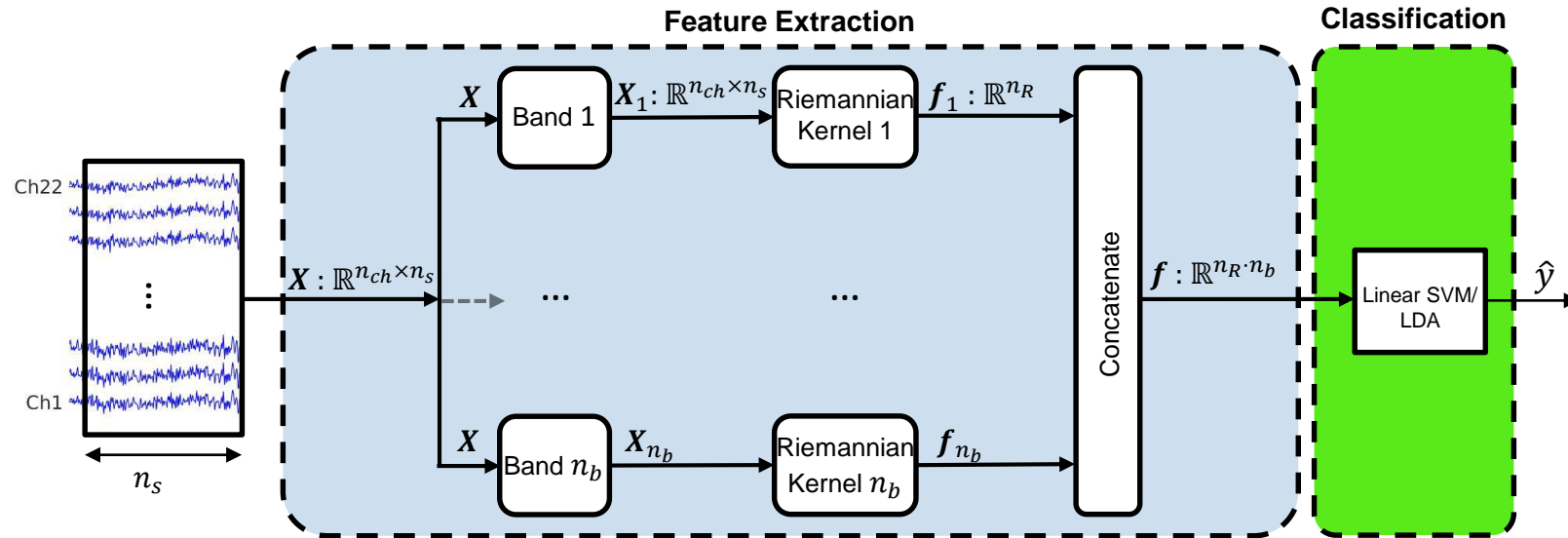
$$\tilde{\mathbf{C}} = \text{logm}(\mathbf{C}_{ref}^{-1/2} \mathbf{C} \mathbf{C}_{ref}^{-1/2})$$

- Reference matrix  $\mathbf{C}_{ref}$  average over all covariance matrices in training (**unsupervised**)
- Half vectorization yields  $n_R = n_{ch}(n_{ch} + 1)/2$  features:

