
Simulation of Quantum Effects in Nanoscale Devices

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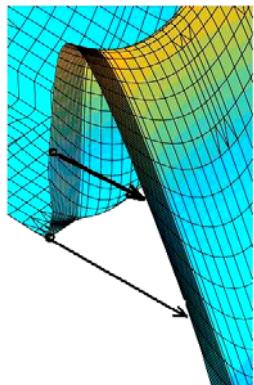
Outline

- Introduction
- Quantum-mechanical confinement effects
 - quantum V_T -shift
 - comparison single, double, triple, and surround gate
- Simulation of quantum-ballistic ON-currents
 - Band structure, transport, electrostatics
 - ON-current for different channel orientations
 - Effect of surface roughness
- Simulation of tunneling-induced OFF-currents
 - Source-drain tunneling
 - Gate tunneling leakage
 - Band-to-band tunneling (GIDL)
- Incoherent scattering
- Conclusion

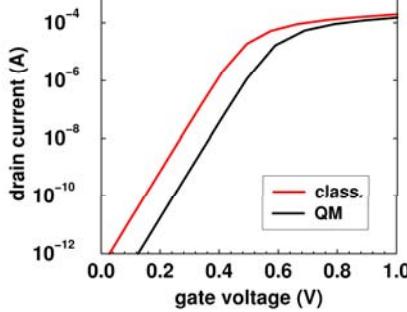
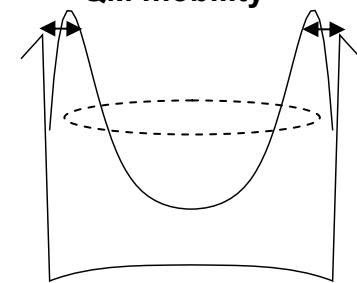
Introduction

Which quantum effects?

source-to-drain tunneling

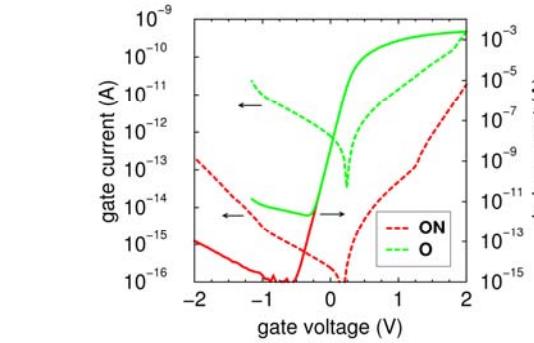
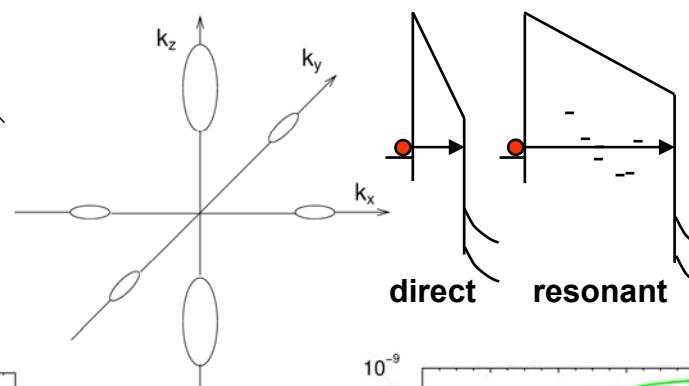


Confinement, quantization
 • quantum V_T shift
 • QM mobility

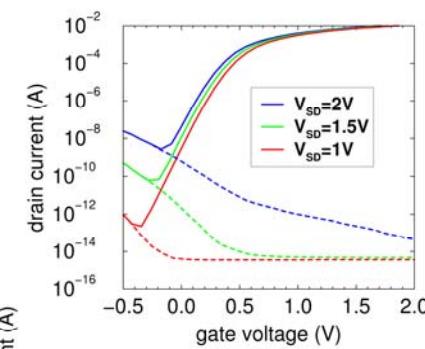
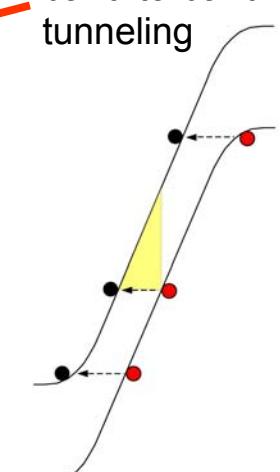


strain

strain



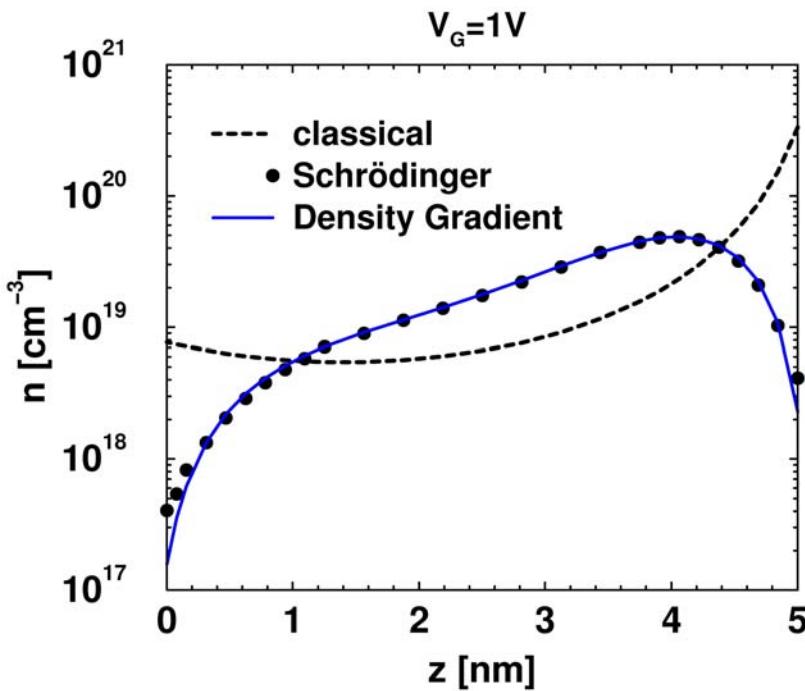
band-to-band tunneling



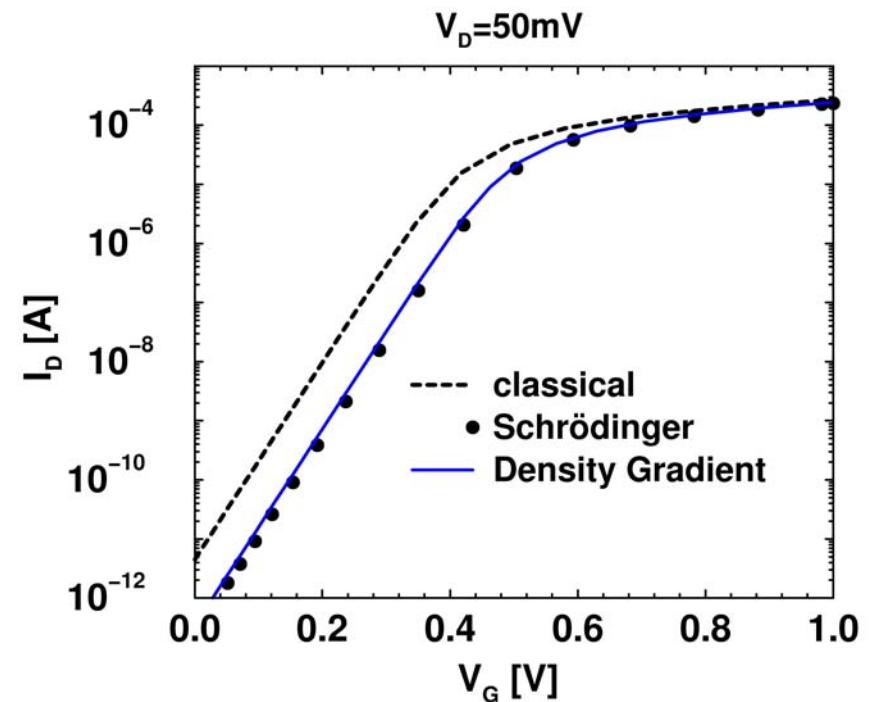
Quantum-mechanical confinement effects

Wave length of a free electron with energy $k_B T$ at 300K $\approx 8\text{nm}$!

channel density profile



transfer characteristics



asymmetrical n⁺p⁺ DGSOI nMOSFET, $t_{\text{Si}}=5\text{ nm}$, $t_{\text{ox}}=1.5\text{ nm}$, $L_G=90\text{ nm}$

A ‘quantum potential’ Λ is introduced in the classical formula of the density:

$$n[\vec{R}] = N_c \exp \left[\beta \left(E_{F,n}[\vec{R}] - E_c[\vec{R}] - \Lambda[\vec{R}] \right) \right]$$

The classical current equation reads:

$$e\vec{j}[\vec{R}] = -\mu k_B T \nabla n[\vec{R}] - \mu n[\vec{R}] \nabla \left(E_c[\vec{R}] + \Lambda[\vec{R}] \right)$$

1D Schrödinger-Poisson solver

Λ follows by equating the density $n[R]$ with the expression

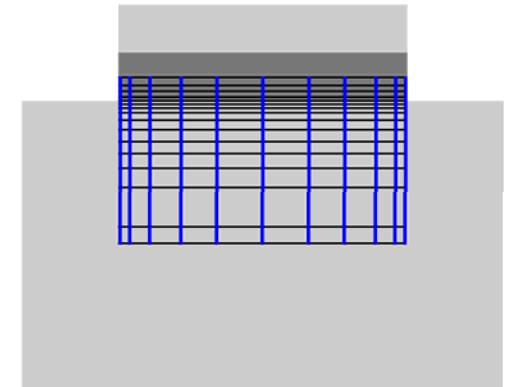
$$n(z) = \frac{1}{\beta \pi \hbar^2} \sum_{j,\nu} \left| \Psi_j^{(\nu)}(z) \right|^2 m_{xy}^{(\nu)}(z) \exp \left[\beta \left(E_{F,n}(z) - E_j^{(\nu)} \right) \right]$$

Boundary condition at the ends of the domain [z⁻,z⁺], defining the ‘quantum box’:

$$\Psi_j^{(\nu)\prime}/\Psi_j^{(\nu)} = \pm \sqrt{2m_z^{(\nu)}|E_j^{(\nu)} - E_c|/\hbar}$$

Full Newton impractical, therefore approximation

$$\partial n_i^{\text{qm}}/\partial \Phi_j \approx -\delta_{ij} \partial n_i^{\text{qm}}/\partial E_{F,i}$$



Density Gradient model

Λ is given by the PDE

$$\begin{aligned}\Lambda &= -\gamma \frac{\hbar^2}{12 m} \left[\nabla^2 \log n + \frac{1}{2} (\nabla \log n)^2 \right] \\ &= -\gamma \frac{\hbar^2}{6m} \frac{\nabla^2 \sqrt{n}}{\sqrt{n}}\end{aligned}$$

Based on method of moments for Liouville equation

$$i\hbar\partial_t\rho = [\mathcal{H}, \rho]_-$$

Hierarchy closed by replacing higher-order derivatives of density matrix ρ by approx. for equilibrium density matrix ρ_0

Assumptions: equilibrium density, isotropy of effective mass, $\delta\Phi/k_B T \ll 1$ (Born approx.)

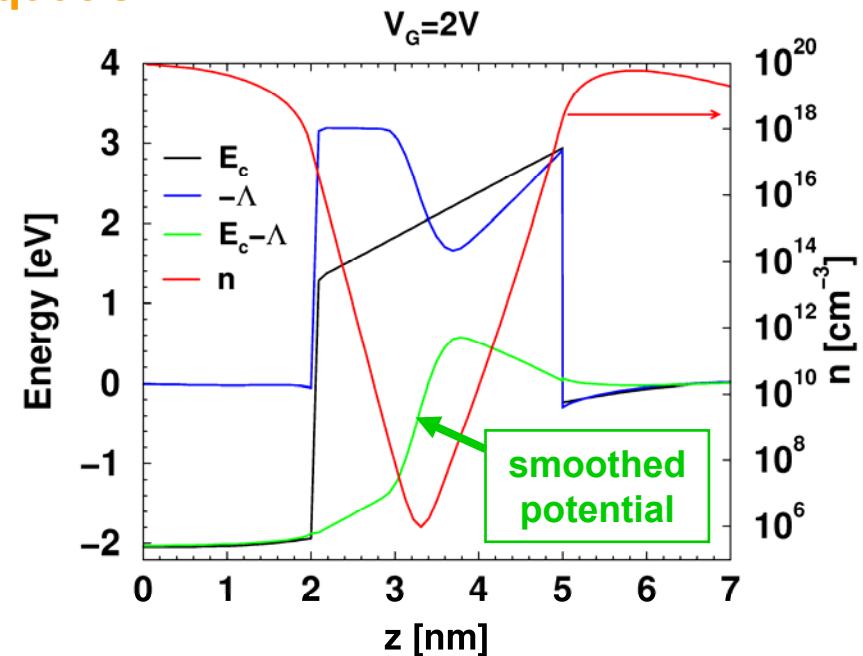
Generalization for device simulation:

- DOS mass $\rightarrow m$
- non-equilibrium density $\rightarrow n$
- non-perturbative formulation of Λ with the *smoothed potential* $\bar{\Phi} = E_c + \Phi_m + \Lambda$

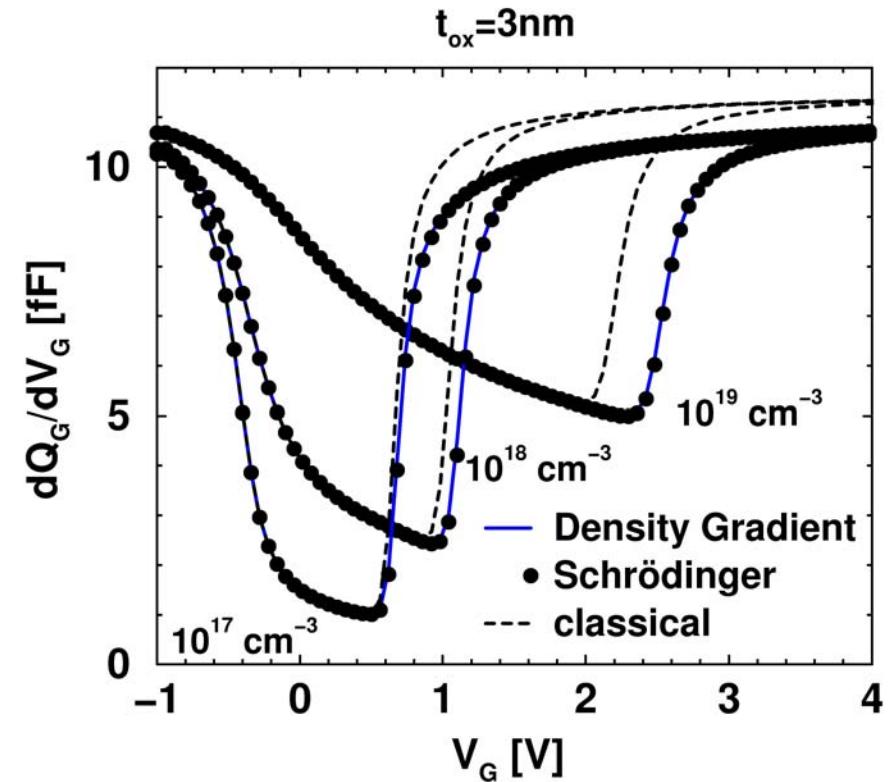
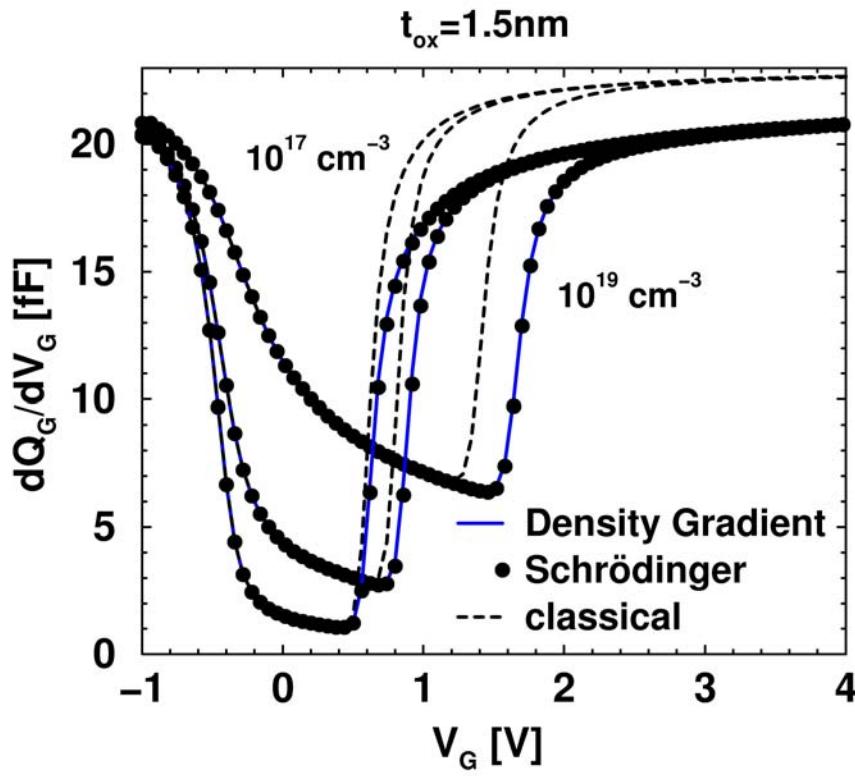
$$\Lambda = -\gamma \frac{\hbar^2}{12m} \left\{ \nabla^2 (\beta E_{F,n} - \beta \bar{\Phi}) + \frac{1}{2} [\nabla (\beta E_{F,n} - \beta \bar{\Phi})]^2 \right\}$$

Λ is new system variable, coupled Newton

DG is multi-dimensional, pre-factor γ is “universal” (3.6 for Si, if $m = m_{\text{DOS}}$)



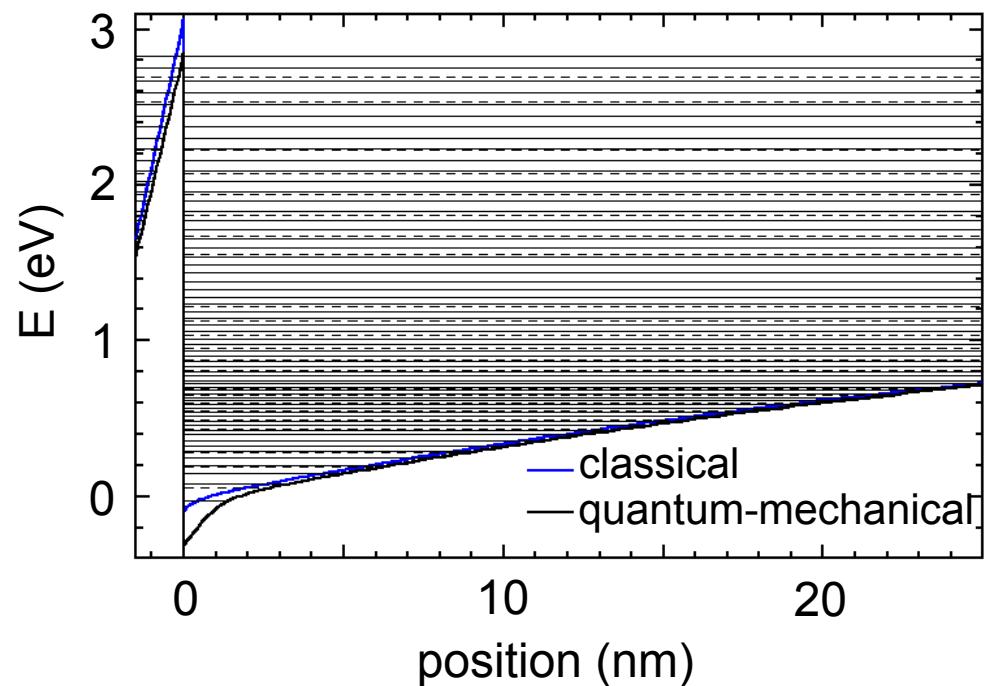
MOS (with poly) capacitor CV curves



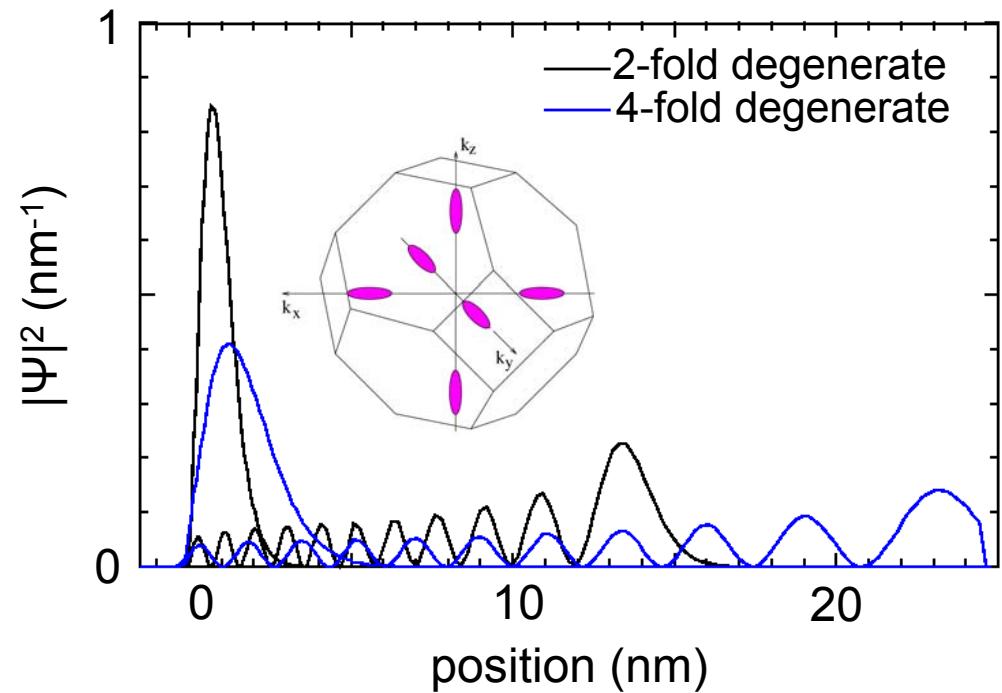
$$N_{\text{poly}} = 1e20 \text{ cm}^{-3}, A_G = 1 \mu\text{m}^2$$

MOS (with poly) capacitor

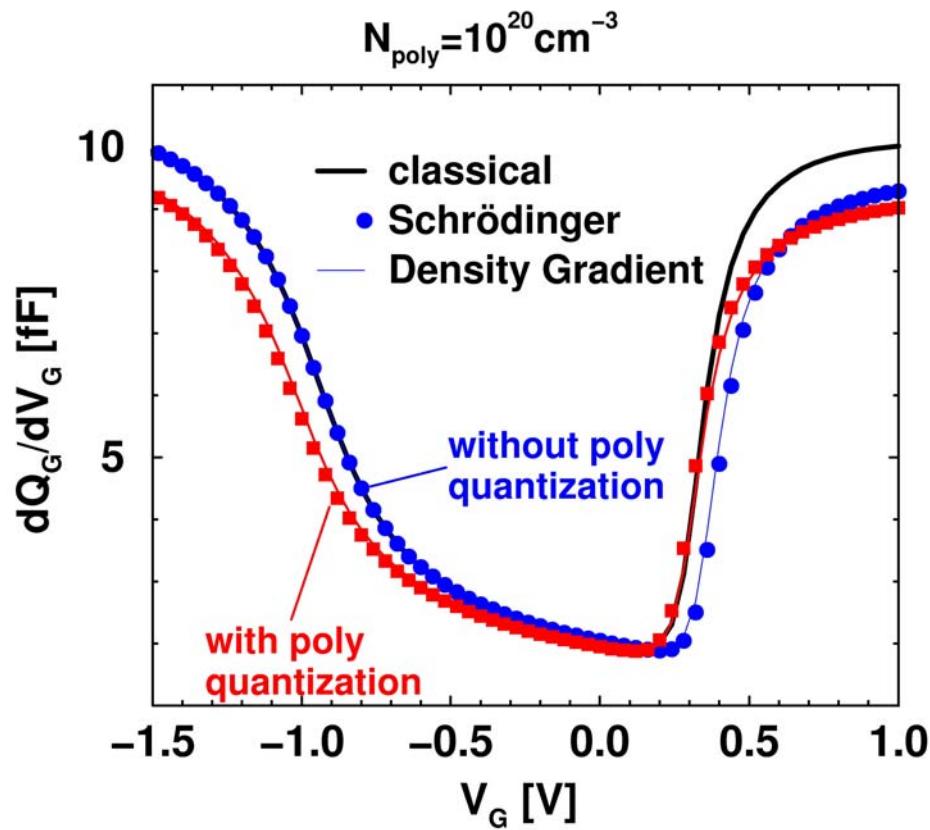
eigenenergies



wave functions

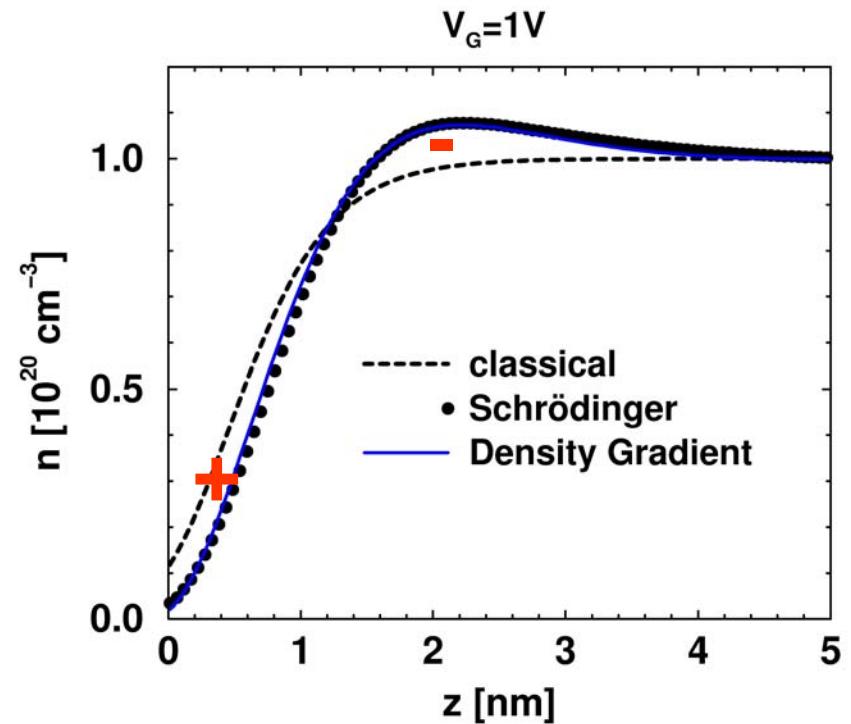
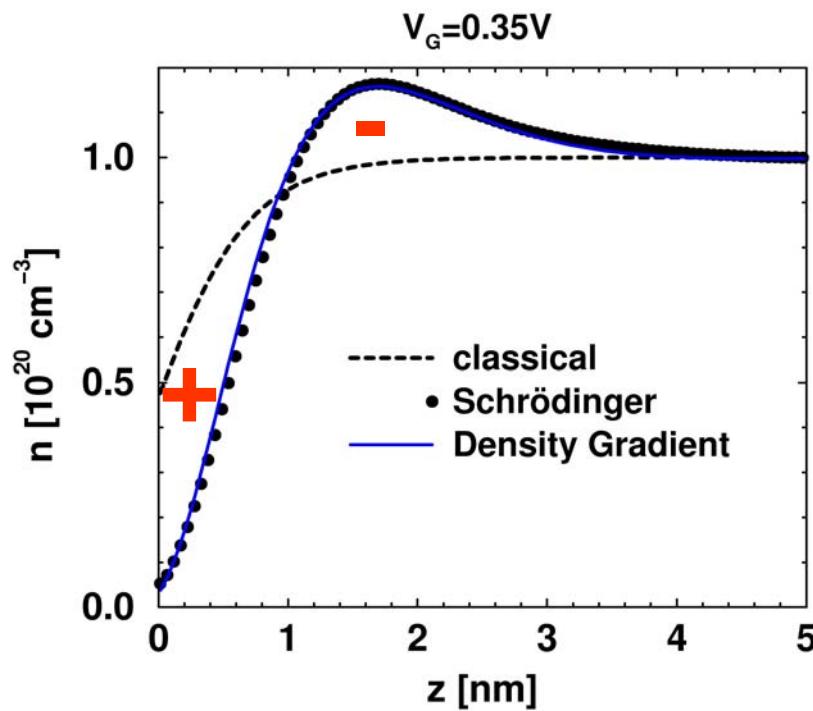


$$N_A = 5 \text{e}17 \text{ cm}^{-3}, t_{\text{ox}} = 3 \text{ nm}, V_G = 3 \text{ V}$$

Quantum depletion at poly-SiO₂ interface

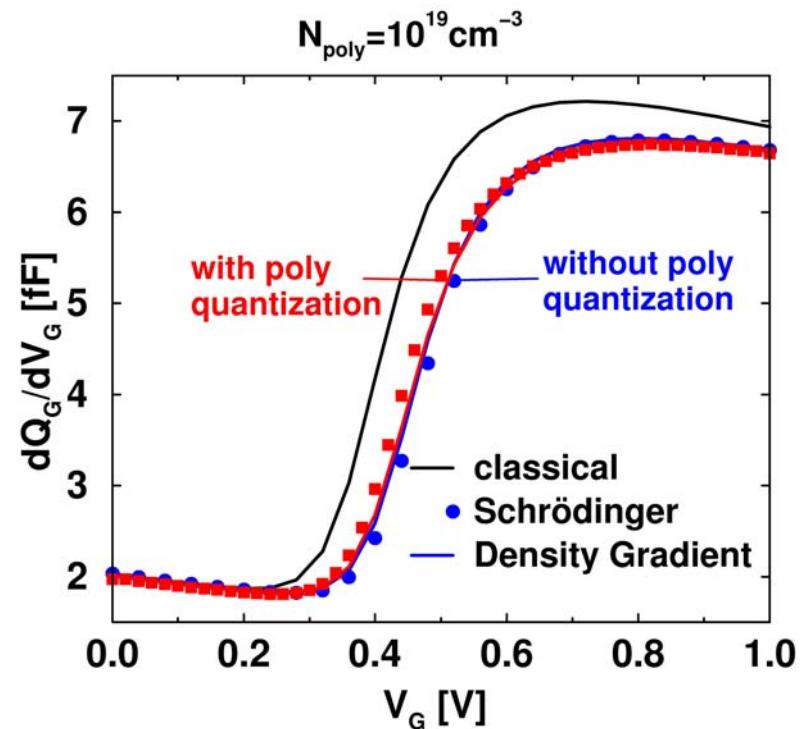
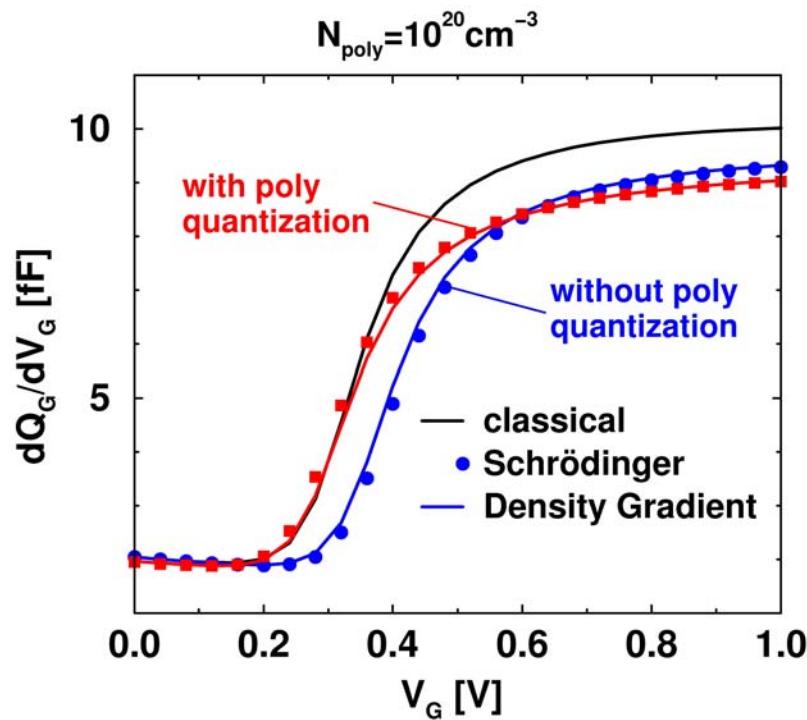
compensation of quantum shift
at threshold for high poly
doping ($\sim 1e20 \text{ cm}^{-3}$)!

$$N_A = 5e17 \text{ cm}^{-3}, t_{\text{ox}} = 3 \text{ nm}, A_G = 1 \mu\text{m}^2$$

Electron density profile at poly-SiO₂ interface

- a “quantum dipole” forms as the electron waves are repelled from the poly-SiO₂ interface
- poly quantum depletion disappears with rising V_G (smoother poly band edge curvature)

Effect on CV curves



- strength of the quantum dipole depends on doping level within the first few nanometers
- no effect on CV, if $N_{\text{poly}} < 1e19 \text{ cm}^{-3}$ at the interface

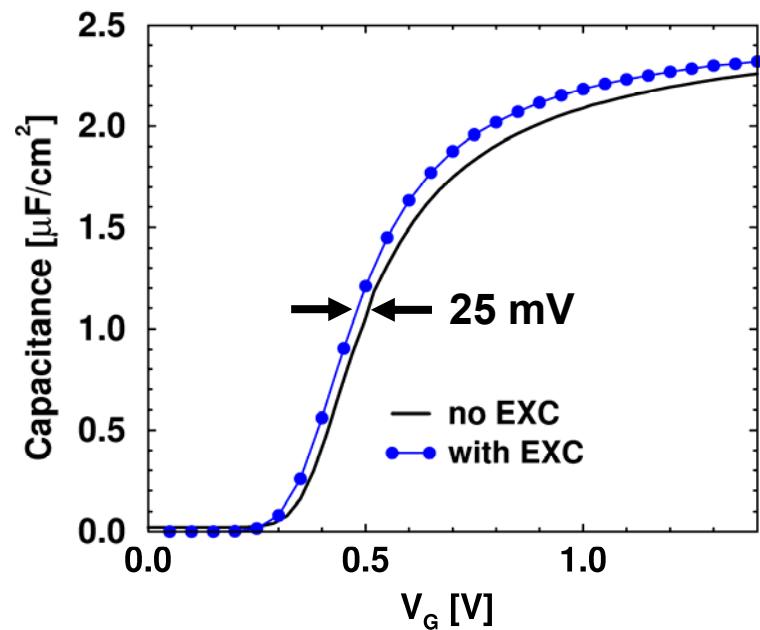
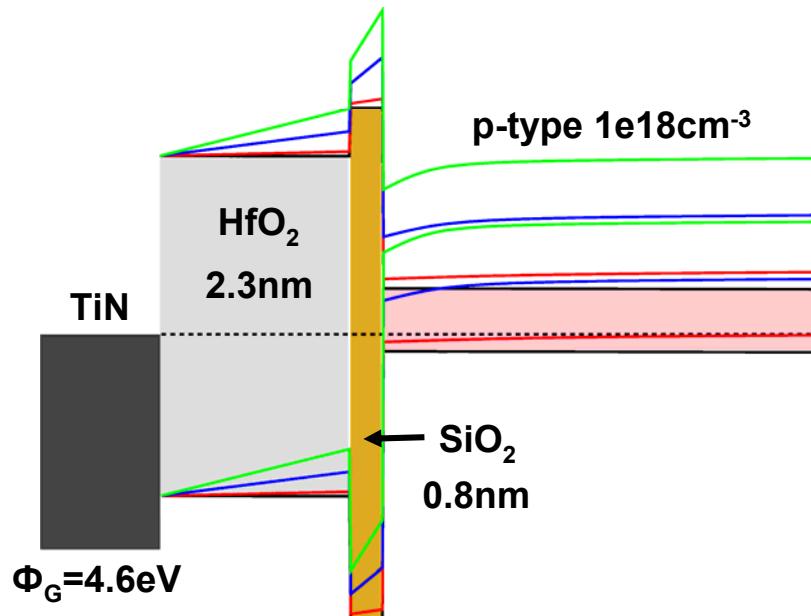
Effect of exchange-correlation potential on CV curves

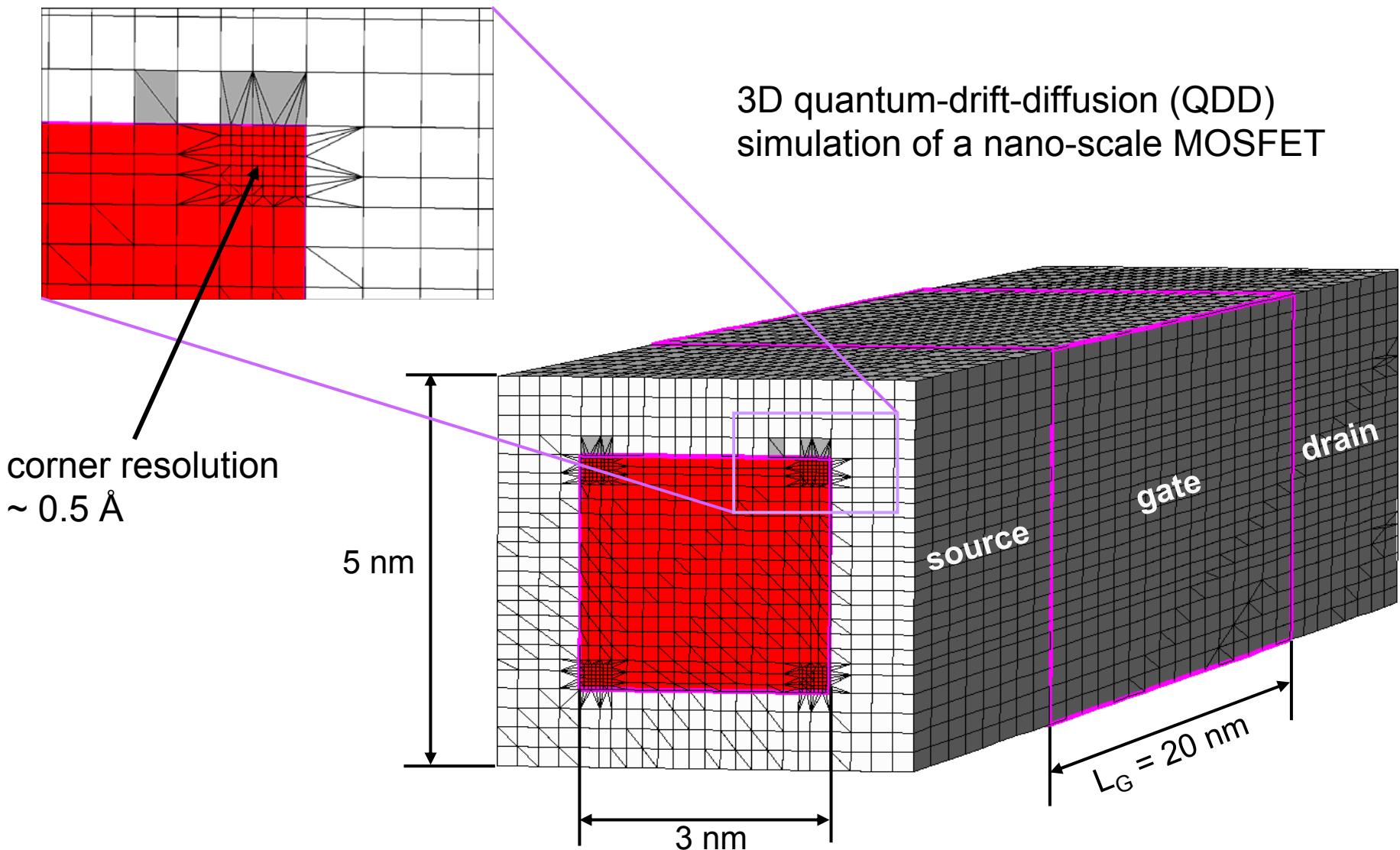
$$\epsilon_X = -\frac{q^2}{4\pi\epsilon_0\epsilon_r} (3n)^{1/3} = -0.909 \cdot 10^{-8} n^{1/3} \text{ [eV]}$$

$$\epsilon_C = -1.224 \cdot 10^{-5} \left[\ln \left(1 + \frac{n}{2.375 \cdot 10^{12}} \right) \right]^2 \text{ [eV]}$$

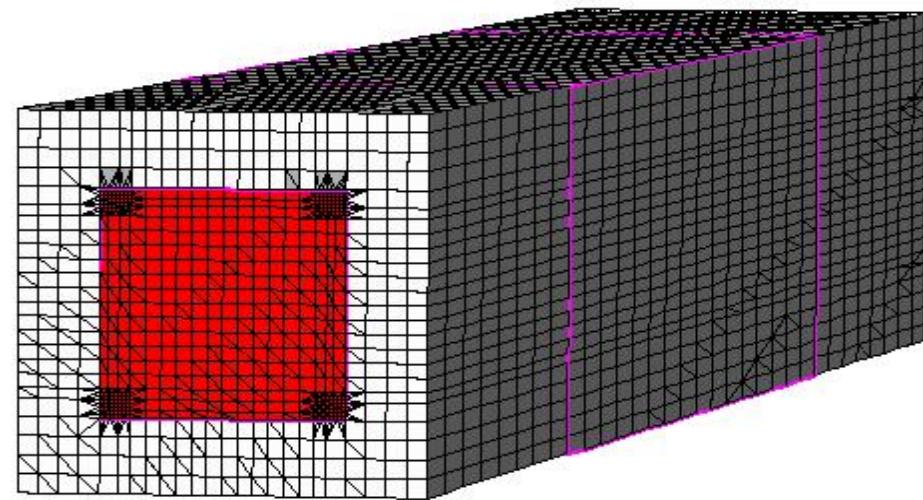
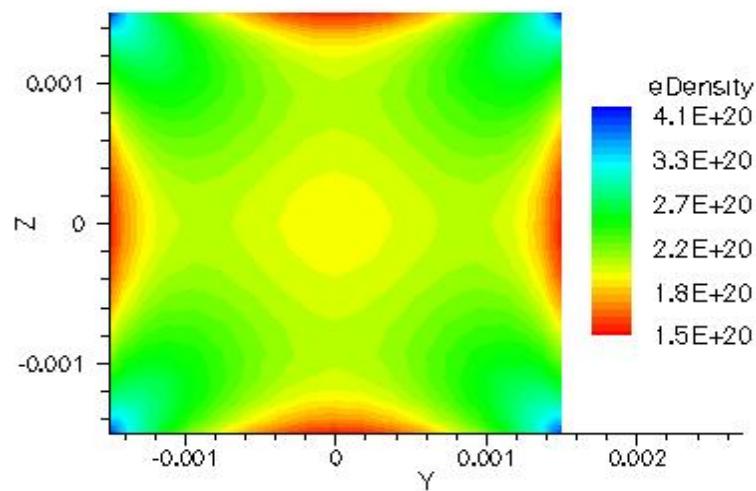
LDA ϵ_{XC} (ϵ_C is continuous fit to Perdew-Zunger theory)

- Many-body effect of exchange-correlation shows up as negative V_T -shift (band gap narrowing)
- Image-force already taken into account by boundary condition for Hartree potential (Poisson equation)

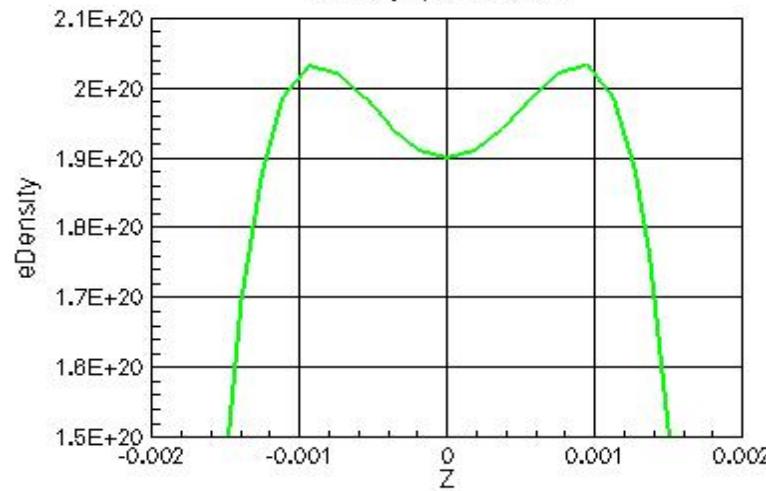




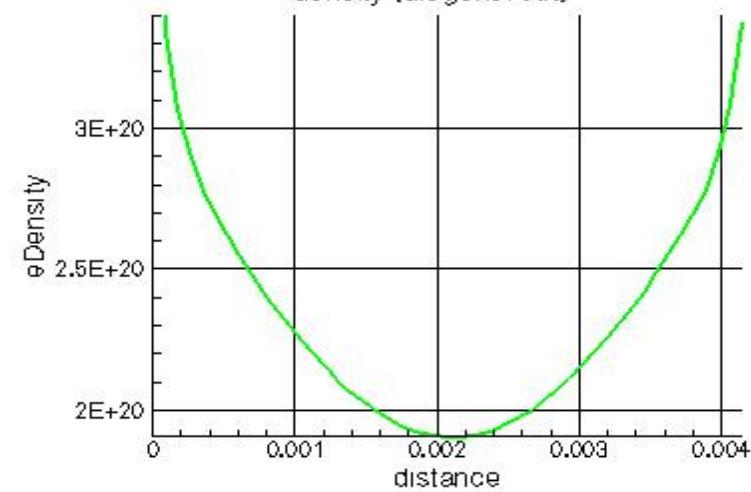
Influence of mesh refinement

density @ $V_{gs}=1V$ 

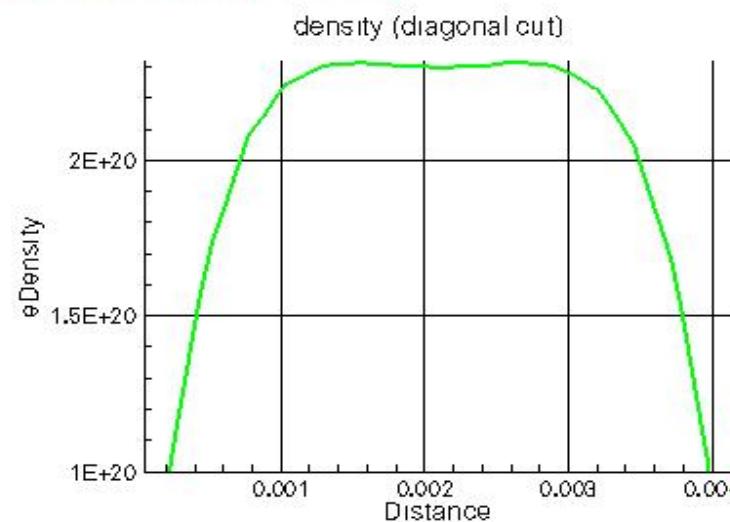
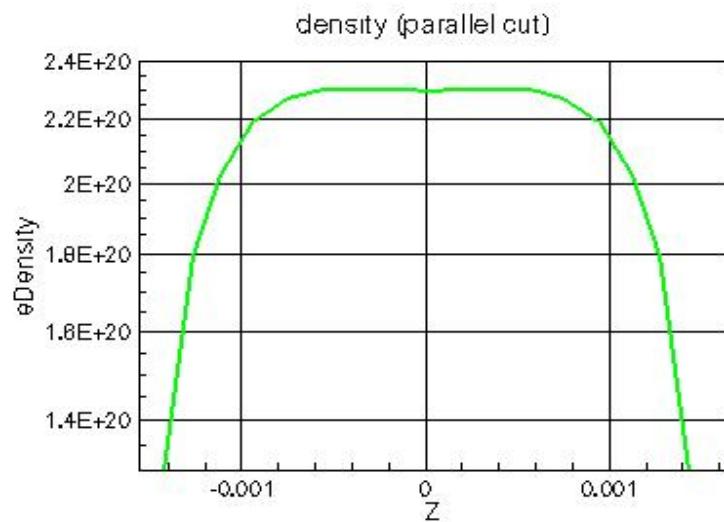
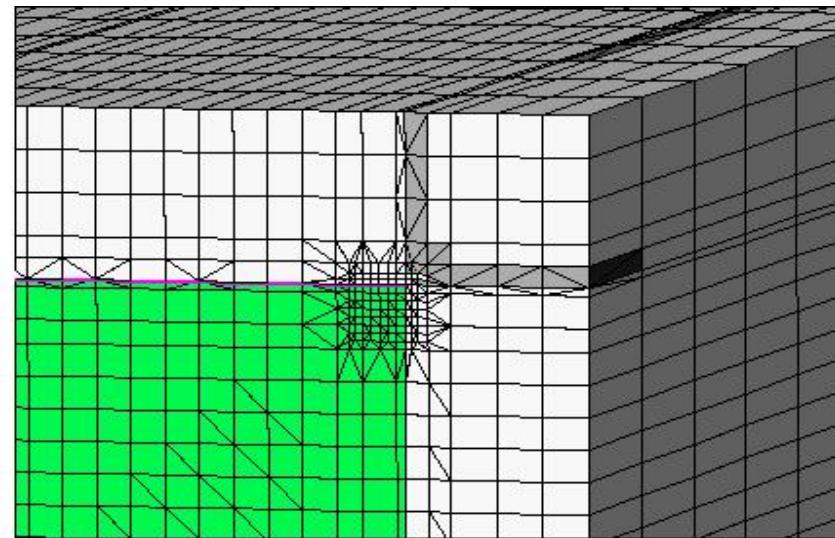
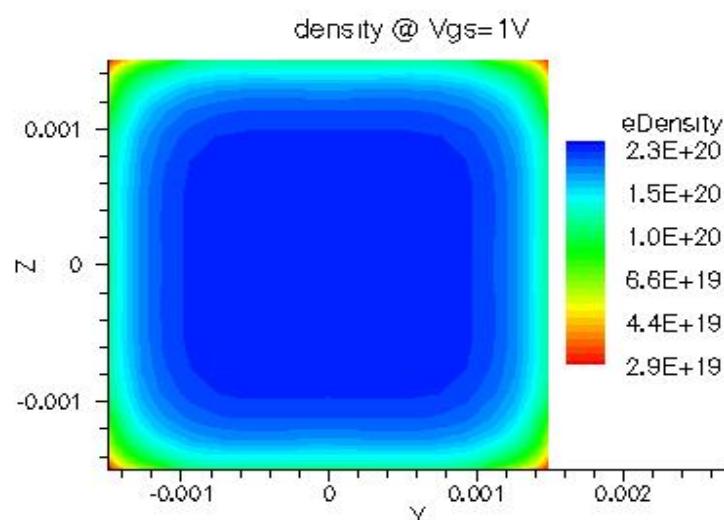
density (parallel cut)