$$\mathbf{f} = \text{vect}(\tilde{\mathbf{C}})$$



# State-of-the-art linear SVM or LDA on multi-spectral Riemannian features



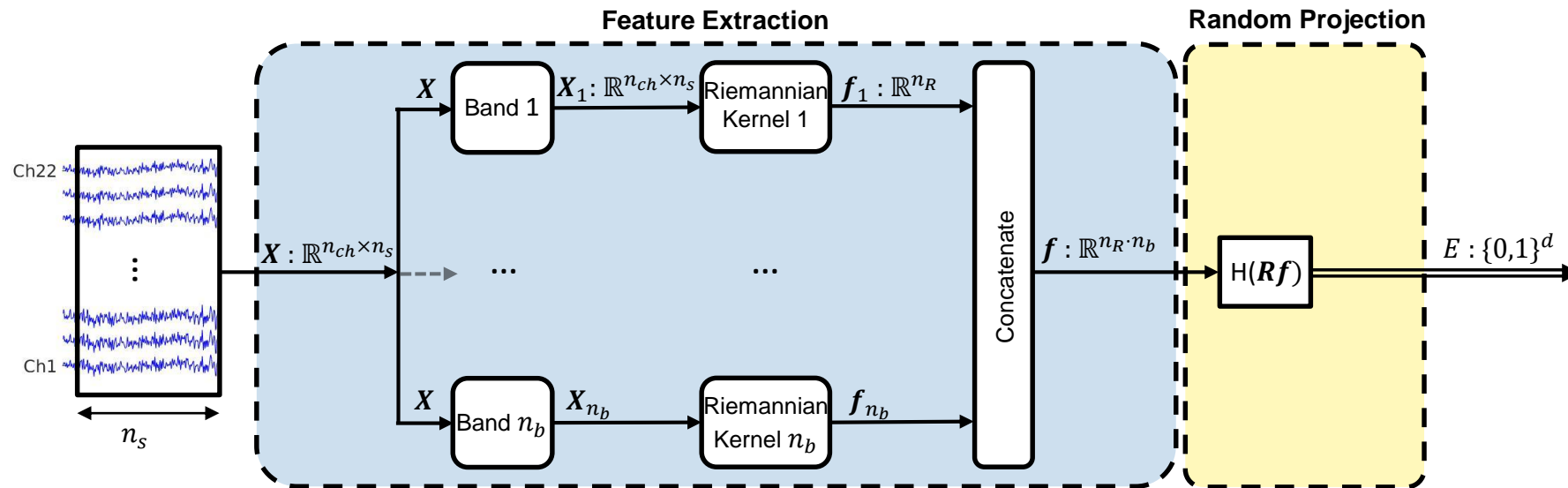
## 4-class MI

- $n_b = 43$  multiscale frequency bands
  - $n_R = \frac{22(22+1)}{2} = 253$  features/band
- => Total 10879 features**

## 3-class MI

- $n_b = 13$  frequency bands
  - $n_R = \frac{16(16+1)}{2} = 136$  features/band
- => Total 1768 features**

# Sparse bipolar random projection encodes feature vector to binary space



# Sparse bipolar random projection encodes the whole feature vector at once

$$E = H(Rf)$$

$$E \in \{0,1\}^d$$

- Elementwise Heaviside function  $H(\cdot)$
- Sparse bipolar random projection matrix

$$\mathbf{R} \in \mathbb{R}^{d \times d} \quad \mathbf{R}_{i,j} = \begin{cases} 1, \text{ w. p. } s/2 \\ 0, \text{ w. p. } 1 - s \\ -1, \text{ w. p. } s/2 \end{cases}$$

- 90% of the elements in  $\mathbf{R}$  are 0

## Implementation of random projection

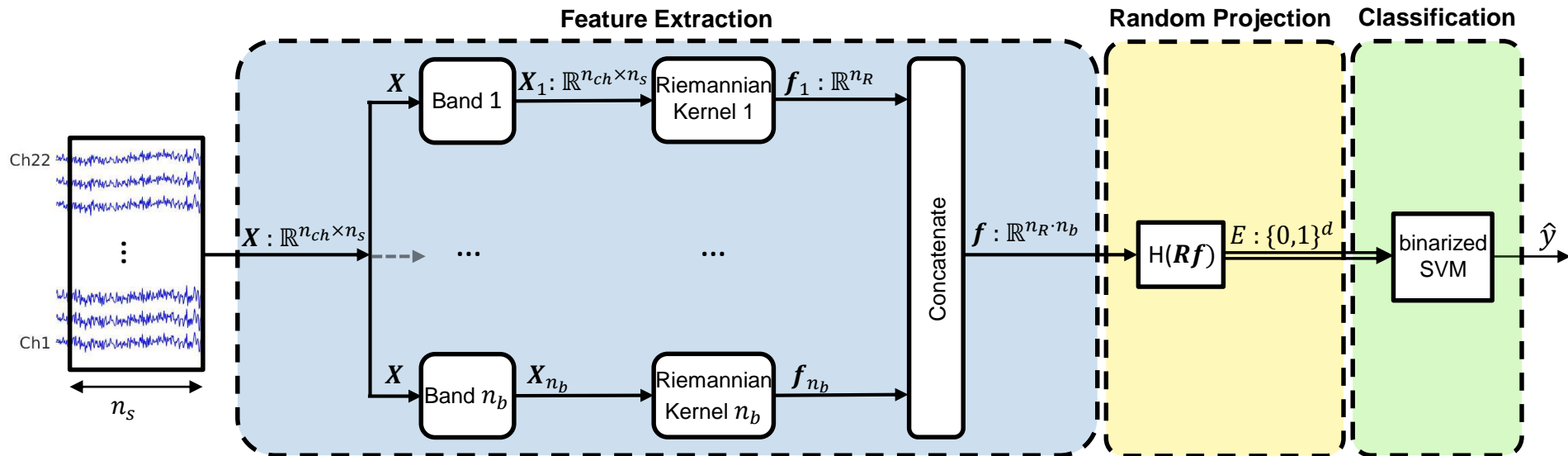
- Traditional processor-based computation
  - $\mathbf{R}$  regenerated with on device random number generator
- Memristors [2]
- Optical devices [3]