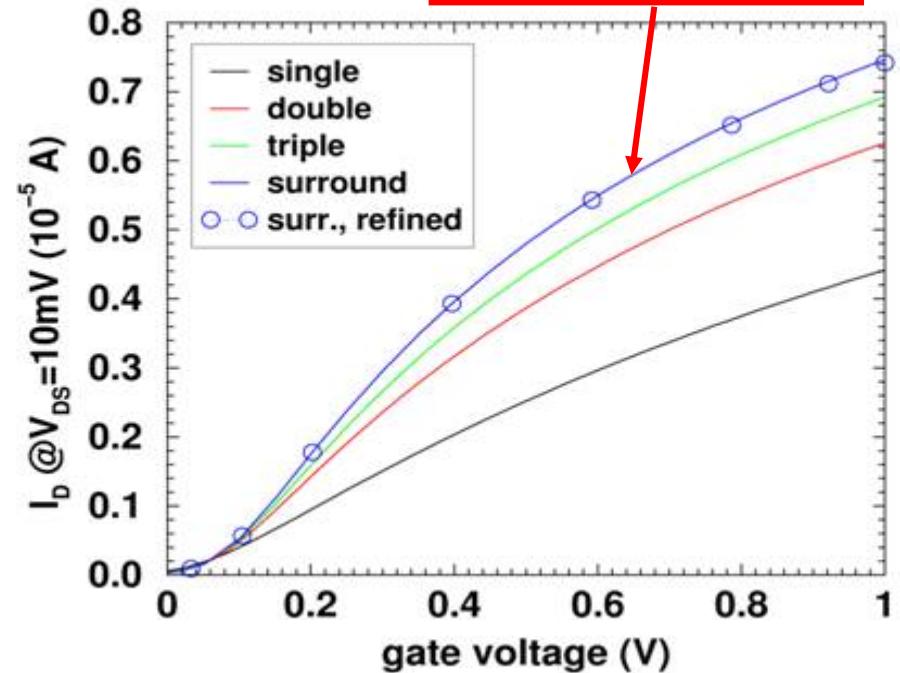
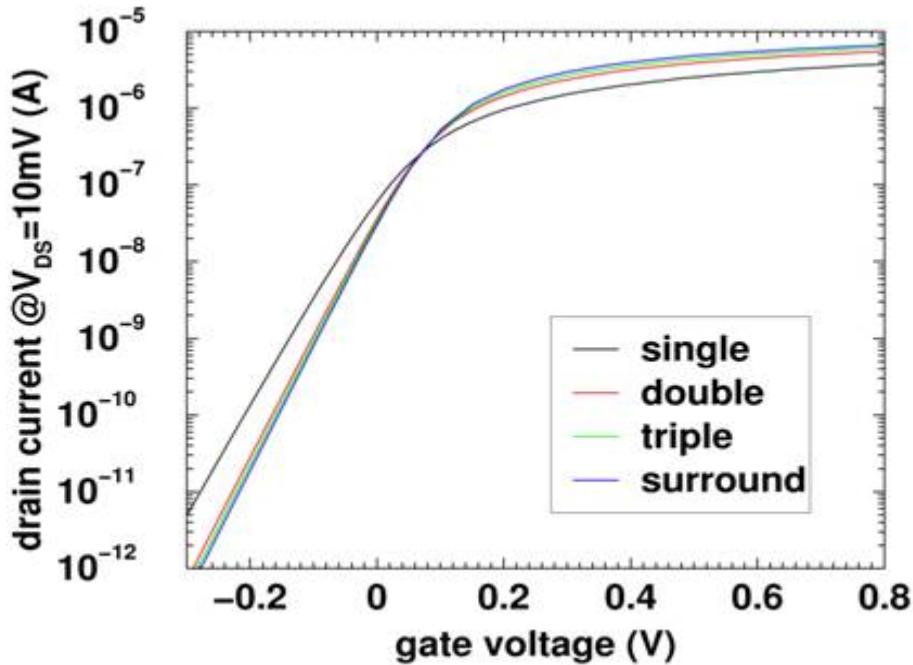
density (diagonal cut)



Influence of mesh refinement



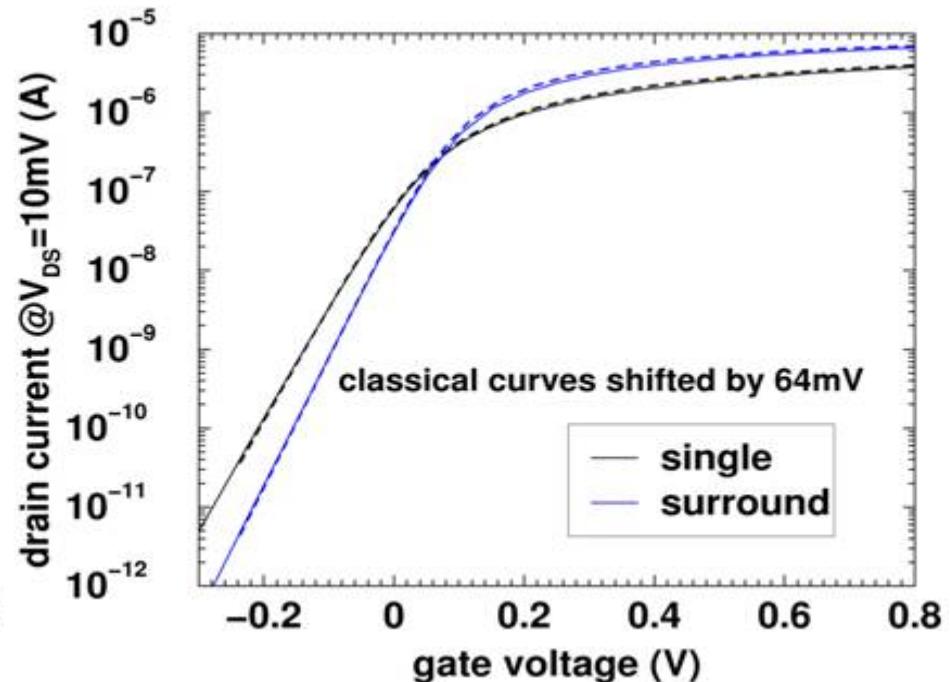
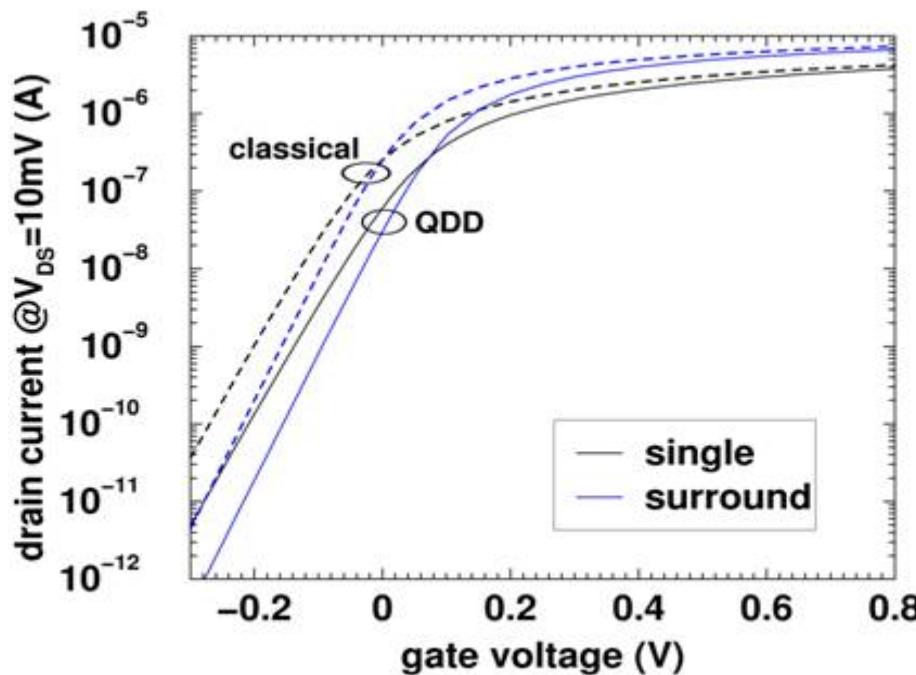
Transfer characteristics



assumption: isotropic, classical mobility

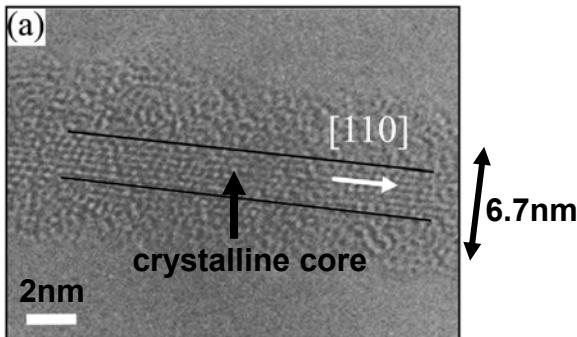
- no corner effect (FD, no channel doping, 3x3 nm wire)
- only little improvement from double → surround (gate overlap, e.g. triple gate is an effective Π -gate)

Transfer characteristics (contd.)



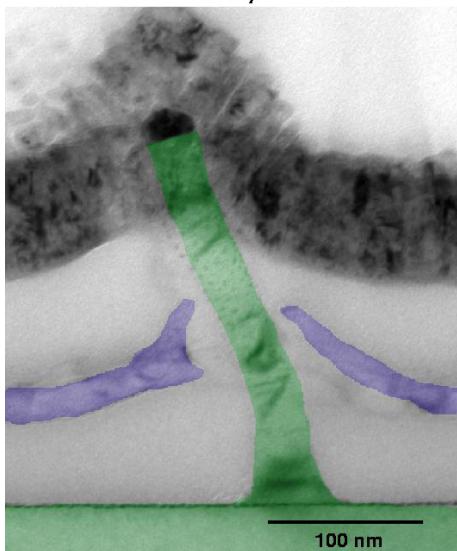
- quantum V_T -shift of $\sim 64 \text{ mV}$, independent of gate configuration
- almost perfect shift on V_{GS} -axis \rightarrow quantum V_T -shift can be translated into work function difference

Simulation of quantum-ballistic ON-currents



Cui et al., APL 78(15), 2214 (2001)

Vertical Schottky barrier FETs.



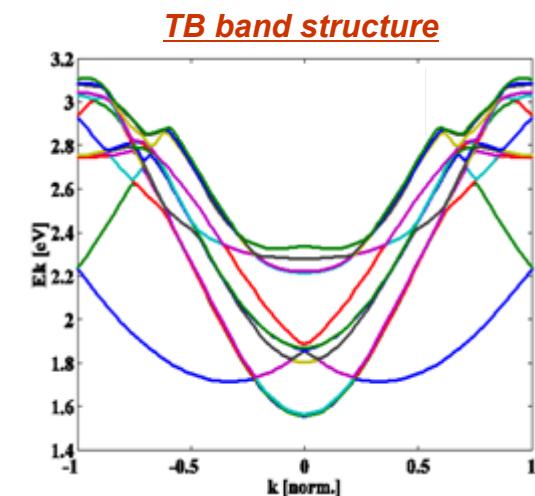
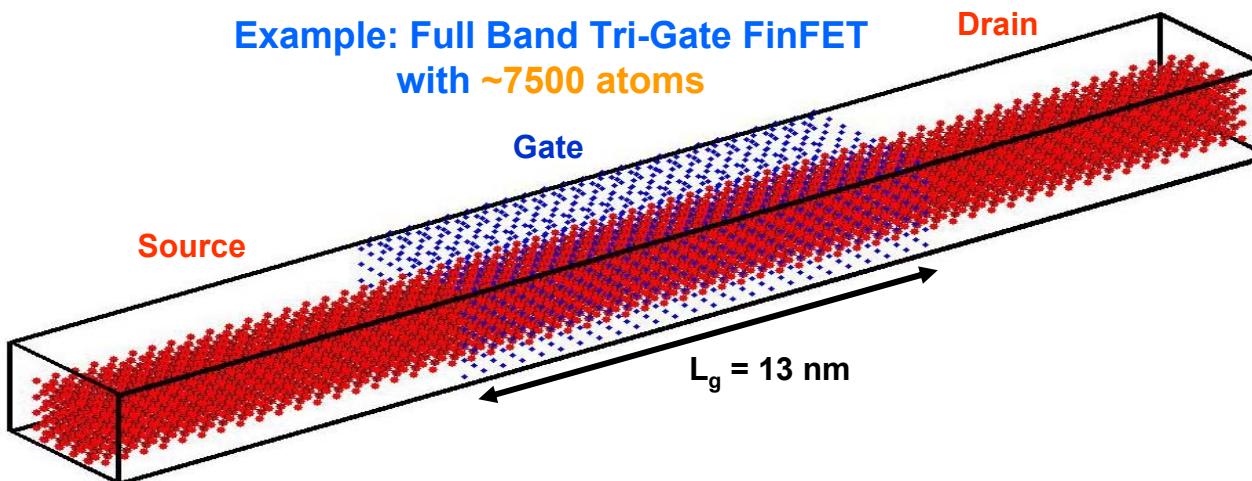
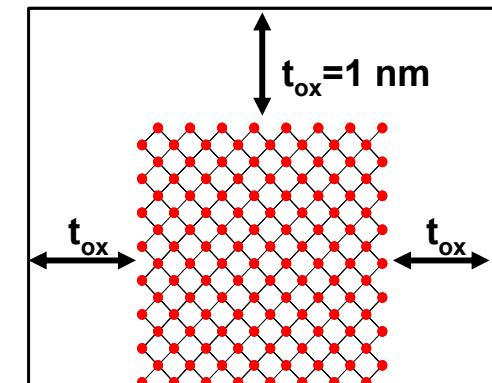
IBM Zürich, Walter Riess

- Si nanowires (NWs) are ‘post-CMOS’ candidates, (transistors and connectors)
- transport in Si NWs is often believed to become “ballistic” (which is wrong)
- all produced Si NWs have cross sections $> 5 \times 5 \text{ nm}^2 \Rightarrow$ no full quantum transport simulation necessary
- if (in the future) cross sections $< 5 \times 5 \text{ nm}^2$, strong confinement \Rightarrow band structure effects become important
- predictive simulations then require: accurate band structure model, quantum transport solver (OBCs), self-consistent electrostatics

Band structure

- **$sp^3d^5s^*$ tight-binding method**
- **bulk band structure exactly reproduced**
- **inclusion of strain, defects, surface roughness possible**
- **extension to nanostructures straight-forward**
- **gate tunneling and b2b tunneling possible**
- **high computational effort required for nanostructures, since 10 bands involved without spin, 20 bands with spin**
- ***bulk* TB parameters, no lattice relaxation**

Atomistic description of a [100] nanowire with 2.1×2.1 nm² cross section



Band structure

On-site and two-center integrals

TABLE IV. Tight-binding parameters for Si and Ge (same-site and two-center integrals) in the Slater-Koster notation (Ref. 3); units are eV.

Parameter	Si	Ge
E_s	-2.15168	-1.95617
E_p	4.22925	5.30970
E_{s^*}	19.11650	19.29600
E_d	13.78950	13.58060
λ	0.01989	0.10132
$ss\sigma$	-1.95933	-1.39456
$s^*s^*\sigma$	-4.24135	-3.56680
$ss^*\sigma$	-1.52230	-2.01830
$sp\sigma$	3.02562	2.73135
$s^*p\sigma$	3.15565	2.68638
$sd\sigma$	-2.28485	-2.64779
$s^*d\sigma$	-0.80993	-1.12312
$pp\sigma$	4.10364	4.28921
$pp\pi$	-1.51801	-1.73707
$pd\sigma$	-1.35554	-2.00115
$pd\pi$	2.38479	2.10953
$dd\sigma$	-1.68136	-1.32941
$dd\pi$	2.58880	2.56261
$dd\delta$	-1.81400	-1.95120

19 Parameters for Si and Ge:

- Optimized to reproduce bulk band structure and effective masses

- 4 different orbital types (s, p, d, s*),
=> 4 on-site energy parameters (E_s , E_p , E_{s^*} , E_d)

- Spin-orbit coupling (λ)

- 14 matrix elements between orbitals with 3 different possible bonds (σ , π , and δ). Symmetry + polarization not considered (Koster-Slater table)

Phys. Rev. B **69**, 115201 (2004)

Band structure

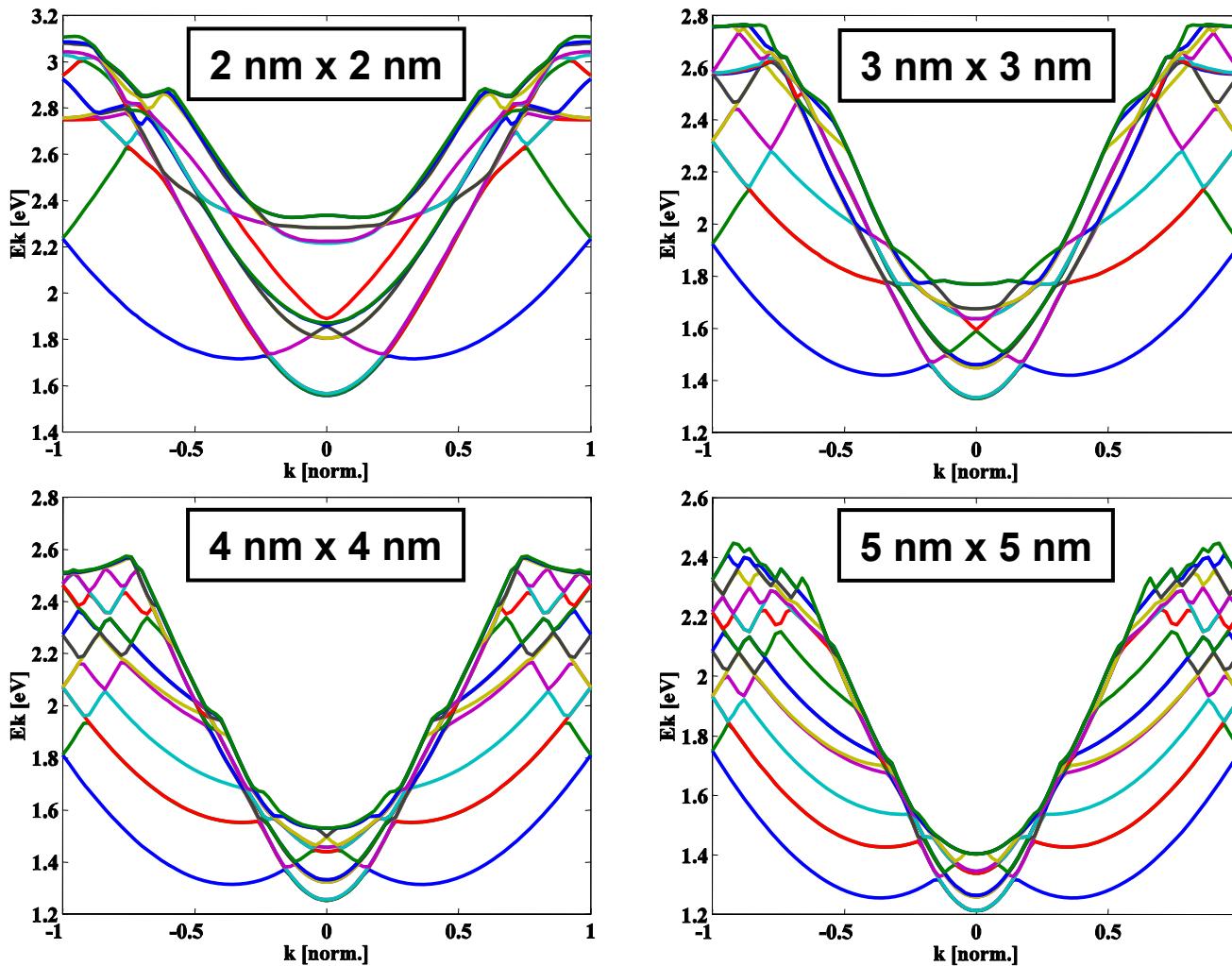
Energy integrals in terms of two-center integrals

$E_{s,s}$	$(ss\sigma)$
$E_{s,x}$	$l(ssp\sigma)$
$E_{x,x}$	$l^2(pp\sigma) + (1-l^2)(pp\pi)$
$E_{x,y}$	$lm(pp\sigma) - lm(pp\pi)$
$E_{z,z}$	$ln(pp\sigma) - ln(pp\pi)$
$E_{s,xy}$	$\sqrt{3}lm(spd\sigma)$
E_{s,x^2-y^2}	$\frac{1}{2}\sqrt{3}(l^2-m^2)(sd\sigma)$
$E_{s,2z^2-r^2}$	$[n^2 - \frac{1}{2}(l^2+m^2)](sd\sigma)$
$E_{x,xy}$	$\sqrt{3}l^2m(pd\sigma) + m(1-2l^2)(pd\pi)$
$E_{x,yz}$	$\sqrt{3}lmn(pd\sigma) - 2lmn(pd\pi)$
$E_{x,zz}$	$\sqrt{3}l^2n(pd\sigma) + n(1-2l^2)(pd\pi)$
E_{x,x^2-y^2}	$\frac{1}{2}\sqrt{3}l(l^2-m^2)(pd\sigma) + l(1-l^2+m^2)(pd\pi)$
E_{y,x^2-y^2}	$\frac{1}{2}\sqrt{3}m(l^2-m^2)(pd\sigma) - m(1+l^2-m^2)(pd\pi)$
E_{z,x^2-y^2}	$\frac{1}{2}\sqrt{3}n(l^2-m^2)(pd\sigma) - n(l^2-m^2)(pd\pi)$
$E_{x,3z^2-r^2}$	$l[n^2 - \frac{1}{2}(l^2+m^2)](pd\sigma) - \sqrt{3}ln^2(pd\pi)$
$E_{y,3z^2-r^2}$	$m[n^2 - \frac{1}{2}(l^2+m^2)](pd\sigma) - \sqrt{3}mn^2(pd\pi)$
$E_{z,3z^2-r^2}$	$n[n^2 - \frac{1}{2}(l^2+m^2)](pd\sigma) + \sqrt{3}n(l^2+m^2)(pd\pi)$
$E_{xy,xy}$	$3l^2m^2(dd\sigma) + (l^2+m^2-4l^2m^2)(dd\pi) + (n^2+l^2m^2)(dd\delta)$
$E_{xy,yz}$	$3lm^2n(dd\sigma) + ln(1-4m^2)(dd\pi) + ln(m^2-1)(dd\delta)$
$E_{xy,zz}$	$3l^2mn(dd\sigma) + mn(1-4l^2)(dd\pi) + mn(l^2-1)(dd\delta)$
E_{xy,x^2-y^2}	$\frac{3}{2}lm(l^2-m^2)(dd\sigma) + 2lm(m^2-l^2)(dd\pi) + \frac{3}{2}lm(l^2-m^2)(dd\delta)$
E_{yz,x^2-y^2}	$\frac{3}{2}mn(l^2-m^2)(dd\sigma) - mn[1+2(l^2-m^2)](dd\pi) + mn[1+\frac{1}{2}(l^2-m^2)](dd\delta)$
E_{xz,x^2-y^2}	$\frac{3}{2}nl(l^2-m^2)(dd\sigma) + nl[1-2(l^2-m^2)](dd\pi) - nl[1-\frac{1}{2}(l^2-m^2)](dd\delta)$
$E_{xy,3z^2-r^2}$	$\sqrt{3}lm[n^2 - \frac{1}{2}(l^2+m^2)](dd\sigma) - 2\sqrt{3}lmn^2(dd\pi) + \frac{1}{2}\sqrt{3}lm(1+n^2)(dd\delta)$
$E_{yz,3z^2-r^2}$	$\sqrt{3}mn[n^2 - \frac{1}{2}(l^2+m^2)](dd\sigma) + \sqrt{3}mn(l^2+m^2-n^2)(dd\pi) - \frac{1}{2}\sqrt{3}mn(l^2+m^2)(dd\delta)$
$E_{xz,3z^2-r^2}$	$\sqrt{3}ln[n^2 - \frac{1}{2}(l^2+m^2)](dd\sigma) + \sqrt{3}ln(l^2+m^2-n^2)(dd\pi) - \frac{1}{2}\sqrt{3}ln(l^2+m^2)(dd\delta)$
$E_{x^2-y^2,x^2-y^2}$	$\frac{3}{4}(l^2-m^2)^2(dd\sigma) + [l^2+m^2-(l^2-m^2)^2](dd\pi) + [n^2+\frac{1}{4}(l^2-m^2)^2](dd\delta)$
$E_{x^2-y^2,3z^2-r^2}$	$\frac{1}{2}\sqrt{3}(l^2-m^2)[n^2 - \frac{1}{2}(l^2+m^2)](dd\sigma) + \sqrt{3}n^2(m^2-l^2)(dd\pi) + \frac{1}{4}\sqrt{3}(1+n^2)(l^2-m^2)(dd\delta)$
$E_{z^2-r^2,3z^2-r^2}$	$[n^2 - \frac{1}{2}(l^2+m^2)](dd\sigma) + 3n^2(l^2+m^2)(dd\pi) + \frac{3}{4}(l^2+m^2)^2(dd\delta)$

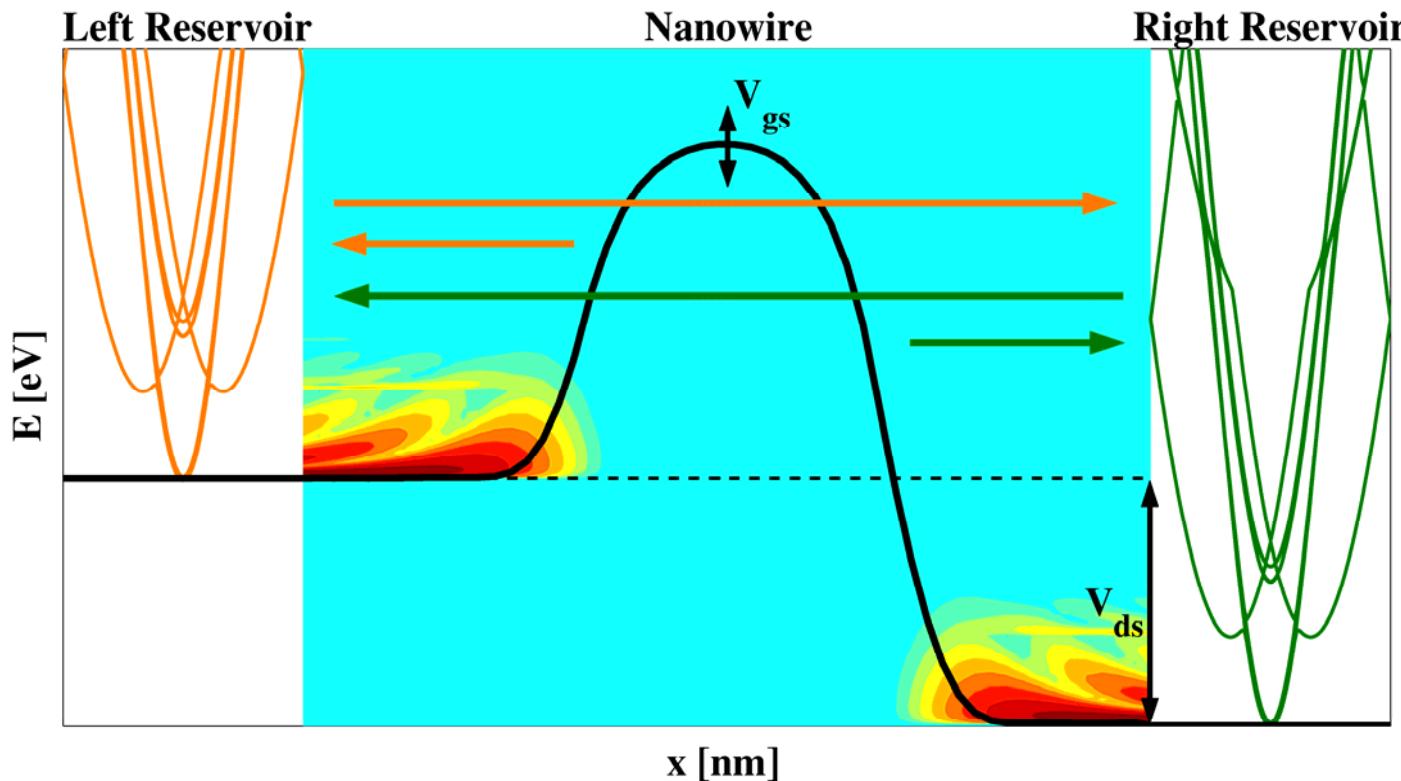
Koster-Slater table

Phys. Rev. 94, 1498 (1954)

How does band structure change with increasing cross section?



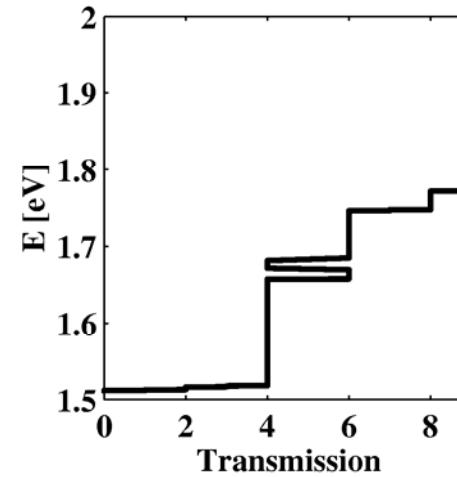
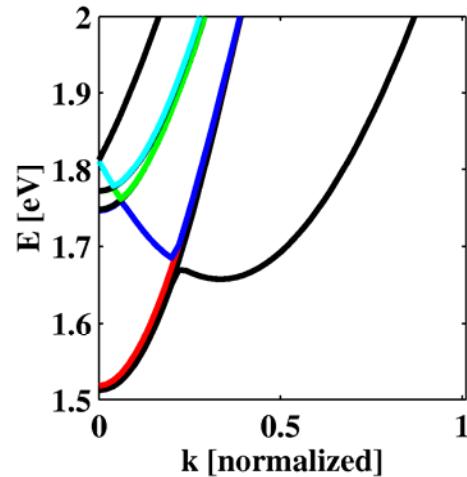
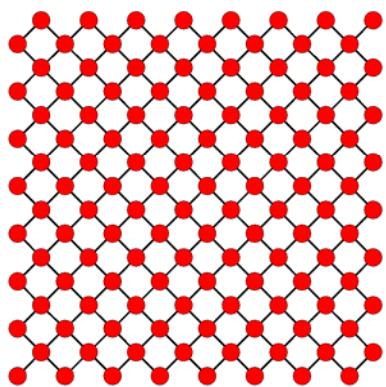
Transport

Cut along the transport direction x in the nanowire

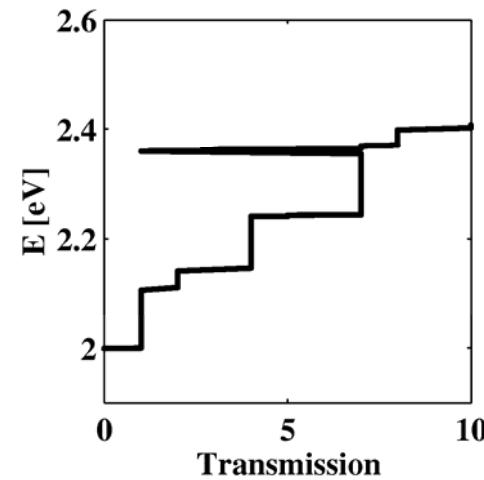
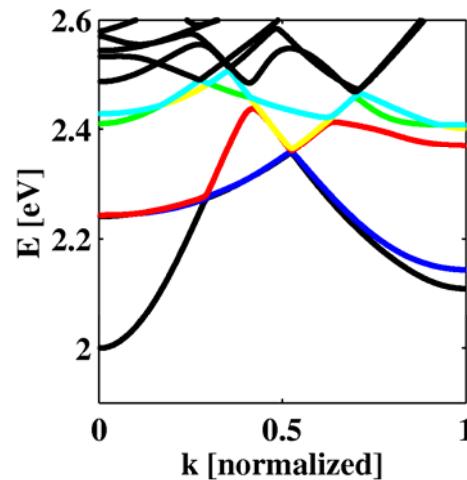
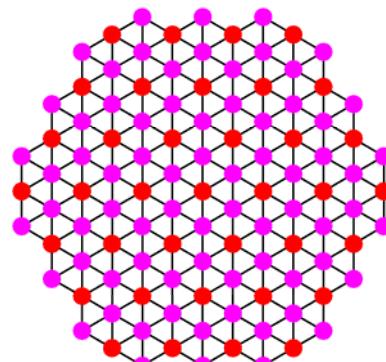
Wave functions are injected from the reservoirs and either **reflected** or **transmitted** to the other side. Band structure of reservoirs can be calculated because semi-infinite. At each energy all the k-states with **positive** (left) or **negative** (right) **velocity** are selected for injection.

Transport

Si [100]

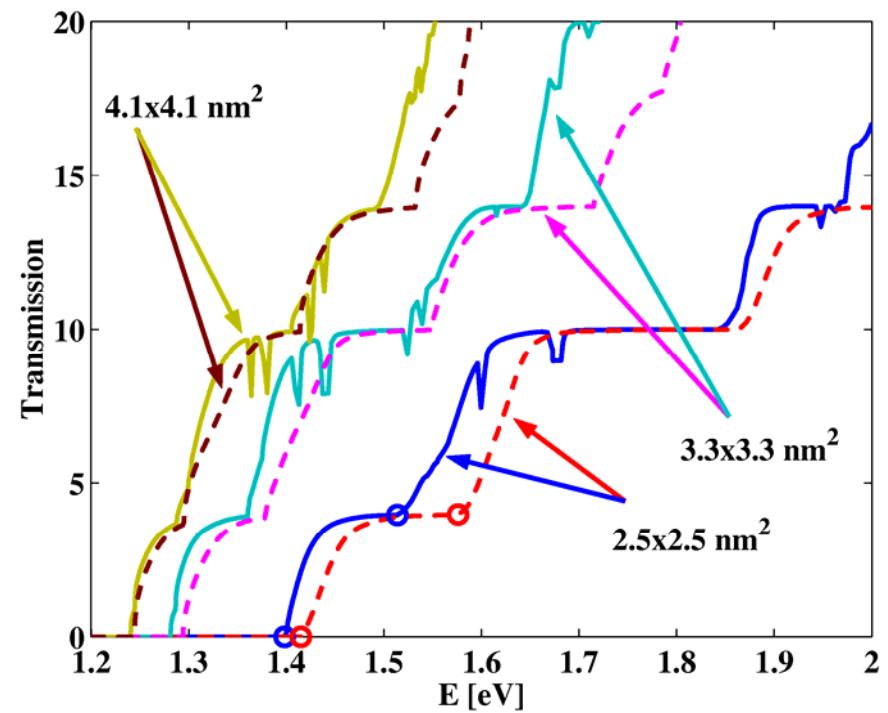
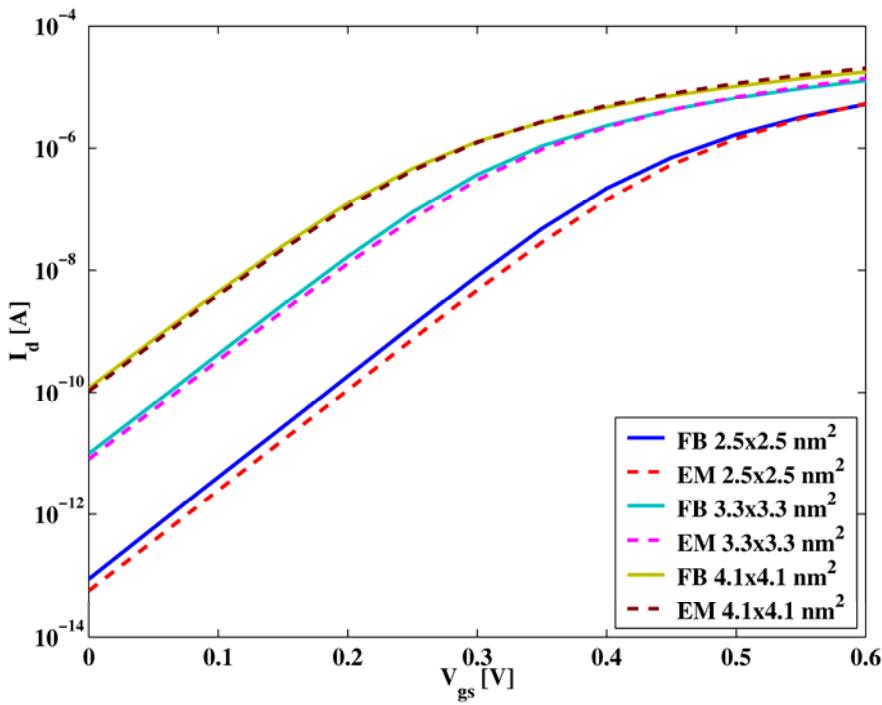


GaAs [111]



Transport

Output characteristics and transmission for [100]
Full Band (solid lines) vs Effective Mass (dashed lines)



Transport

WF formalism**Schrödinger Equation**

$$H|\psi_E\rangle = E|\psi_E\rangle$$

Tight-Binding ansatz for the wave function

$$\langle \mathbf{r} | \psi_E \rangle = \sum_{\sigma,ijk} C_{ijk}^{\sigma}(E) \phi_{\sigma}(\mathbf{r} - \mathbf{R}_{ijk})$$

Löwdin orbitals

Scattering Boundary Conditions => ordinary eigenvalue problem!!

$$M(E, A)\phi_{k(E)}(A) = \lambda(k(E))\phi_{k(E)}(A)$$

Final form of the problem in the Wave Function formalism

$$\mathbf{H}_{tot} \cdot \mathbf{C}_{p,n}^{\sigma}(k) = \mathbf{I}_{0,p,n}(k)$$

Injection matrix

Orbital-coefficient vector

Transport

Carrier and current density

$$n(x, \mathbf{r}_s) = \frac{1}{N_x} \sum_{n,p,\sigma} \sum_i \sum_{\mathbf{R}_s} |C_{i,p,n}^{\sigma}(\mathbf{R}_s, k)|^2 f(E_{p,n}(k) - \mu_p) \delta(x - x_i) \delta(\mathbf{r}_s - \mathbf{R}_s)$$

$$\begin{aligned} \mathbf{J}(\mathbf{r}) = & \sum_{i_1, i_2} i \frac{e}{2\hbar} \sum_{p, n_p} \frac{\Delta}{2\pi} \int dE \left(H_{i_1 i_2} C_{i_2, p, n_p} C_{i_1, p, n_p}^* - C_{i_1, p, n_p} C_{i_2, p, n_p}^* H_{i_2 i_1} \right) \times \\ & \times \left| \frac{dE}{dk_{p, n_p}} \right|^{-1} f(E - \mu_p) (\mathbf{R}_{i_2} - \mathbf{R}_{i_1}) \delta(\mathbf{r} - \mathbf{R}_{i_1}) \end{aligned}$$

Alternatively, in Landauer-Büttiker formula with transmission T(E)

$$T(E) = \sum_{n,m} |C_{N_s+1, p=1, n}(k_m)|^2 \left| \frac{dE}{dk_m} \right| \left| \frac{dE}{dk_n} \right|^{-1}$$

NEGF formalism

$$n(\mathbf{r}) = -i \sum_j \int \frac{dE}{2\pi} G_{jj}^<(E) \delta(\mathbf{r} - \mathbf{R}_j)$$

$$\mathbf{J}(\mathbf{r}) = \sum_{i_1} \sum_{i_2} \frac{e}{2} \left(H_{i_1 i_2} G_{i_2 i_1}^< - G_{i_1 i_2}^< H_{i_2 i_1} \right) (\mathbf{r}_{i_2} - \mathbf{r}_{i_1}) \delta(\mathbf{r} - \mathbf{r}_{i_1})$$

Transport

WF \leftrightarrow NEGF (if no incoherent scattering)

$$G_{ij}^<(E) = \sum_p \sum_n \underbrace{C_{i,p}(k_n) C_{j,p}^T(k_n)}_{(\mathbf{t}_b \cdot \mathbf{N}_A) \times (\mathbf{t}_b \cdot \mathbf{N}_A)} \left| \frac{dE(k_n)}{dk_n} \right|^{-1} f(E(k_n) - \mu_p)$$

When NEGF? In case of incoherent scattering.

When WF? Otherwise, because CPU time is greatly reduced!

Iterative solutions ($N = \mathbf{t}_b \cdot \mathbf{N}_A$)

$$(\mathbf{E} - \mathbf{H} - \mathbf{t}_{10} \cdot \mathbf{g}_{00}^R \cdot \mathbf{t}_{01}) \cdot \mathbf{g}_{00}^R = \mathbf{I}$$

Generalized eigenvalue problem ($N = 2 \mathbf{t}_b \cdot \mathbf{N}_A$)

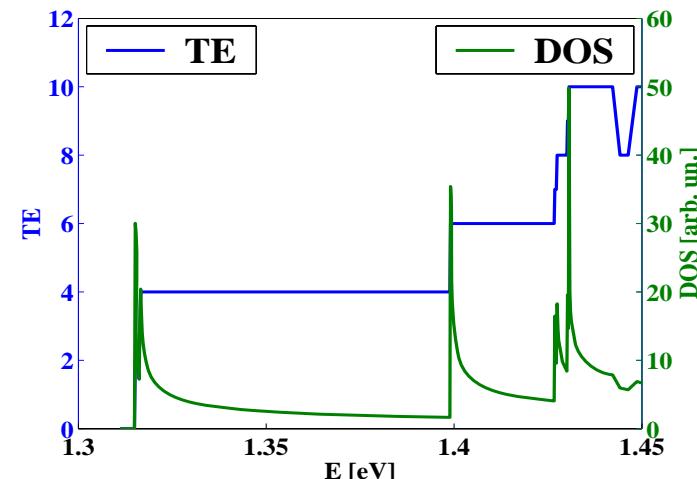
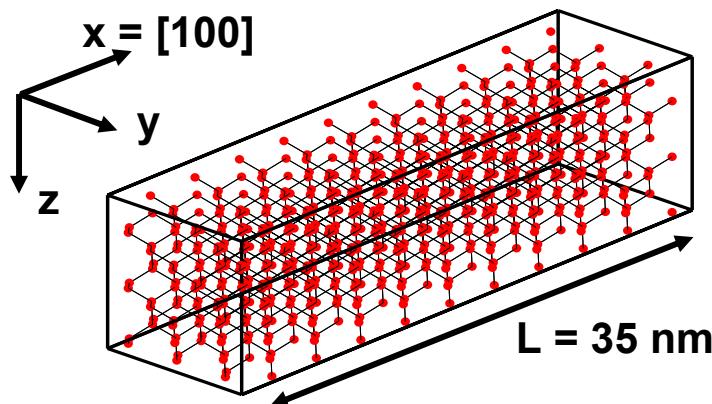
$$\mathbf{A}(\mathbf{E}) \cdot \mathbf{C}_n = \exp(i\mathbf{k}_n(\mathbf{E})\Delta) \cdot \mathbf{B}(\mathbf{E}) \cdot \mathbf{C}_n$$

Shift-and-invert + ordinary eigenvalue problem ($N < \mathbf{t}_b \cdot \mathbf{N}_A$) (PRB 74, 205323 (2006))

$$\mathbf{M}(\mathbf{E}) \cdot \mathbf{C}_n = \lambda_n(\mathbf{k}_n(\mathbf{E})) \cdot \mathbf{C}_n$$

Transport

Benchmark example: 35 nm long [100] nanowire, 1 energy point



First task: Open Boundary Conditions

$L_y \times L_z \text{ nm}^2$	$t_b \times N_A$	Iterative Solver	Generalized EVP	Ordinary EVP
2.5×2.5	1810	197	506	7.2
2.9×2.9	2420	462	1490	18.5
3.3×3.3	3130	1070	3930	39

All CPU times (in sec) obtained on a Sun Fire with $8 \times 2.8 \text{ GHz}$ AMD processors

Transport

Benchmark example: 35 nm long [100] nanowire, 1 energy point

Second task: Transport problem

#CPU	Umfpack	Pardiso	SuperLU _{dist}	MUMPS	Basis Compression	Recursive GF
1	406	271	560	240	105	1418
2	-	141	258	129	54	-
4	-	84	130	76	31	-
8	-	63	112	56	21	-

The diagram shows a horizontal double-headed arrow spanning the width of the table. Below the arrow, the text "Wave Function" is centered under the first two columns, and "NEGF" is centered under the last five columns.

All times in sec for a 3.3×3.3×35 nm³ NW without SO coupling

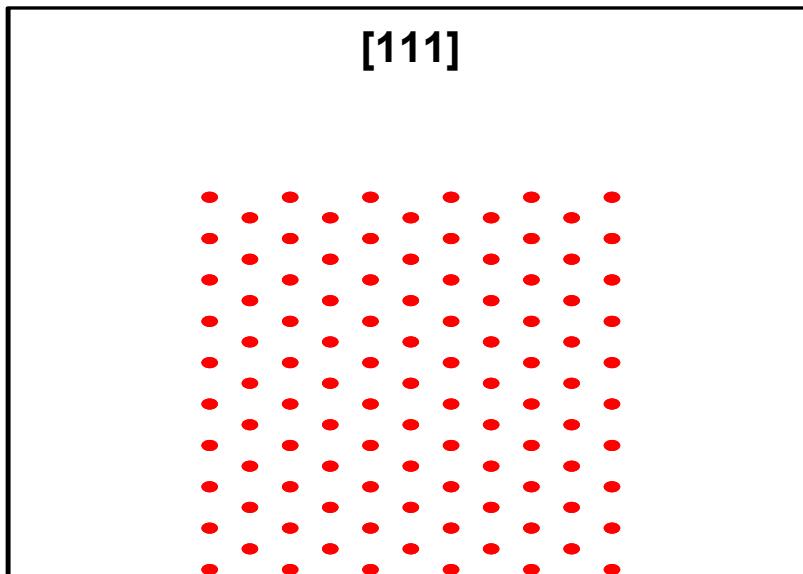
Electrostatics

Grid Generation for Poisson equation

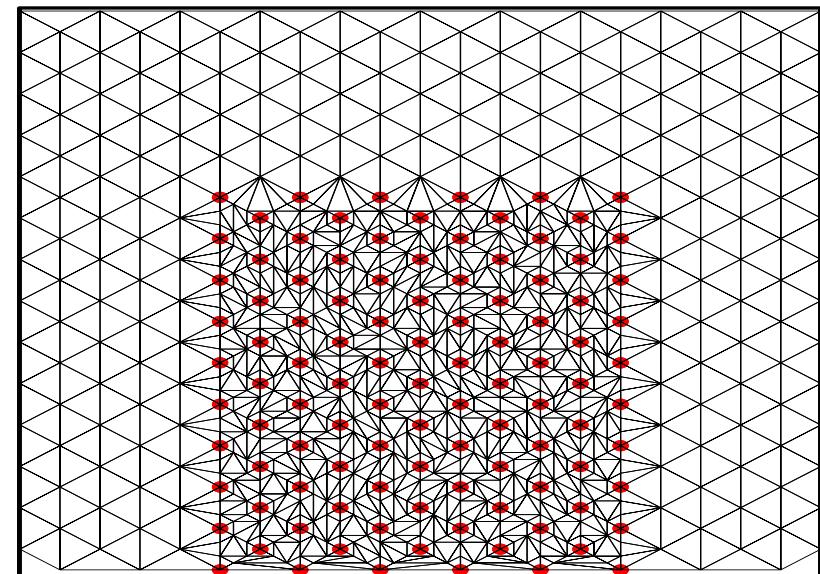
Grid must be general => Delaunay mesh: no data point (atoms) is contained in any triangle's circumcircle (2D) or in any tetrahedron's circumspheres (3D).