[2] Du, et al. "Reservoir computing using dynamic memristors for temporal information processing." *Nature Communications*. 2016.

[3] Saade, et al. "Random projections through multiple optical scattering: Approximating Kernels at the speed of light." *IEEE ICASSP*. 2016



# Binarized SVM for classification of projected binary features with Hamming distance



# Key contribution: binarized SVM for classification of projected binary features with Hamming distance

Decision function original linear SVM

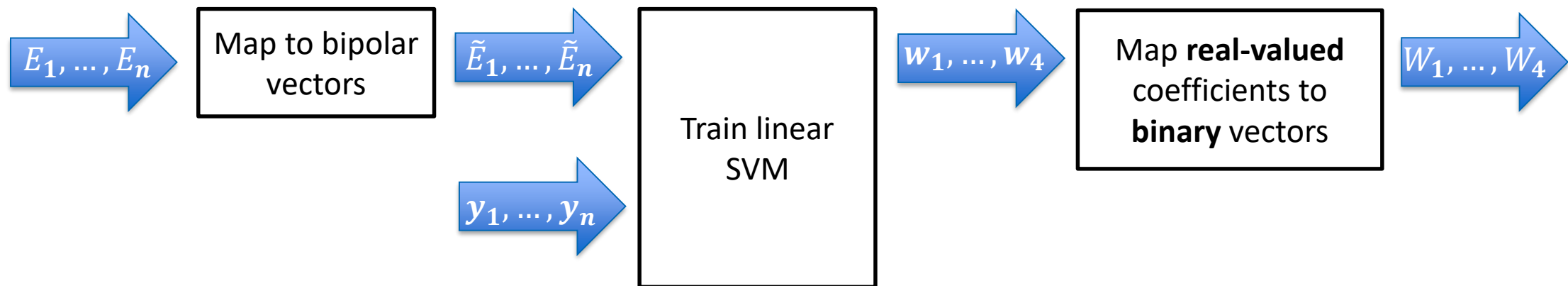
$$\hat{y} = \operatorname{argmax}_{i=\{1,2,3,4\}} \langle \mathbf{f}, \mathbf{w}_i \rangle + b_i$$