Carriers localized around atom positions

$$n(\mathbf{r}) = \sum_i n_i \delta(\mathbf{r} - \mathbf{r}_i)$$



Projection of FEM mesh on cross section.
No charge in the oxide => larger elements



Electrostatics

Poisson Equation

$$\nabla \epsilon \nabla V(\mathbf{r}) = -q (N_D^+(\mathbf{r}) - n(\mathbf{r}))$$

Carrier Density

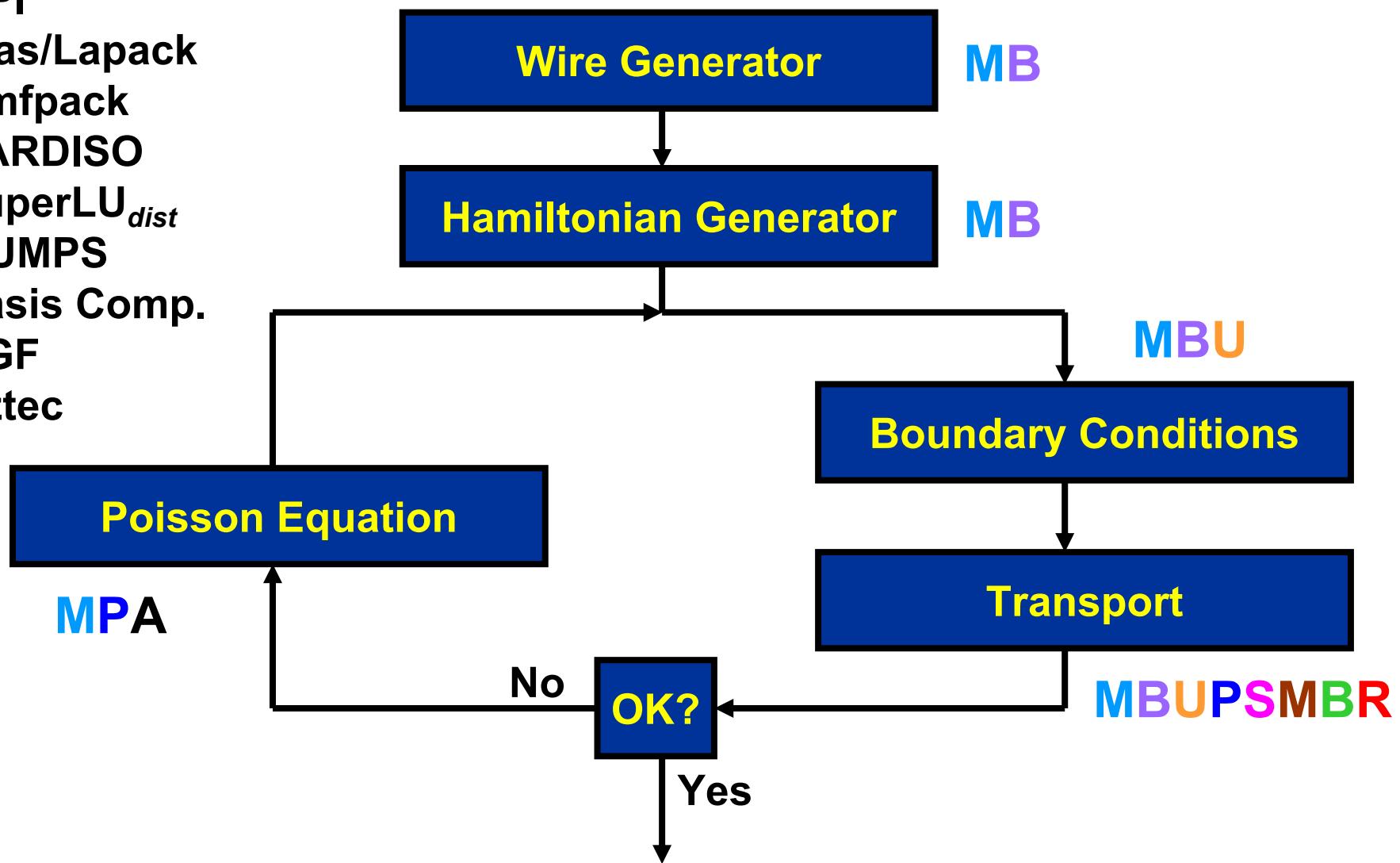
$$n(\mathbf{r}) = \sum_i n_i \delta(\mathbf{r} - \mathbf{r}_i)$$

Solution: Finite Element Method (FEM)

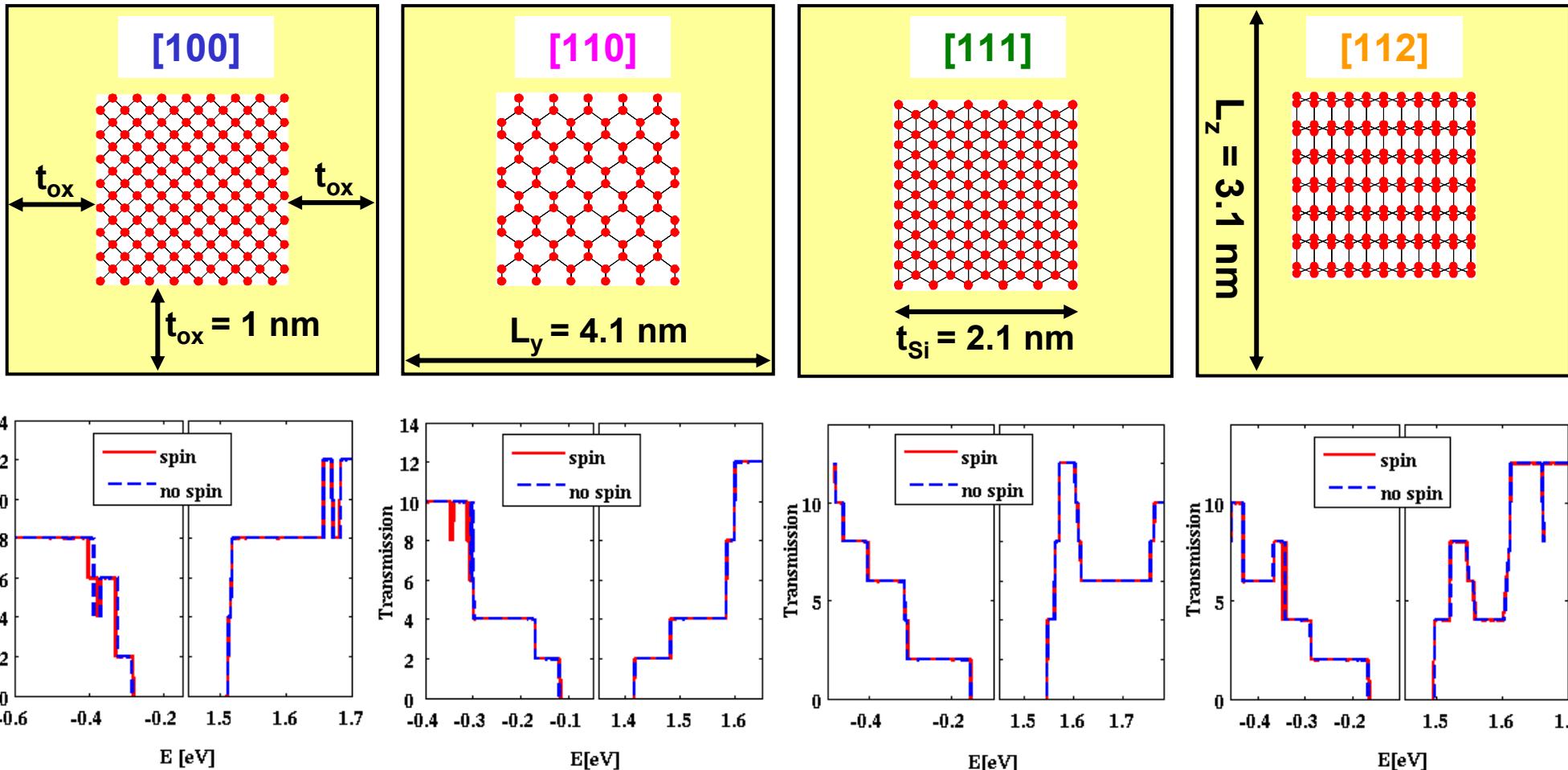
$$\int dV \psi(\mathbf{r}) \nabla \epsilon \nabla V(\mathbf{r}) = -q \int dV \psi(\mathbf{r}) (N_D^+(\mathbf{r}) - n(\mathbf{r}))$$

$$\int dV \psi(\mathbf{r}) n(\mathbf{r}) = \sum_i n_i \psi(\mathbf{r}_i)$$

- MPI
- Blas/Lapack
- Umfpack
- PARDISO
- SuperLU_{dist}
- MUMPS
- Basis Comp.
- RGF
- Aztec

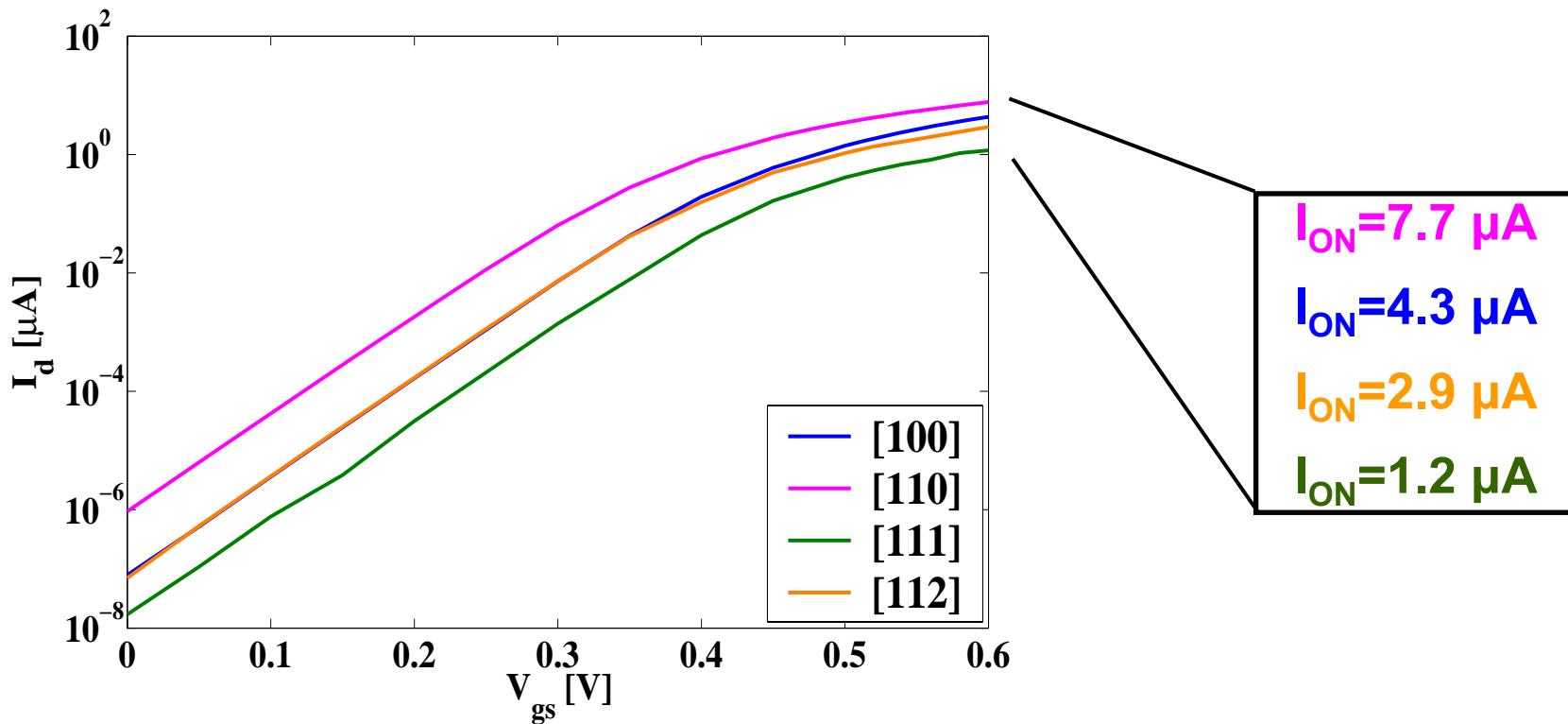


How does transmission change with channel orientation?

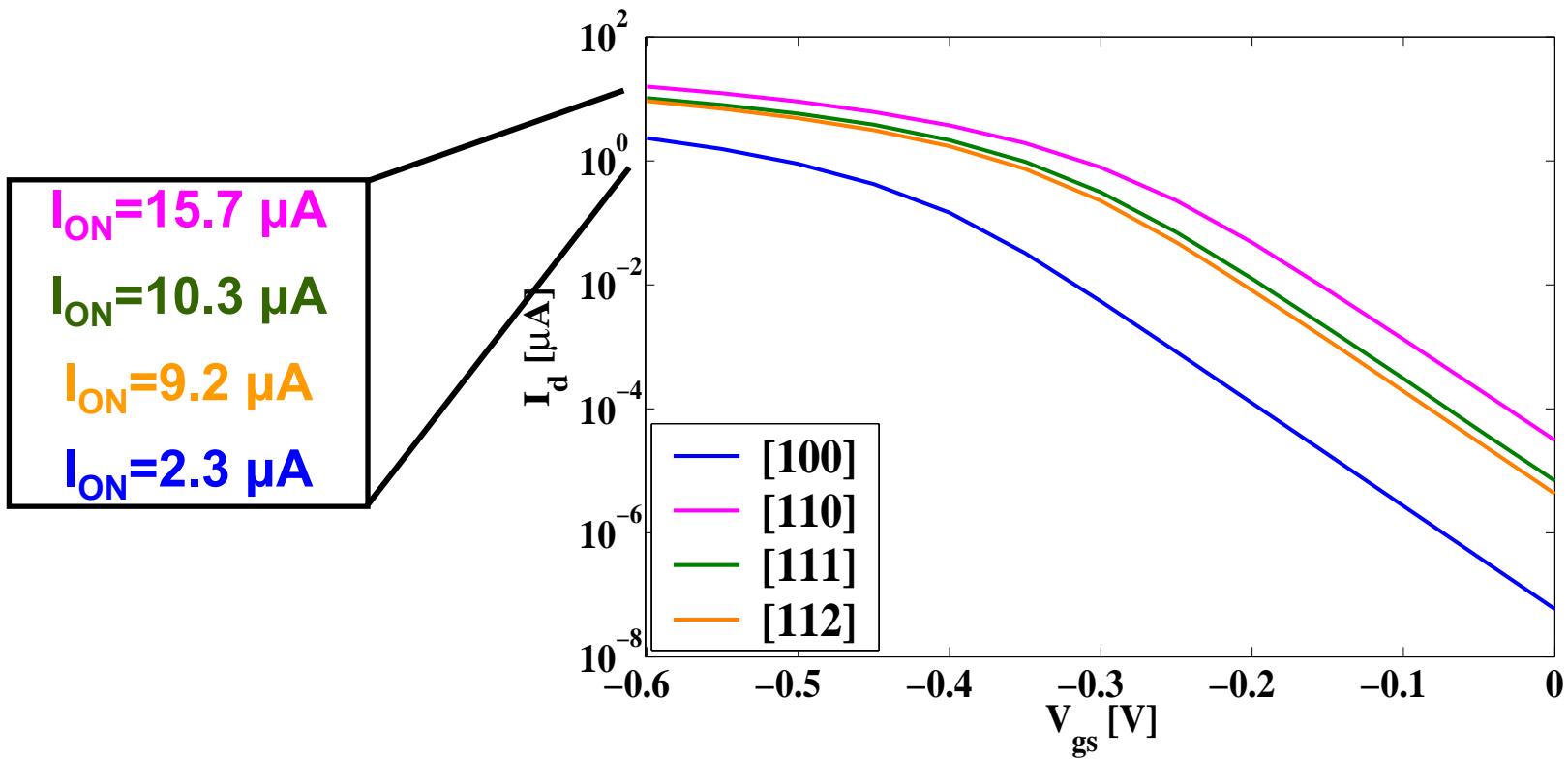


How does current depend on channel orientation?

**Full-band (FB) transfer characteristics: I_d - V_{gs} at $V_{ds}=0.4$ V
n-FET with [100], [110], [111], and [112], $L_g=13$ nm**

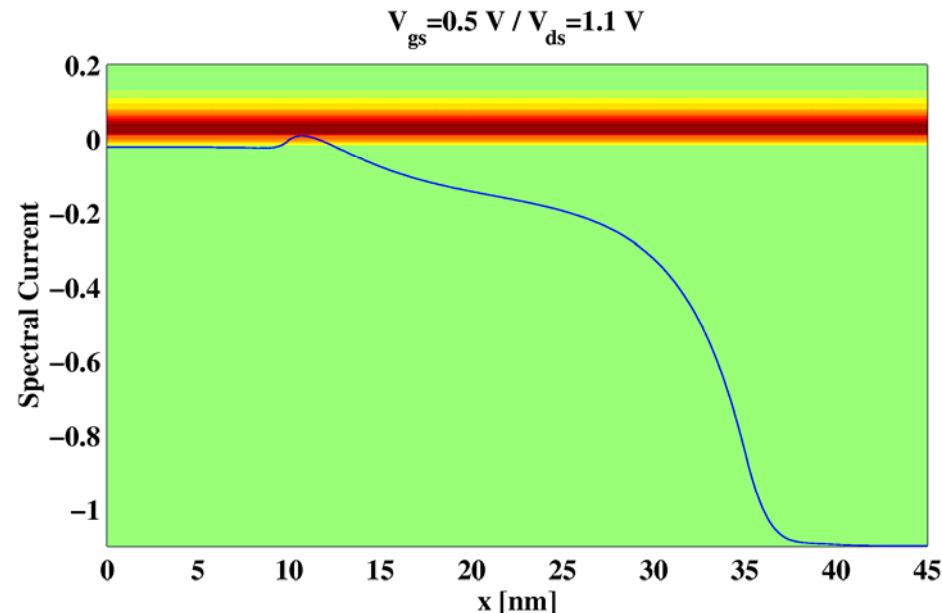
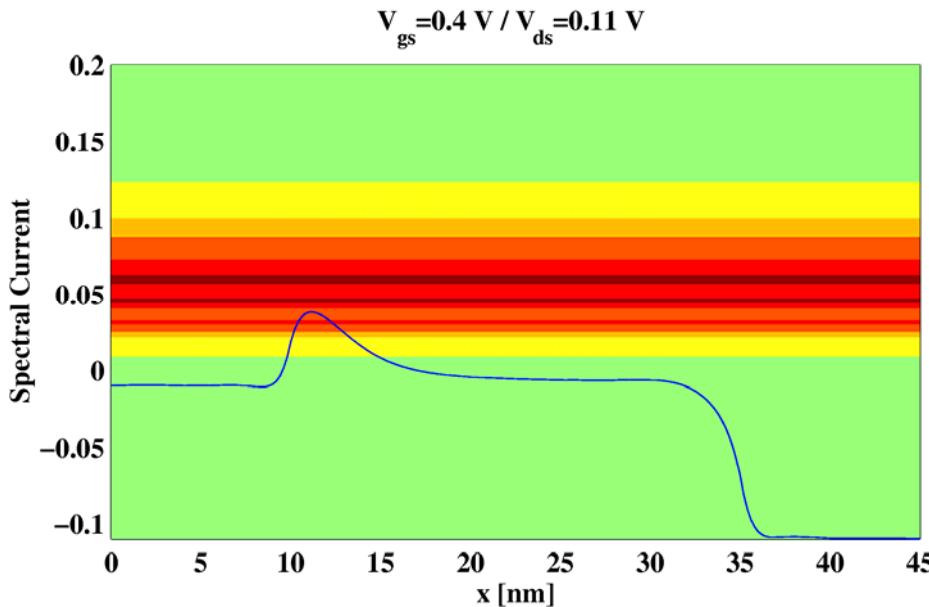


Full-band (FB) transfer characteristics: I_d - V_{gs} at $V_{ds} = -0.4$ V
p-FET with [100], [110], [111], and [112], $L_g = 13$ nm



Quantum-ballistic spectral currents

Can we trust the high quantum-ballistic ON-currents?



Spectral currents at $V_{gs} = 0.4 \text{ V}$, $V_{ds} = 0.11 \text{ V}$ (left) and $V_{gs} = 0.5 \text{ V}$, $V_{ds} = 1.1 \text{ V}$ (right).

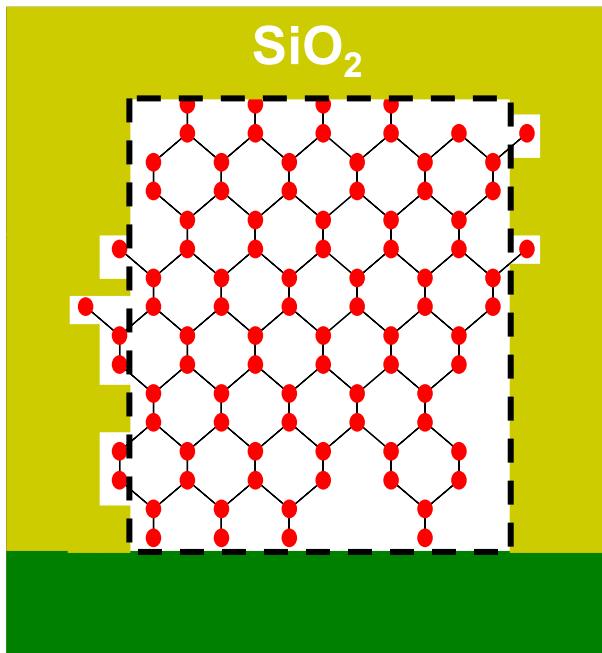
There is a strong injection-induced tunneling part of the ON-current. This is a quantum-ballistic artifact (traveling states from source carry their Fermi level to the drain, negligible back-scattered states, too low density, Poisson equation shifts the conduction band down, deformation of S-D barrier, strong tunneling).

How does interface roughness influence the current?