$\mathbf{w}_i$ : support vector  
 $b_i$ : bias

Decision function new **binarized SVM**

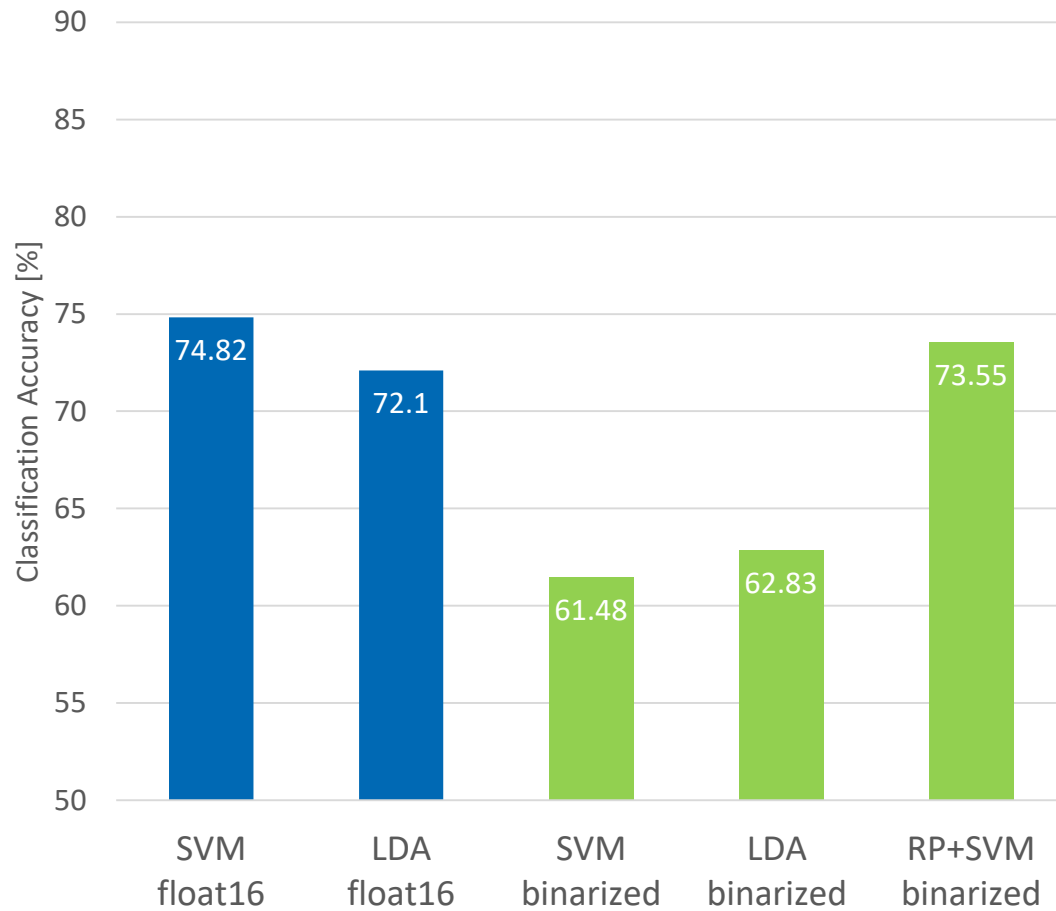
$$\hat{y} = \operatorname{argmin}_{i=\{1,2,3,4\}} d_h(E, W_i)$$

$W_i$ : binary support vector

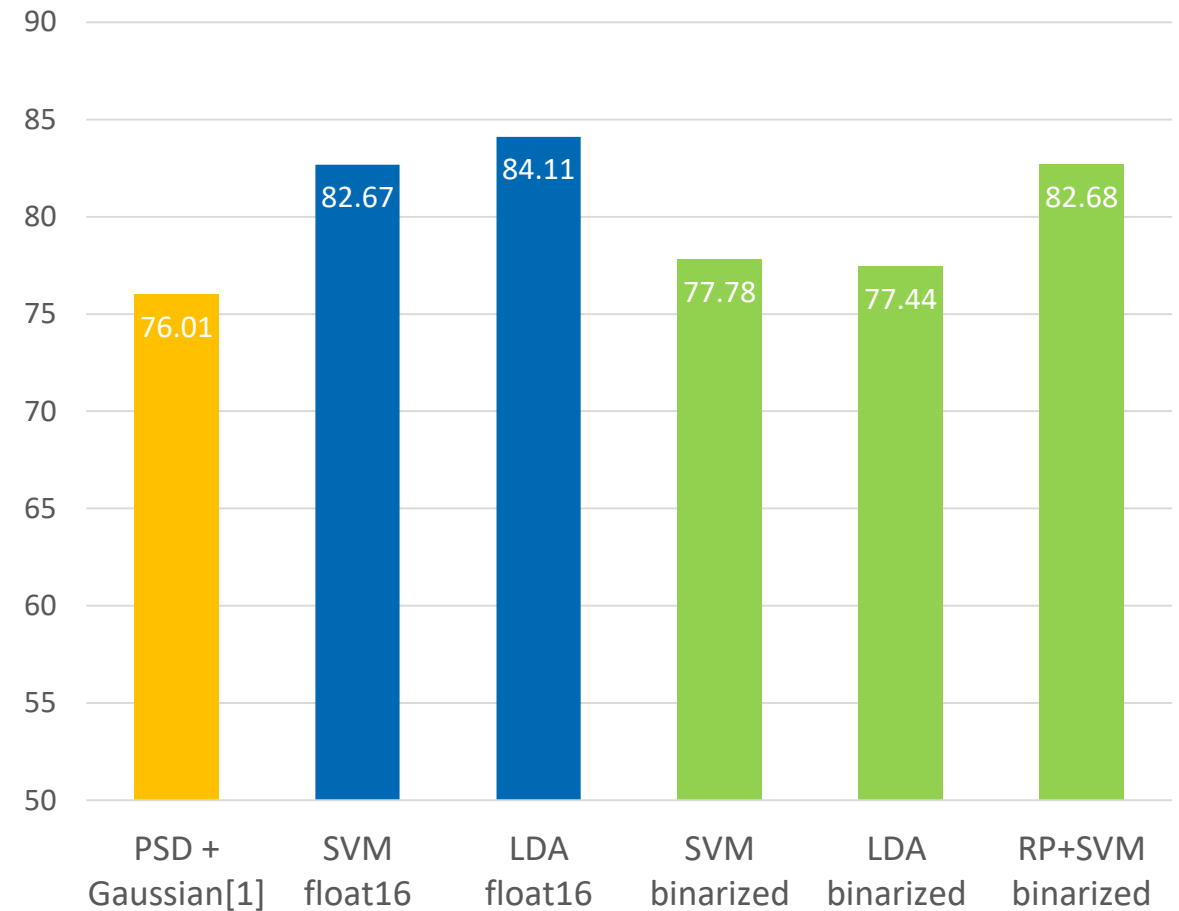


# Classification results

## 4-class MI



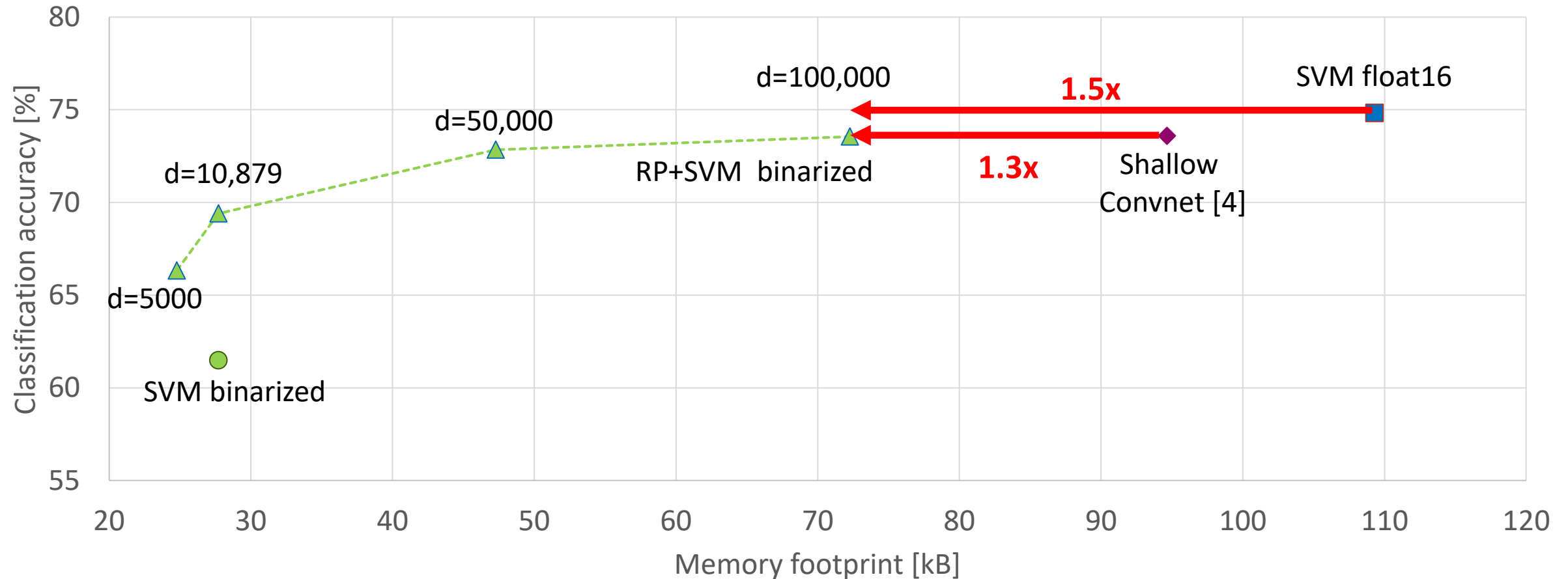
## 3-class MI



[1] Saeedi, et al. "Adaptive Assistance for Brain-Computer Interfaces by Online Prediction of Command Reliability." *IEEE Computational Intelligence Magazine*. 2016.