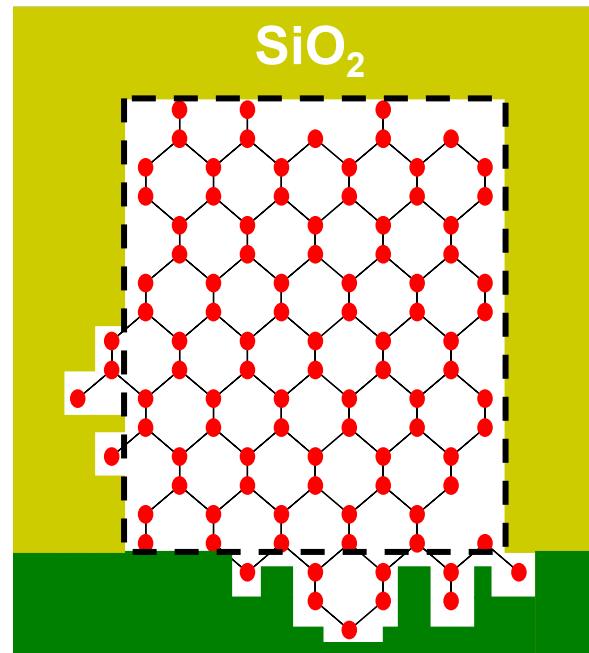
Process variations => cross section variations

Example: [110] nanowire

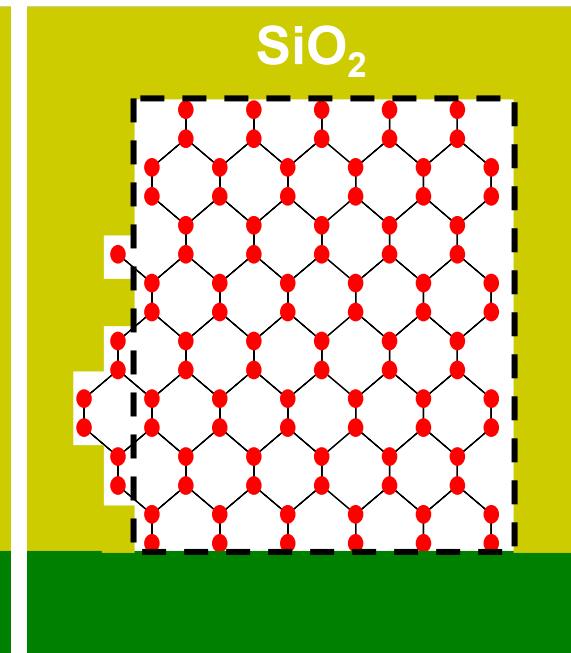
$x=14 \text{ nm}$



$x=16 \text{ nm}$

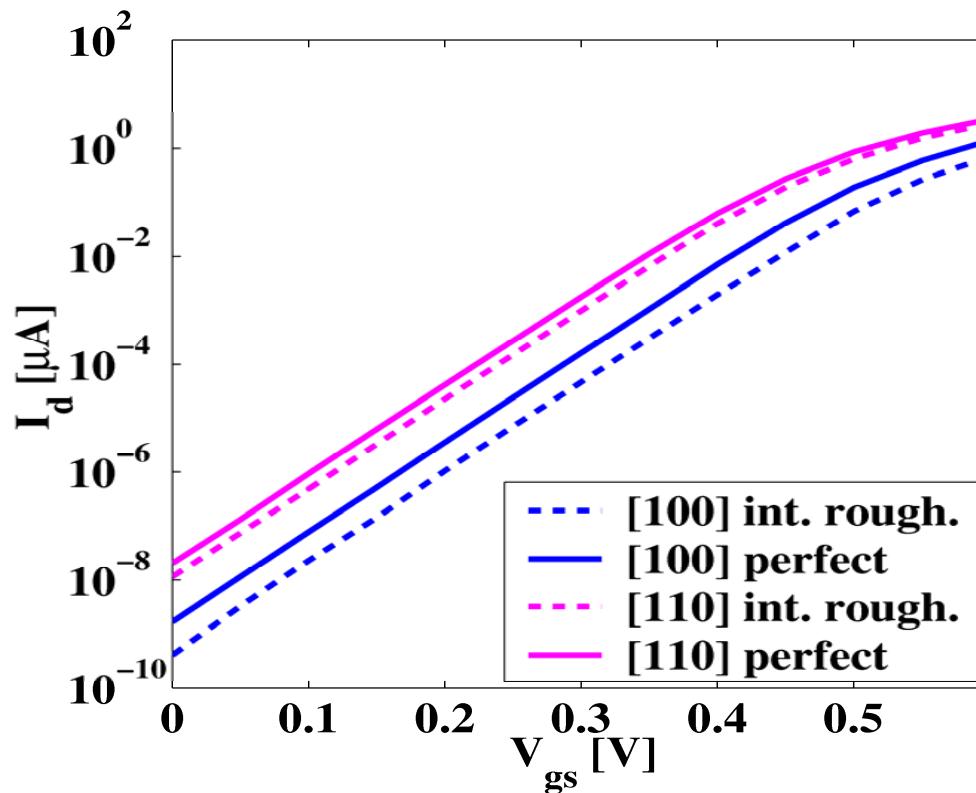


$x=26 \text{ nm}$



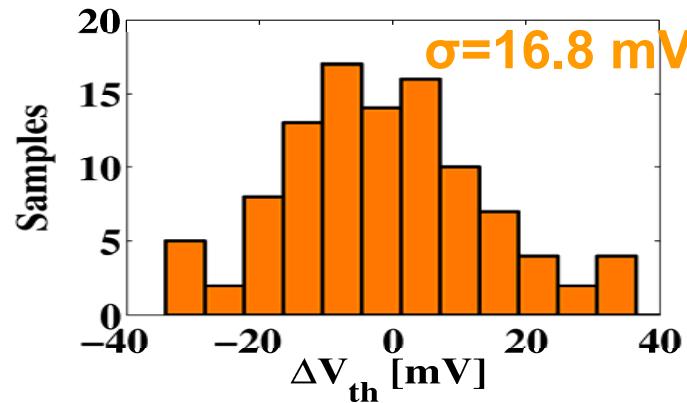
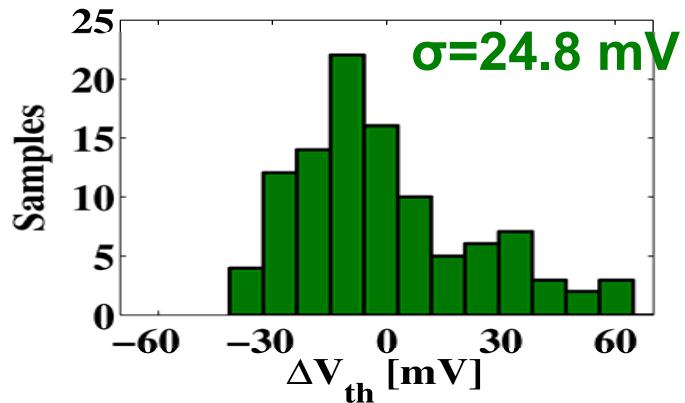
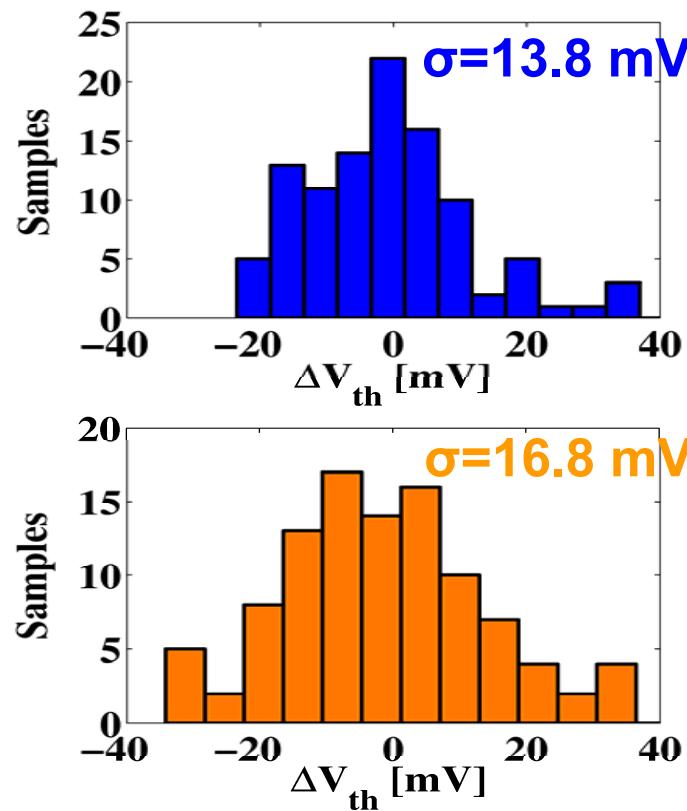
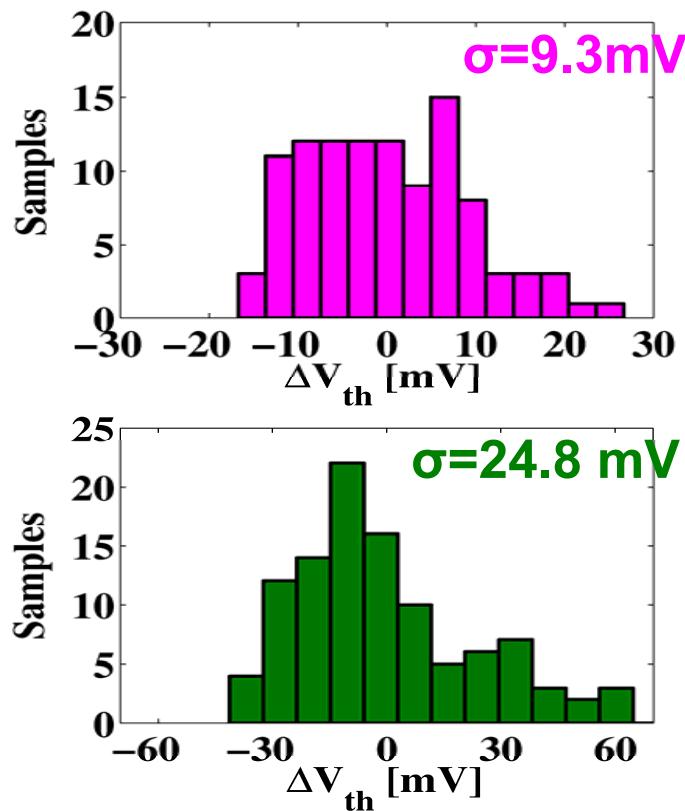
$$\text{interface roughness scattering: } S(x) = \Delta^2 \exp(-|x|/L_m)$$

FB I_d - V_{gs} at $V_{ds}=0.4$ V for one possible interface realization



- 1) Sub-threshold swing remains constant: $S \approx 60$ mV/dec.
- 2) Threshold voltage V_{th} ↑, drain current I_d ↓

Variation of the threshold voltage V_{th} at $V_{ds}=0.4$ V
[110], [100], [111], and [112]



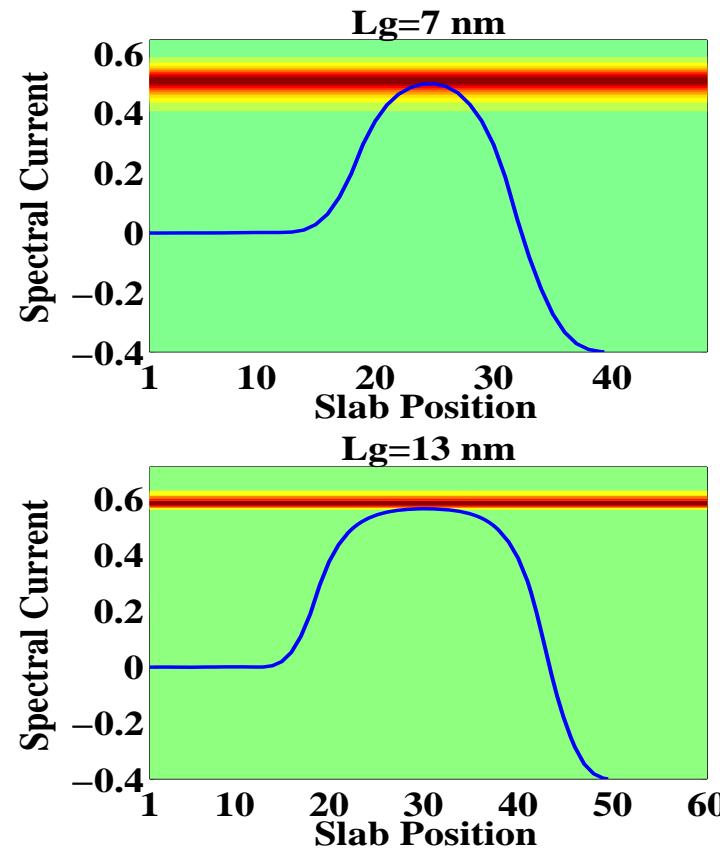
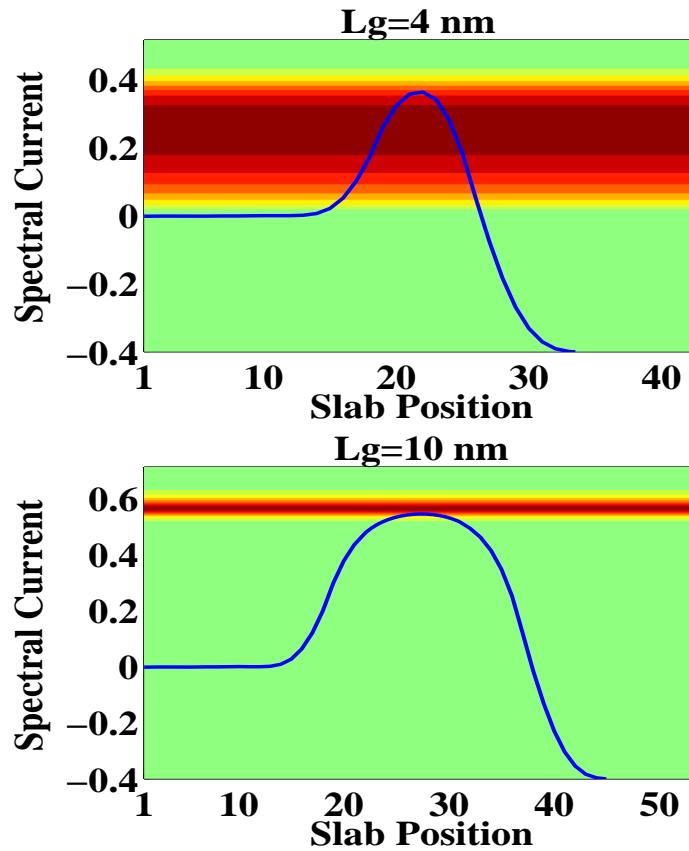
Performance summary: ON-current, OFF-current, roughness

	n- I_{on} [μA]	p- I_{on} [μA]	σ [mV]
[110]	7.7	15.7	9.3
[100]	4.3	2.3	13.8
[112]	2.9	9.2	16.8
[111]	1.2	10.3	24.8

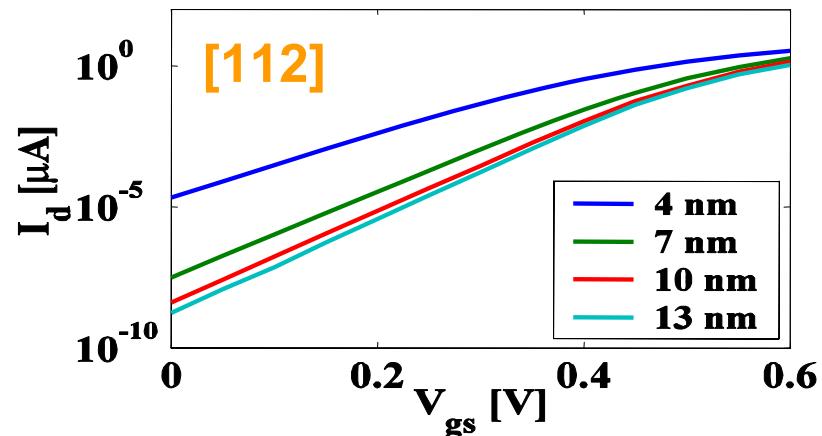
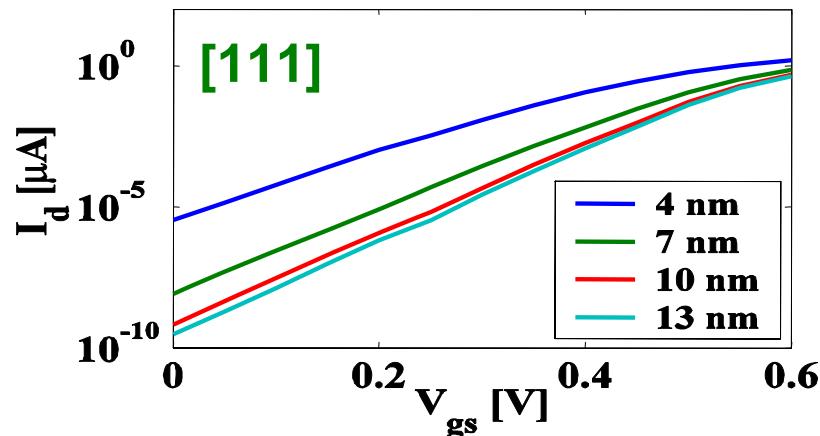
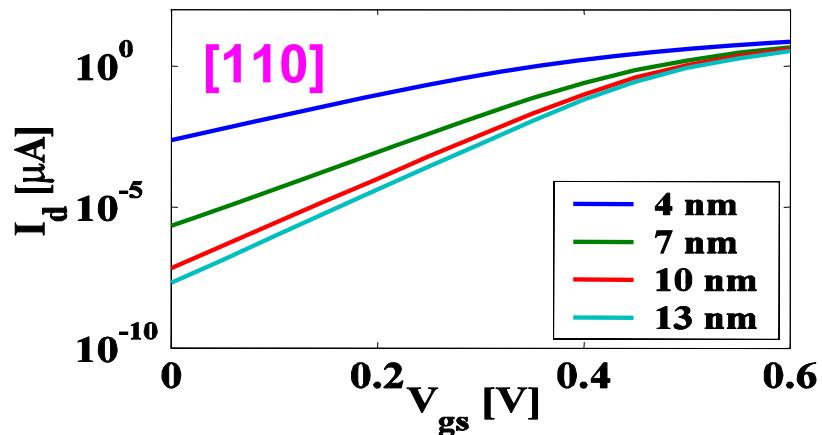
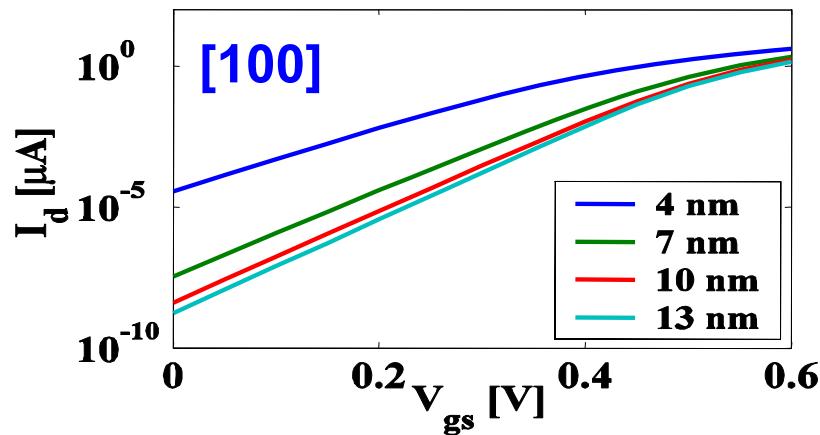
[110] has the highest on-current, is the least sensitive to interface roughness

Simulation of tunneling-induced OFF-currents

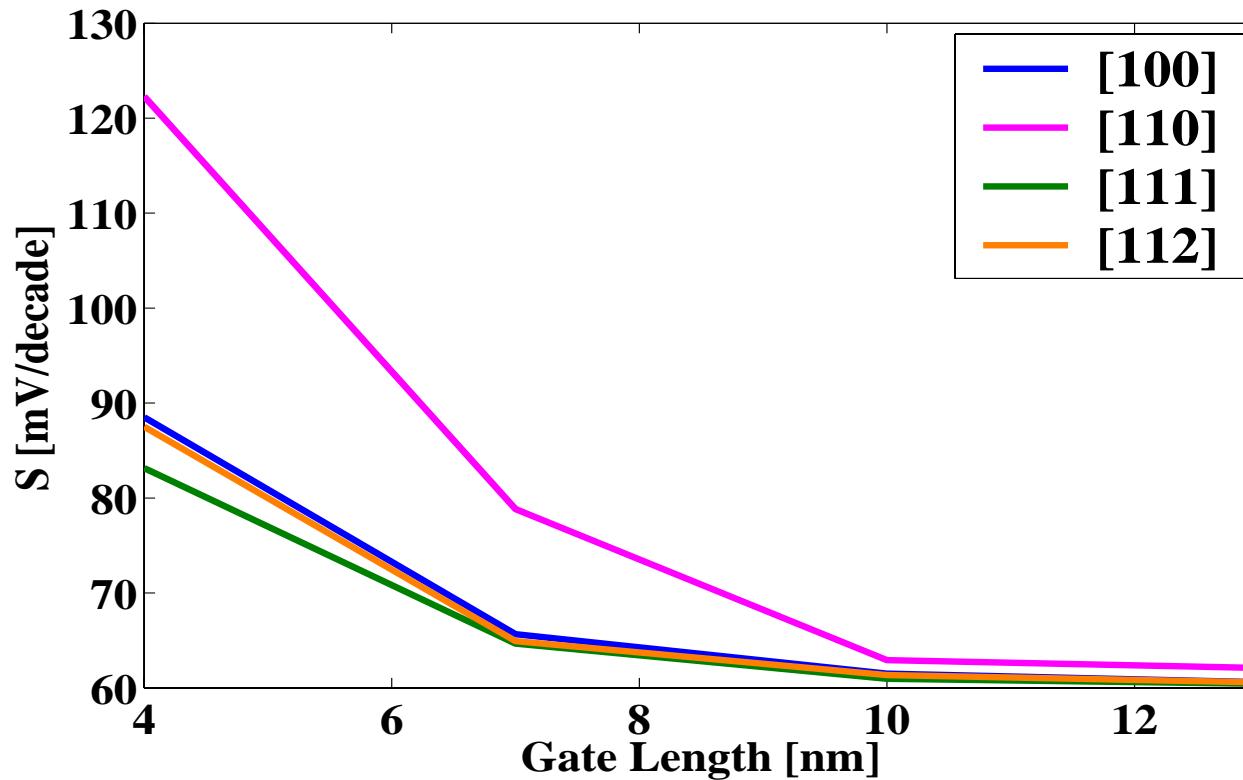
L_g influence for nanowire n-FET with [100] channel



I_d - V_{gs} @ $V_{ds}=0.4$ V for 4 different channel lengths (4 nm, 7 nm, 10 nm, and 13 nm) and for [100], [110], [111], [112]



Sub-threshold swing S as function of gate length L_g
Low effective mass => high on-current / strong tunneling

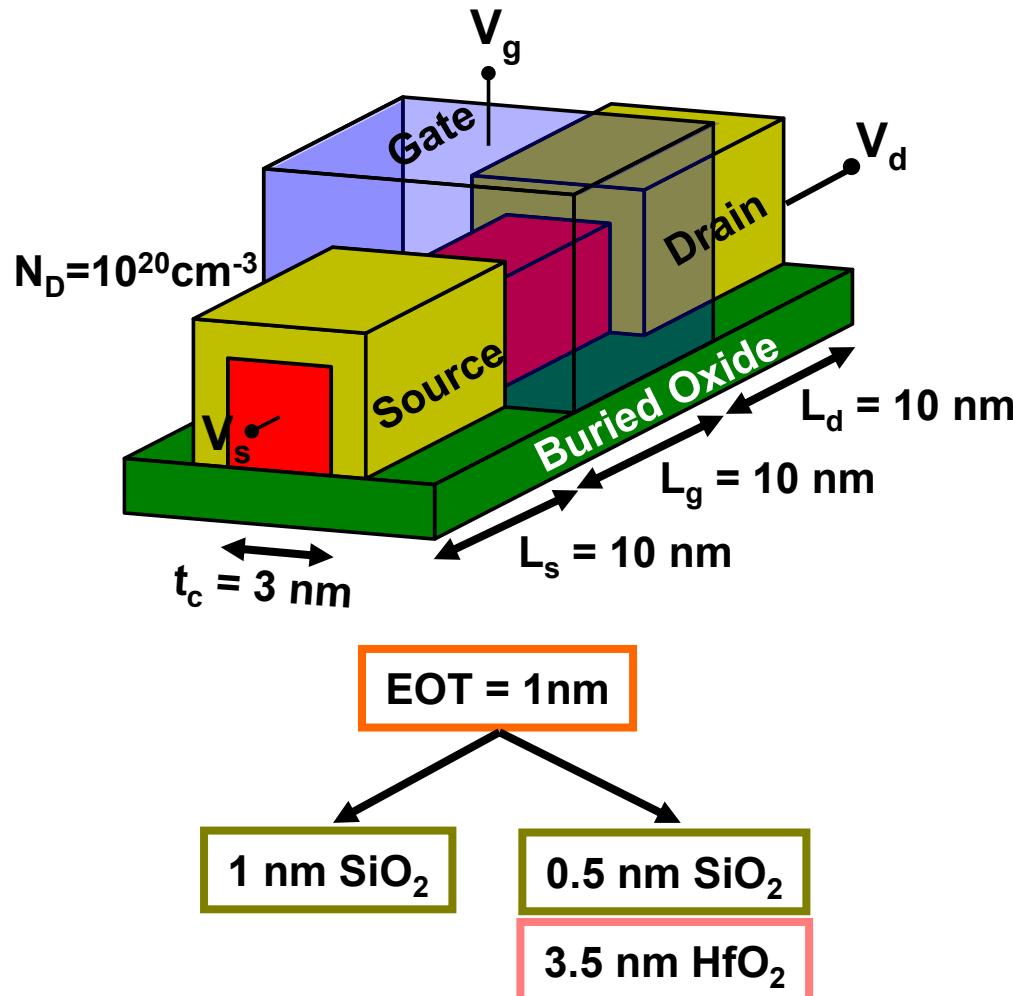


Performance summary: ON-current, OFF-current, roughness, S-D leakage

	n- I_{on} [μA]	p- I_{on} [μA]	σ [mV]	S @ $L_g=4$ nm
[110]	7.7	15.7	9.3	122.3
[100]	4.3	2.3	13.8	88.5
[112]	2.9	9.2	16.8	87.5
[111]	1.2	10.3	24.8	83.2

[110] has the highest on-current, is the least sensitive to interface roughness, but suffers the most from source-to-drain tunneling

Triple-gate nanowire FET with poly-Si or TiN contacts



Popular 3D mode-space approx. not suited => multi-terminal real space simulator (eff. mass!)