# Our binarization method reduces the memory footprint of the model

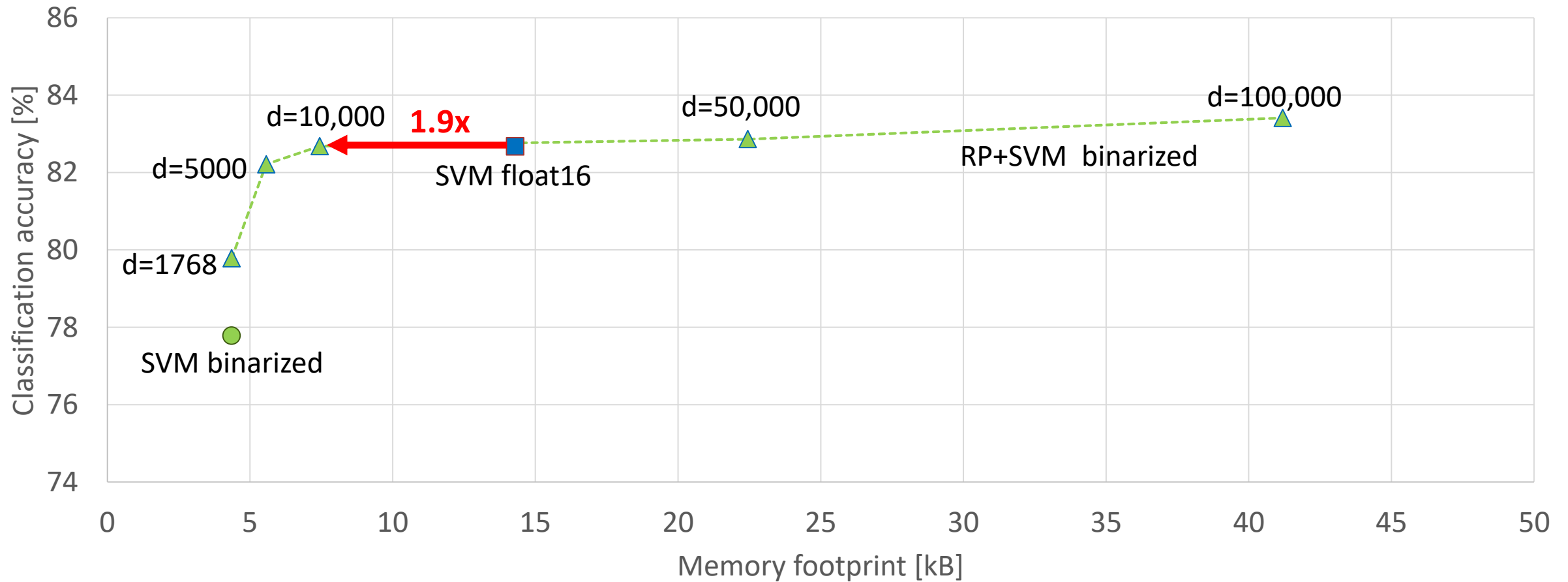
## 4-class MI



[4] Schirrneister, et al. "Deep learning with convolutional neural networks for EEG decoding and visualization." *Human Brain Mapping*. 2017.