3D Schrödinger equation

$$\mathbf{H} |\Psi_E\rangle = E |\Psi_E\rangle$$

eff. mass approx. + finite difference

$$\langle \mathbf{r} | \Psi_E \rangle = \sum_{ijk} C_{ijk}(E) \delta(\mathbf{r} - \mathbf{R}_{ijk})$$

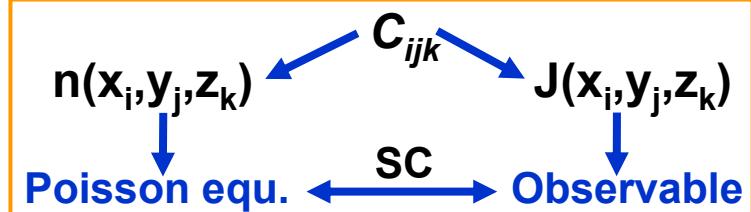
3D sparse linear problem $\mathbf{A}\mathbf{x}=\mathbf{b}$

$$(\mathbf{E} - \mathbf{H} - \Sigma_S - \Sigma_D - \Sigma_G) \cdot \mathbf{C} = \mathbf{S}_{\text{Inj}} + \mathbf{D}_{\text{Inj}} + \mathbf{G}_{\text{Inj}}$$

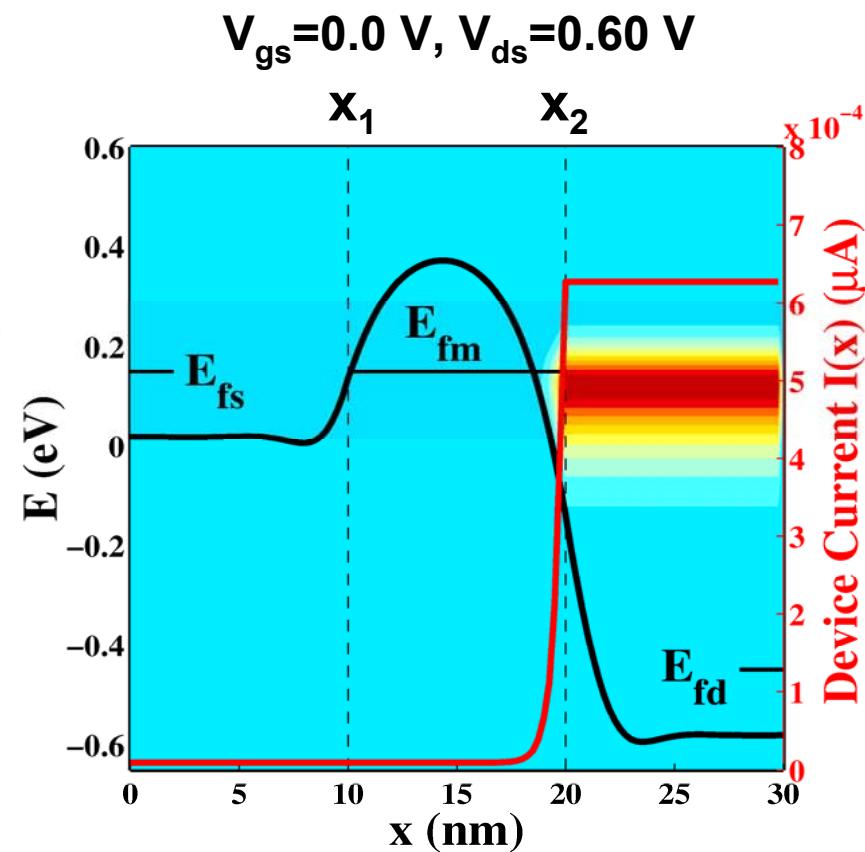
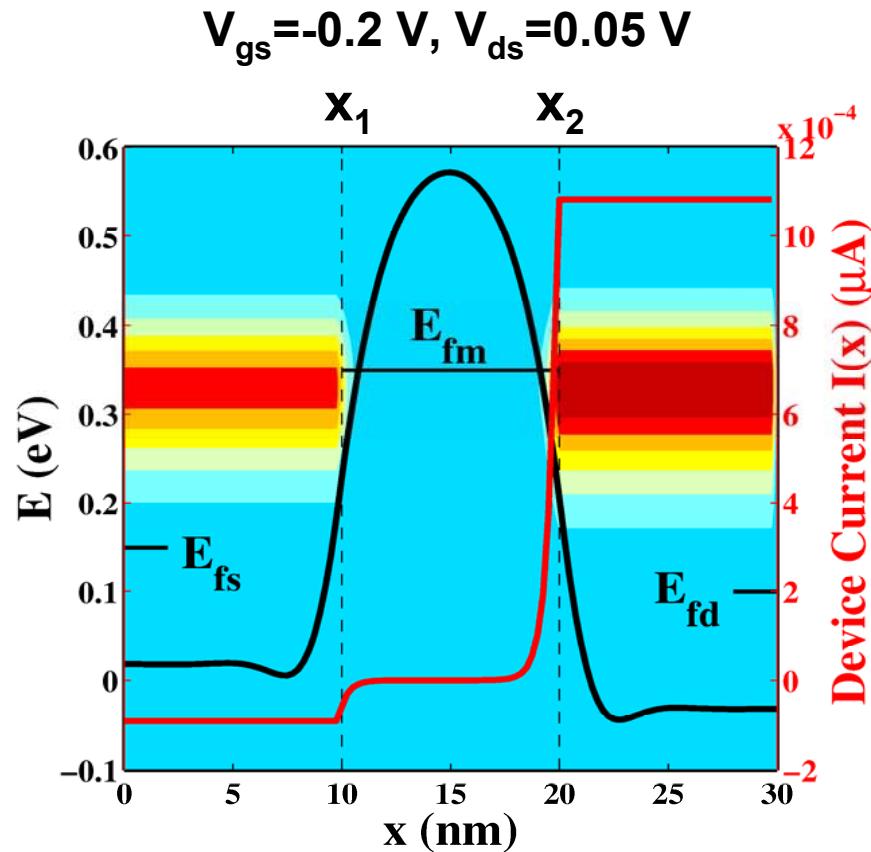
BCs and injection mechanism

$$\mathbf{M} \cdot \mathbf{C}_B = 2 \cdot \cos(k_B) \cdot \mathbf{C}_B$$

3D carrier and current densities



Spectral gate current and total device current along the x -axis



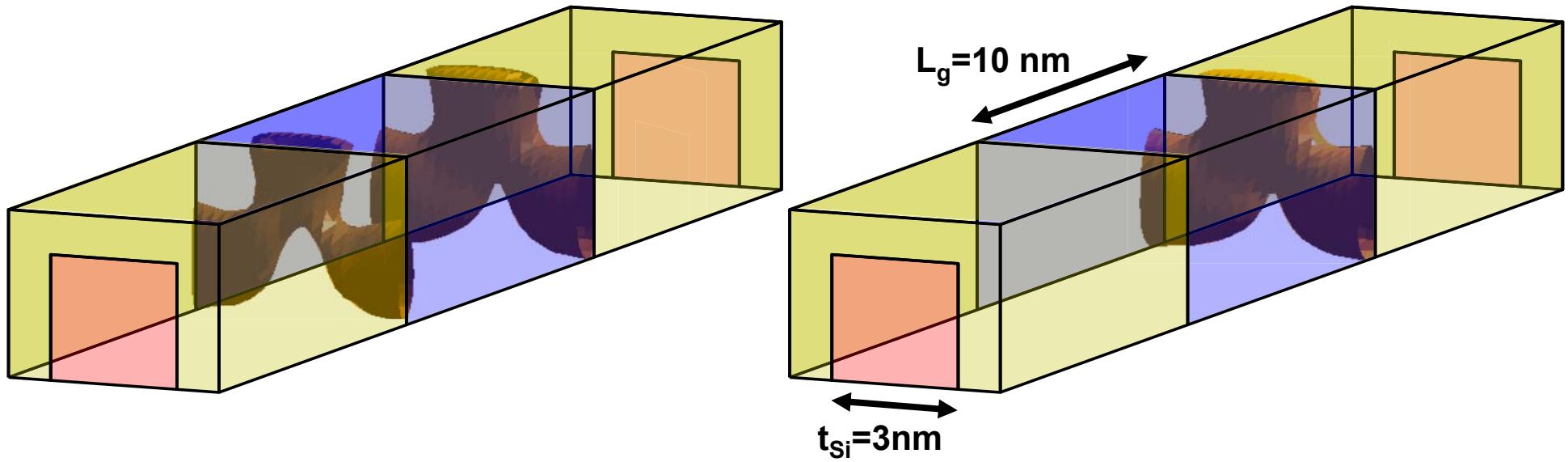
current conservation: $I(x_2) - I(x_1) = I_G$

Isosurfaces of the gate current for a triple-gate structure
 SiO_2 dielectric layer + TiN metal contact

Current escapes at the **gate corners**

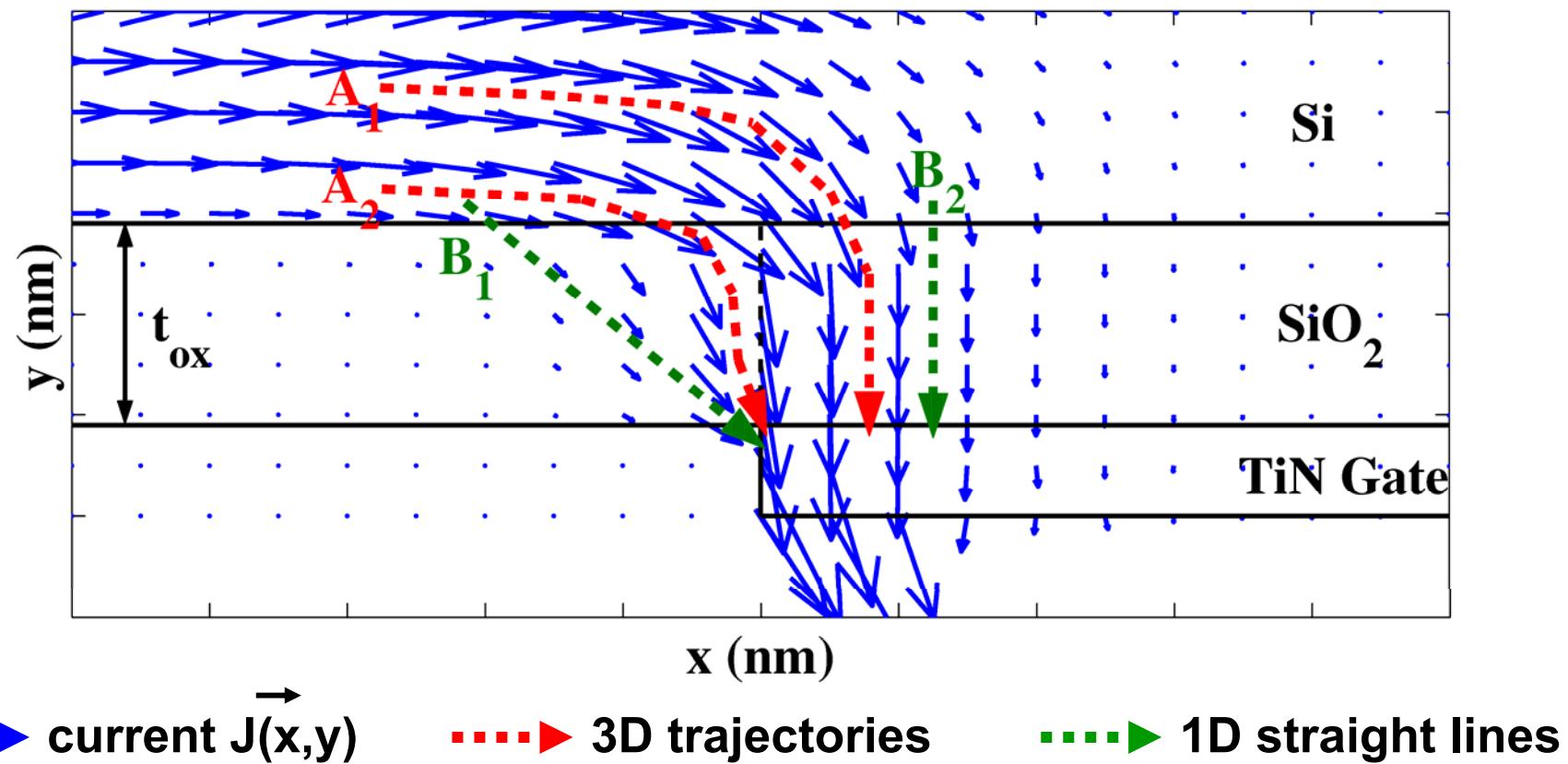
$$V_{gs} = -0.2 \text{ V}, V_{ds} = 0.05 \text{ V}$$

$$V_{gs} = 0.0 \text{ V}, V_{ds} = 0.60 \text{ V}$$



Current trajectories around gate corner

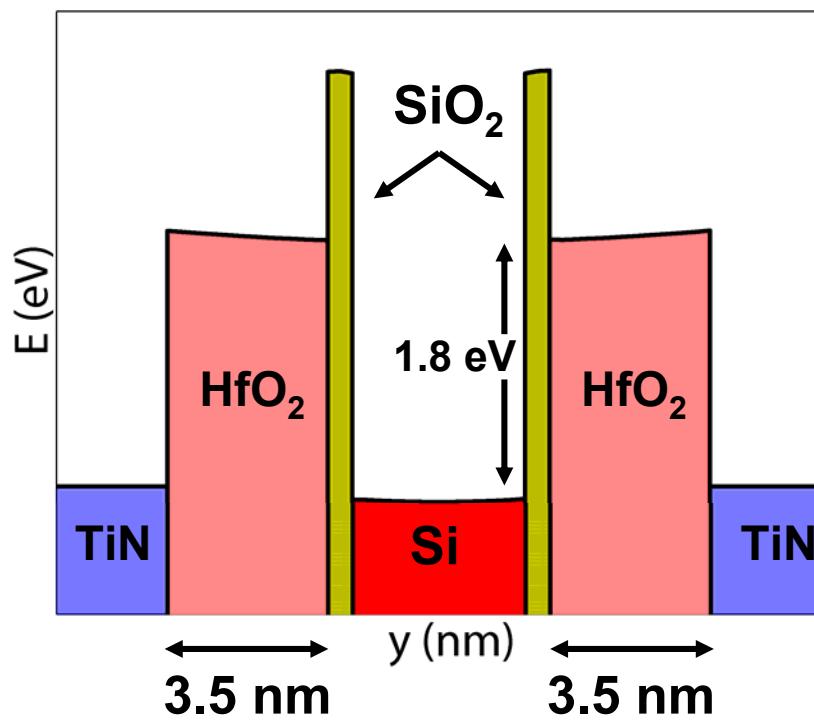
1D approximation vs full 3D (projected)



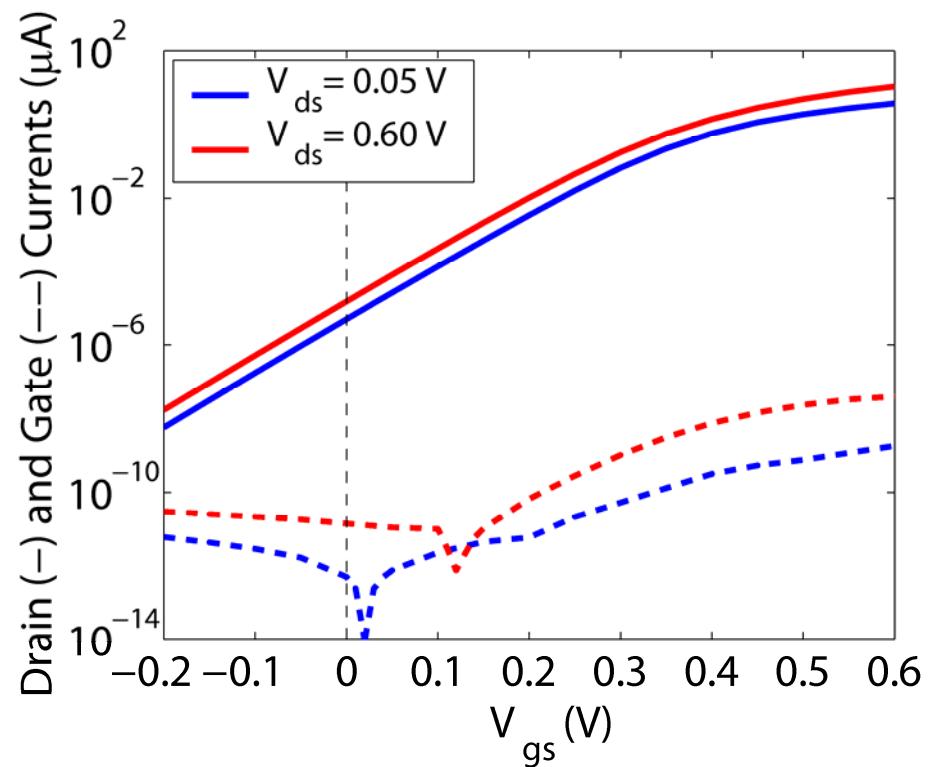
Gate stack: SiO_2 (0.5 nm) + HfO_2 (3.5 nm, $m^* = 0.2 m_0$, $\epsilon_R = 25$)

Performance: Good threshold voltage V_{th} , low off-current I_{OFF}

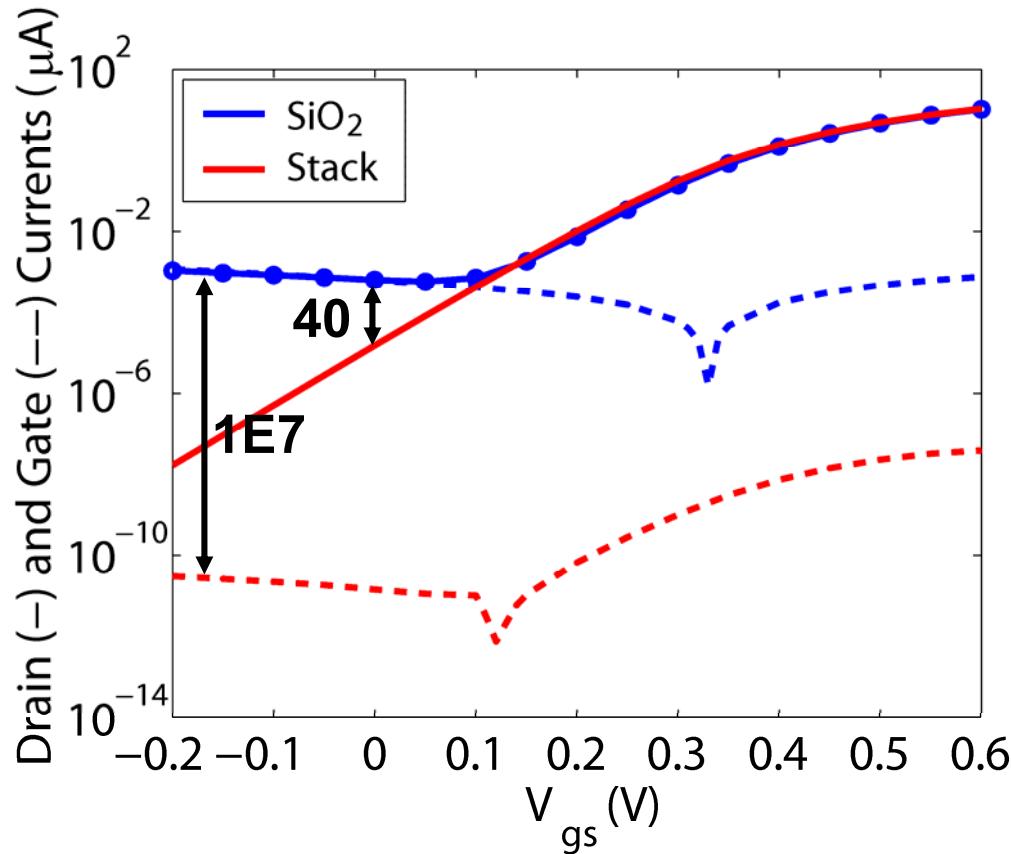
Dielectric + Contact Structure



Transfer Characteristics



Stack reduces **gate current** by 7 orders of magnitude at low V_{gs} , **off-current** by a factor of 40, and keeps the same **on-current**



Phonon-assisted band-to-band tunneling is an important leakage mechanism in steep pn-junctions (with a doping level of 10^{19} cm^{-3} or more on both sides) or in high normal electric fields of MOS structures.

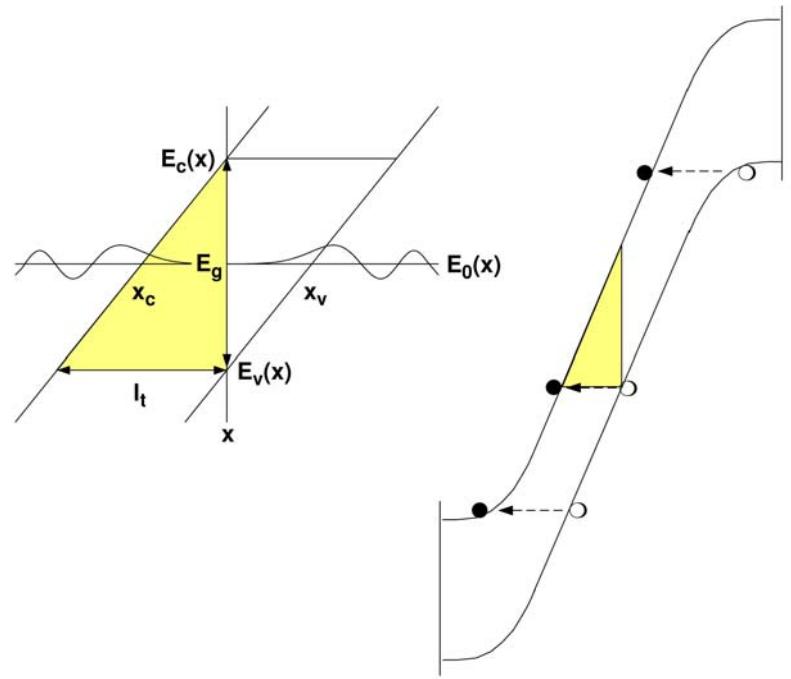
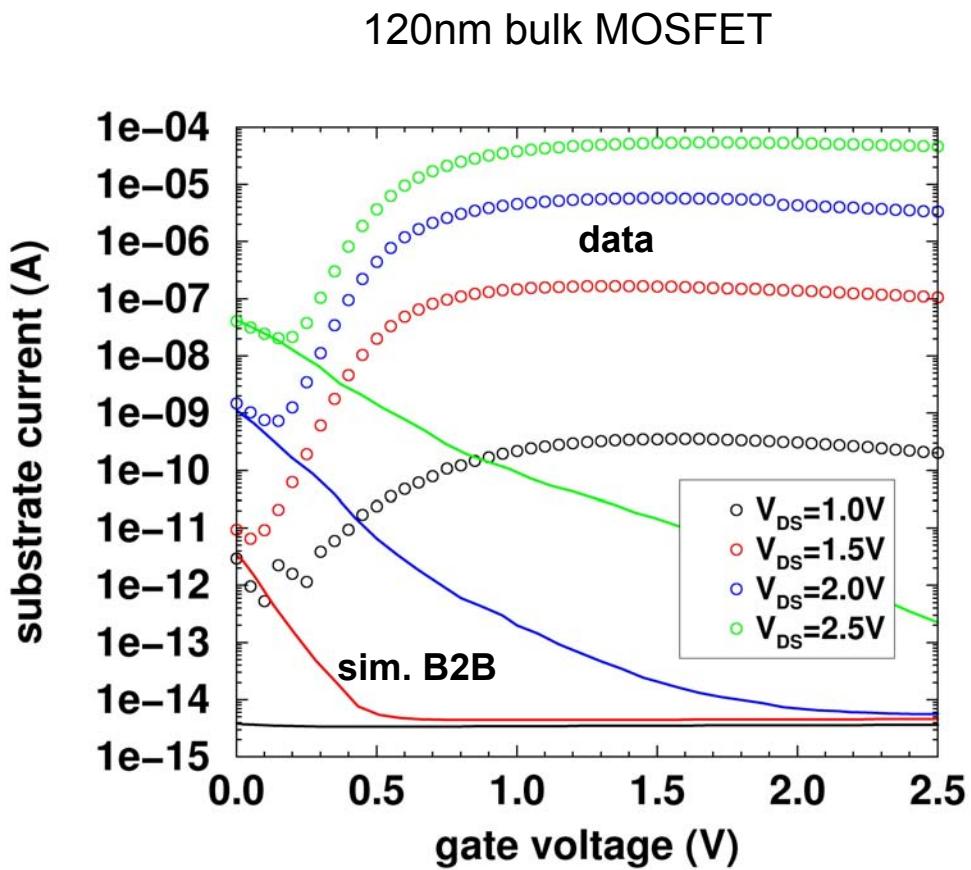
$$R_{\text{net}}^{\text{bb}} = AF^{7/2} \frac{\tilde{n}\tilde{p} - n_{i,\text{eff}}^2}{(\tilde{n} + n_{i,\text{eff}})(\tilde{p} + n_{i,\text{eff}})} \left[\frac{(F_C^\mp)^{-3/2} \exp\left(-\frac{F_C^\mp}{F}\right)}{\exp\left(\frac{\hbar\omega}{kT}\right) - 1} + \frac{(F_C^\pm)^{-3/2} \exp\left(-\frac{F_C^\pm}{F}\right)}{1 - \exp\left(-\frac{\hbar\omega}{kT}\right)} \right]$$

Non-local nature of the B2B rate can be modeled in a simple way:

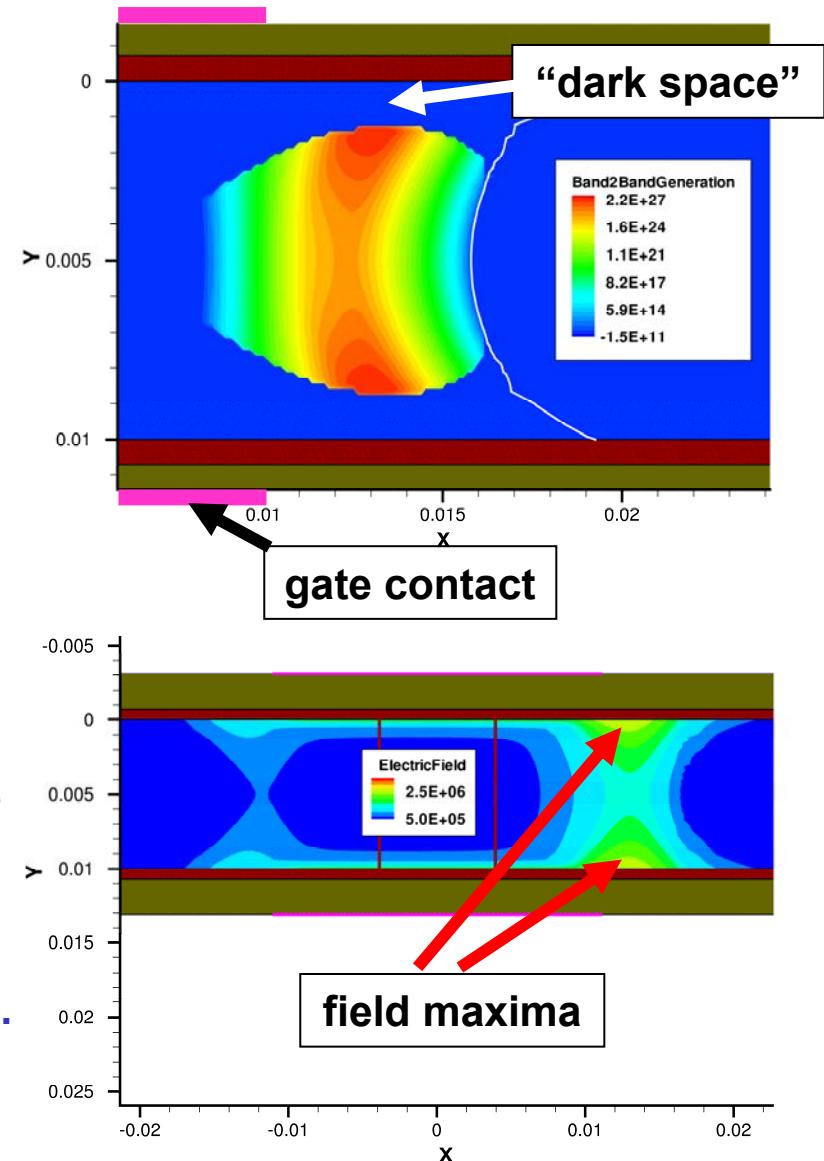
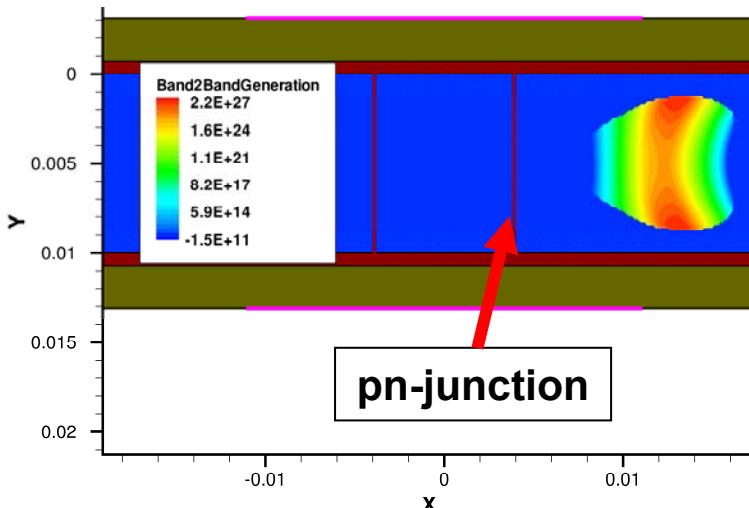
$$\tilde{n} = n \left(\frac{n_{i,\text{eff}}}{N_C} \right)^{\frac{|\nabla E_{F,n}|}{F}}$$

Non-locality is crucial, as it e.g. prevents tunneling where no final states are available. In a MOSFET this usually happens close to the gate oxide interface, i.e. in a region where the electric field F in the semiconductor becomes maximal. The “critical field strengths” are given by

$$F_C^\pm = B(E_{g,\text{eff}} \pm \hbar\omega)^{3/2}$$



- No direct experimental verification of the B2B rate in Si exists
- Calibrations based on GIDL data rely on correct modeling of lateral dopant diffusion

22nm UTB DG SOI (*PULLNANO* template)

- The non-local B2B model accounts for the “dark space” near the oxides. This reduces the rate compared to a local B2B model.
- Maxima of the electric field do *NOT* occur in the pn-junction, but right to the drain-side gate corners (largest voltage drop).
- => the B2B rate is also located right to the gate corners and *NOT* at the metallurgical pn-junction.
- The B2B rate cannot be changed much by changing the steepness of the pn-junction.

Incoherent scattering

Example: acoustic phonon scattering

Assumptions: Bulk phonon dispersion, bulk coupling constants, EMA

Simplifications: High-T appr. $\hbar\omega_q \ll k_B T$, lin. dispersion $\hbar\omega_q = c_s q$

→ self-energy $\Sigma_{ac}^<$ becomes local in space

$$\Sigma_{ac}^<(r, r', E) = \frac{\Xi^2 k_B T}{\rho c_s^2} G^<(r, r', E) \delta(r - r')$$

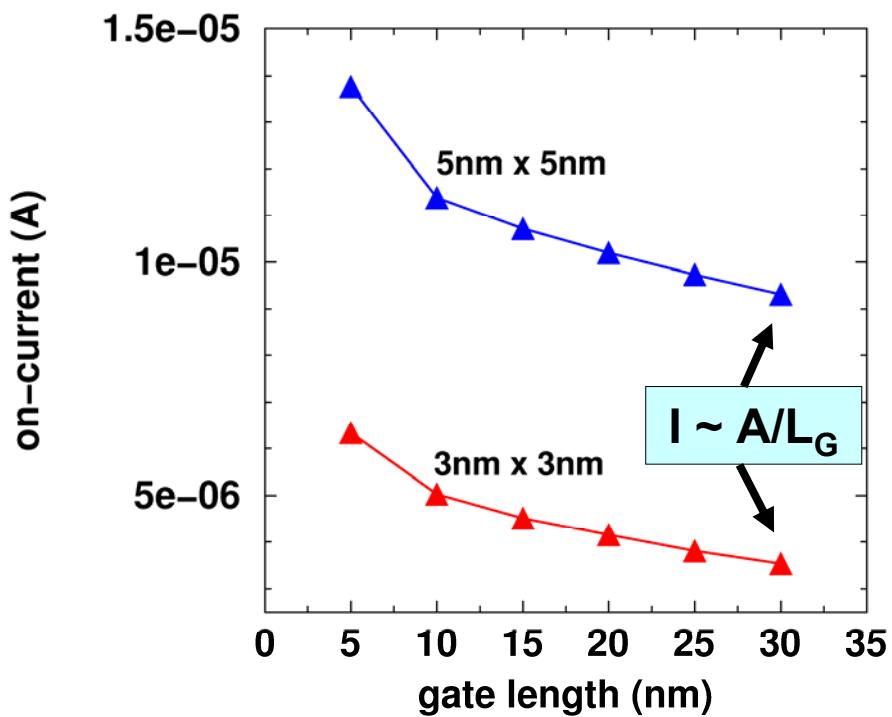
$G^<$ requires G^R (full size): $G^< = G^R (\Sigma_S^< + \Sigma_D^< + \Sigma_{ac}^<) G^A$

$$(E - H - \Sigma^R) G^R = 1$$

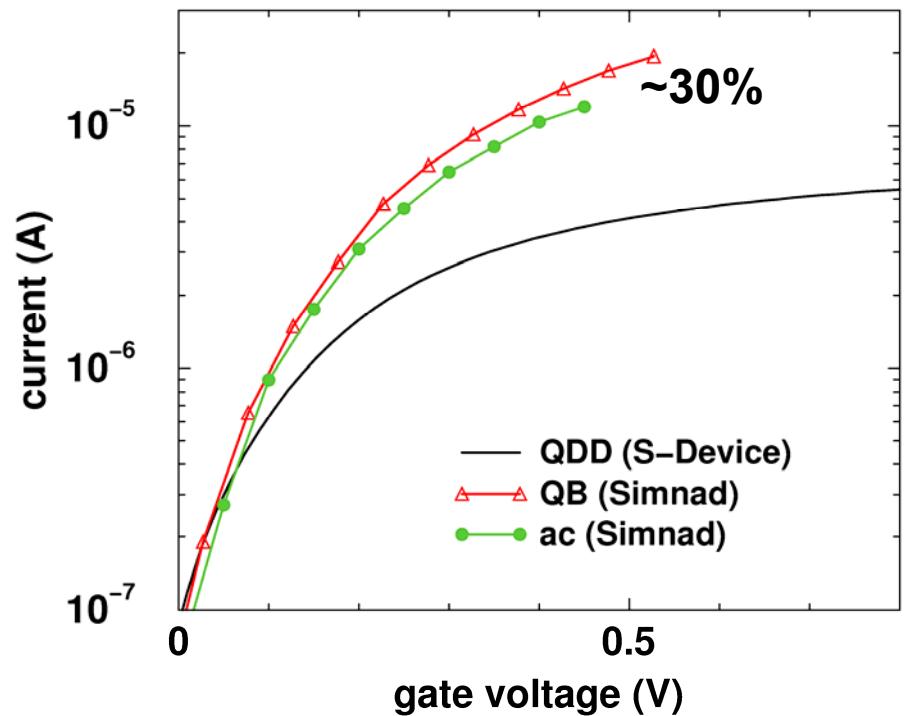
Elastic appr. $E \pm \hbar\omega_q \approx E \rightarrow \Sigma^R$ simplifies to

$$\Sigma^R(r, r', E) = \frac{\Xi^2 k_B T}{\rho c_s^2} G^R(r, r', E) \delta(r - r')$$

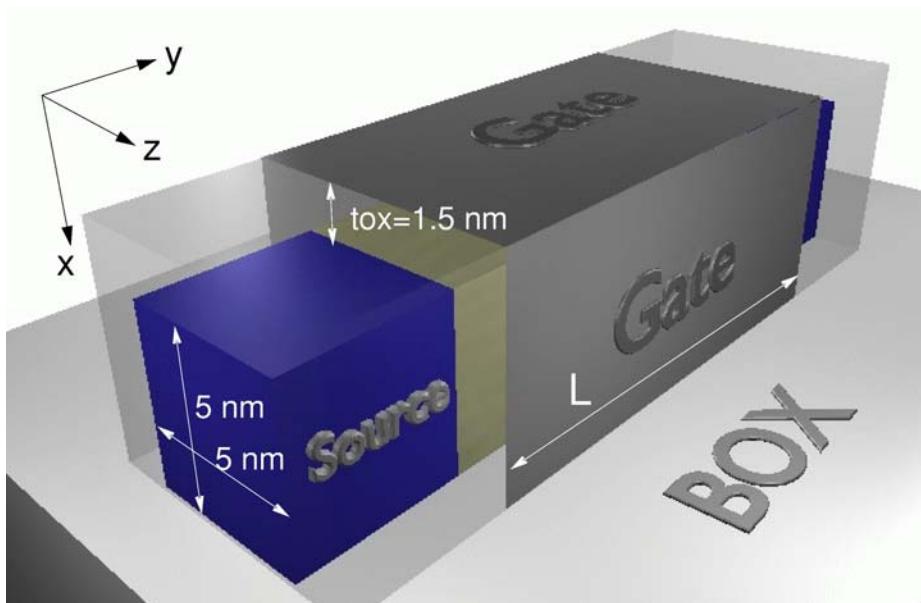
Scaling @ $V_{GS}=0.5V$, $V_{DS}=50mV$



TG $5 \times 5 \times 25 \text{ nm}^3$ NW FET



Example: Triple-gate 5nm x 5nm NW FET



TGNW-FET (courtesy EU SINANO project)

Gate length: 25 nm (65 nm technology node).

Channel Cross-Section : Square ($5 \times 5 \text{ nm}^2$).

Source/drain extensions: 10 nm.

Oxide parameters: material is SiO_2 ($k \sim 3.9$).

Field Oxide Thickness : 1.5 nm.

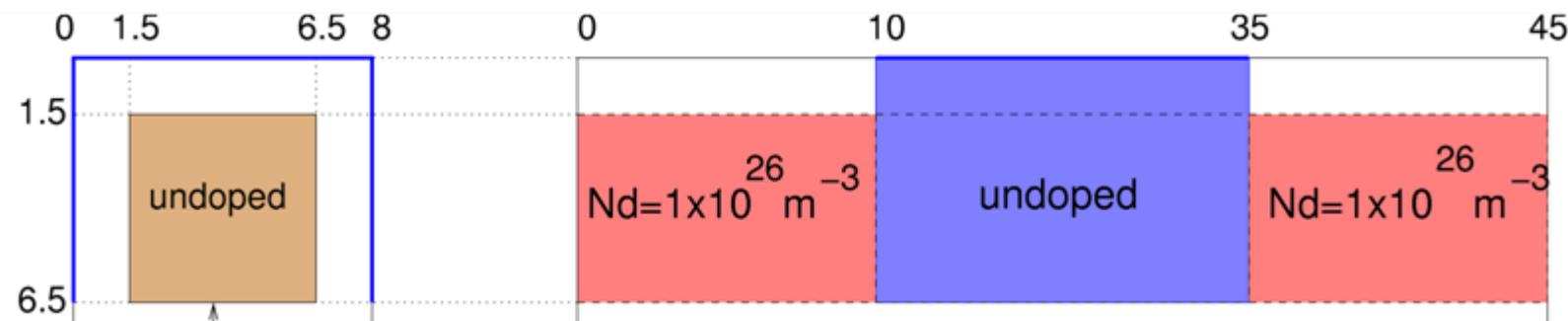
Buried Oxide Thickness : 150 nm.

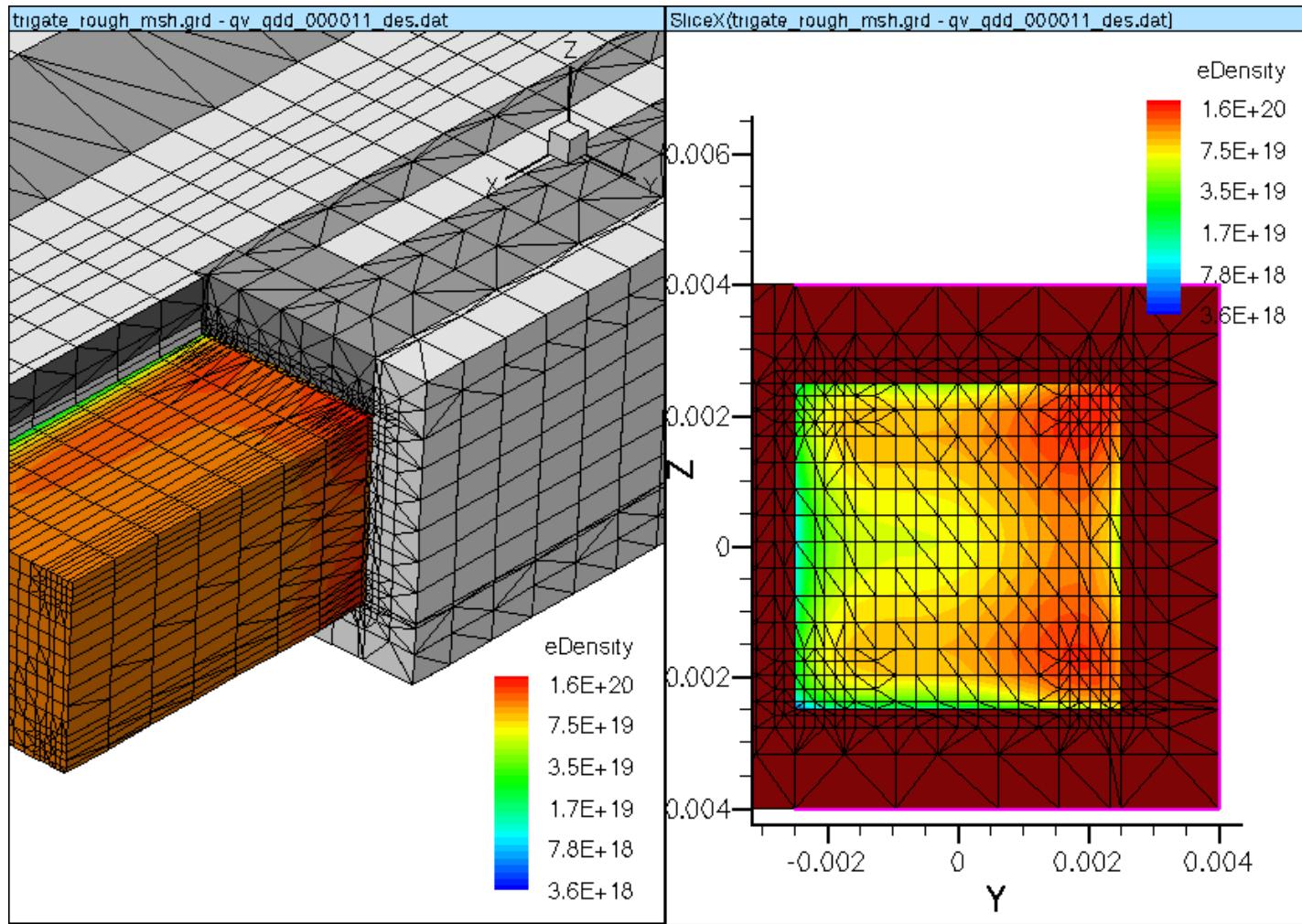
Gate electrode work function: 4.1 eV.

von Neumann boundary conditions at S/D ends.

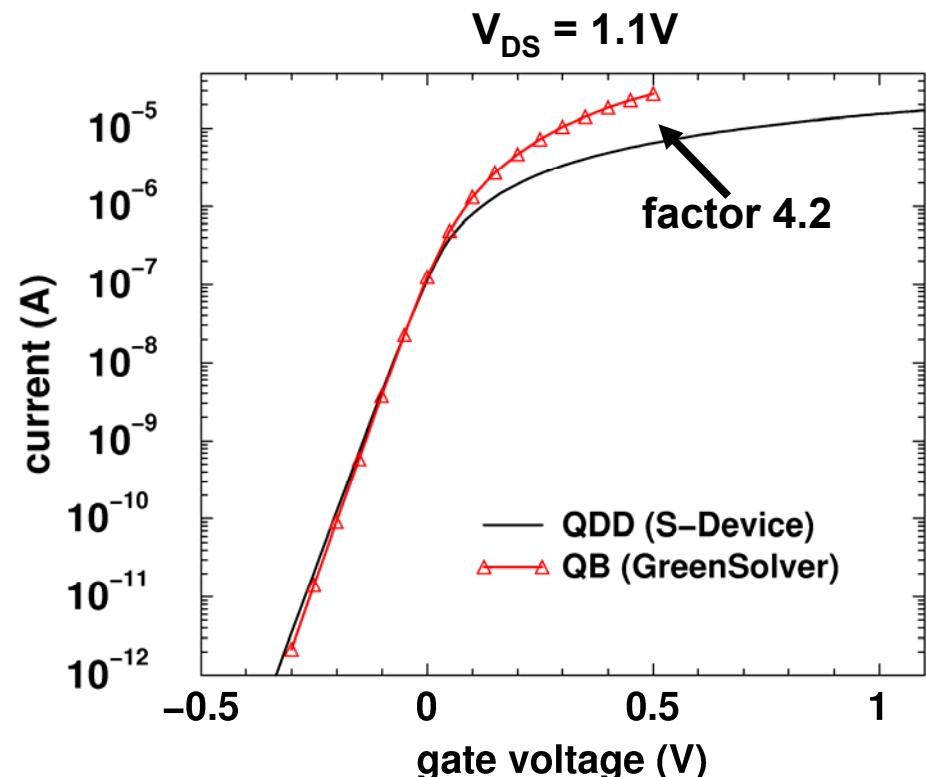
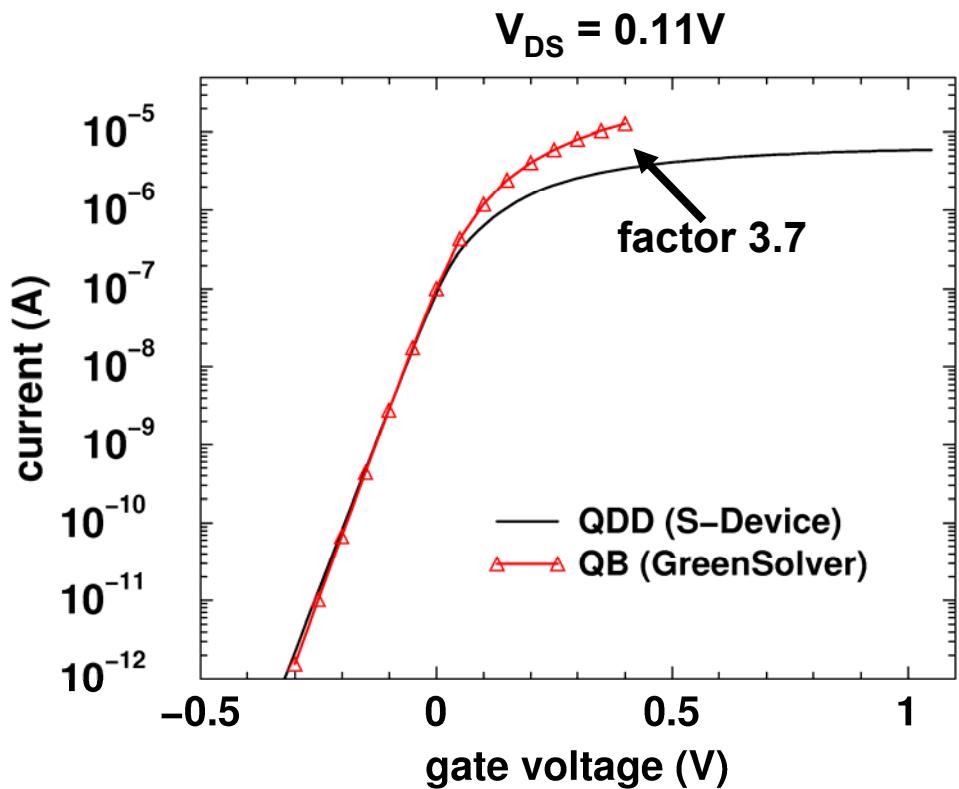
Doping specifications:

Substrate undoped, source and drain: $N_d = 10^{20} \text{ cm}^{-3}$.



S-DEVICE mesh for the TGNW-FET and electron density at $V_{GS} = 1.1V$ 

Comparison of currents



Conclusion

- DG and 1D-SP are now state-of-the-art TCAD tools for the modeling of quantum-mechanical confinement effects
- DG is most practical method, because: (i) quantum-corrected dissipative transport scheme, (ii) full Newton, (iii) multi-dimensional
- Atomistic, full-band approach to simulate Si nano FETs is possible (and justified) up to $5 \times 5 \text{ nm}^2$ cross sections (wire) or 5 nm body thickness (UTB)
- A variety of effects (channel orientation, strain, surface roughness, S-D tunneling, gate tunneling) can be studied in the quantum-ballistic limit
- Quantum-ballistic treatment overestimates the ON-current, because (i) incoherent scattering remains important, (ii) source-drain tunneling artifact
- For *ballistic* transport use WF formalism and not NEGF, because much more efficient!
- Challenges: Incoherent scattering, CPU time