# Similar results in 3-class MI

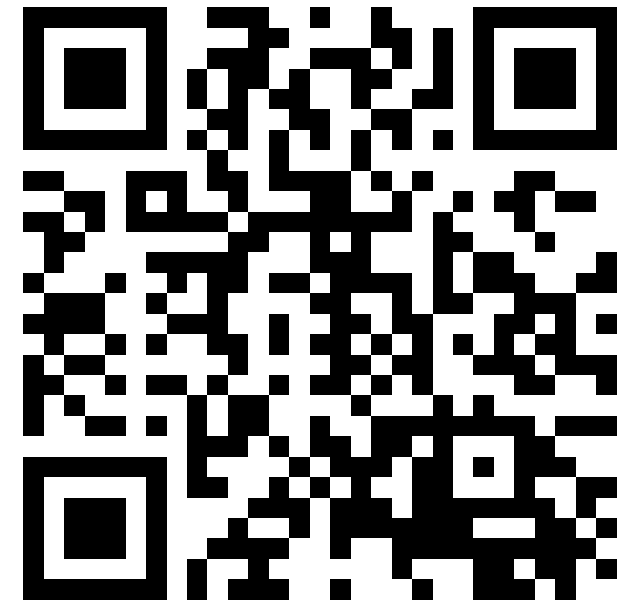
## 3-class MI



# Conclusion

- Binarize multi-spectral Riemannian features with sparse bipolar random projection
- Novel binarized SVM
- Test on two MI datasets:
  - 4-class MI: 1.27% lower accuracy at **1.5x smaller model** size
  - 3-class MI: Same accuracy at **1.9x smaller model** size
- **Next:** Binarize CNN-based classifier with Memory Augmented Neural Networks (MANNs)

Code available!



<https://github.com/MHersche/HDembedding-BCI>

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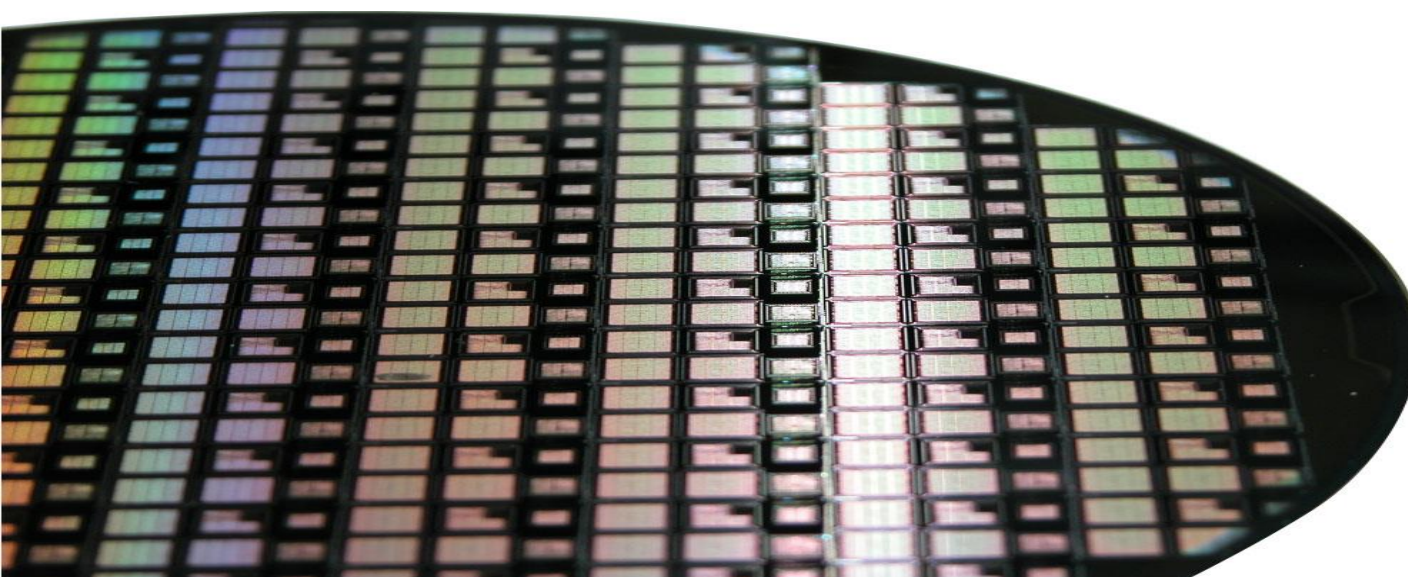


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